THE BAKHSHĀLĪ MANUSCRIPT

A Study in Medieval Mathematics

INDIAN HISTORICAL RESEARCHES

THE BAKHSHALI MANUSCRIPT

Early Hindu Mathematics A Study in Mediaeval Mathematics

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Vol. 24 (ii)



First Published 1817 This series 1987

Published by RANI KAPOOR (Mrs) COSMO PUBLICATIONS 24-B, Ansari Road, Darya Ganj, New Delhi-110002 (India)

Printed at M/S Mehra Offset New Delhi

PREFACE.

In order to correct an impression that certain passages in this volume might convey unless distinctly qualified, I must here refer to my indebtedness to the late Dr. Hoernle. Indeed, a considerable part of the analysis of the MS, is really his work,* and by his preliminary survey of the manuscript my task was considerably lightened. It was at Dr. Hoernle's special request that I undertook to carry on the work he had started, and he handed over to me most of the material he had himself prepared. Had he lived a little longer I should, no doubt, have had the benefit of further help from him, and this volume might have been issued as our joint work. Dr. Hoernle's lamented death prevented that plan being carried out; and unfortunately my views are so often opposed to those that where held by Dr. Hoernle that it would hardly be proper to make him a participator in them.

I am much indebted to Bodley's Librarian for special facilities that enabled me to examine the original manuscript under the most favourable conditions; to the Oxford University Press for their most excellent work in preparing the photo graphs of the manuscript and the collectype reproductions of the text; and to the Manager, Government of India Press, Calcutta, for the care and skill with which the transliteration has been printed.

G. R. KAYE.

Banham, Attleborough, Norfolk.

^{*} Sections B, G, H, K and L are almost wholly the work of Dr. Hoernle, who also transiterated about half of the leaves of the MS. References to his published papers on the MS. are given on page 2.

PART III.

1.—The Text Re-arranged.

State Control Library, Govt. of West sengal, 86-A, B. T. Read, Calcutta-700086

Quotations in the text are distinguished by daggers \(\tau \).... \(\tau \), and abbreviations by \(\text{o} \) superscribed. Asterisks attached to numbers denote change-ratios (See \(\text{o} \) 103). In the foot-notes angular crotchets \(\text{o} \) indicate that the portion enclosed formed part of the argument or was implied in the original text, but is now missing.

On pp. 13 and 14 of Part I are tables equating the Bodleian Library order with the revised arrangements.

The notes attached to the revised arrangement are very crude and are presented with considerable diffidence; but they are the result of much labour and will possibly save the student of the MS a good deal of spade work.

G. R. K.

Owing to Mr. Kaye's unfortunate death, the last proofs of this part have been prepared for the press by Mr. K. N. Dikshit, Deputy Director General of Archaeology for Exploration, who has also made a few emendations.

A 1.

yatra y .g bhāgam chai	iva kārayet kshetra vaipulya 40 recto.
prishthā śata-dvayam chaiva uchare ś	
	amcha bhavet chānam bhakti sthāne зы гессо.
r dhā sapta pamchānām tr	
vāhasya kim ka tatrā mama	
sthāpanam kriyate	·
kshetram 100 15 12 10 7 5	karanam kshetra
	esha shat
6210 esha vāhasya kāṇḍa pramāṇam	guņitā jātā 40° verso. śake mūlyam <i>karta</i> vyam
adha chchhedam chatus sashthi 1	a sutha dvi trimsabhi mandalakai 39 veno.
tallika esa chchhedam bhavati yath	e chchh kāryā svtha tala
kriyā udāharanam talasya :	mekam ta dvā sashti satānārir
daśādhīkānām kim mulyam : talla	tale a° 38' verso,
1 rū 1 mūlye 6210	

^[38-40.] Plates xxvi and xxvii exhibit some sixteen fragments all placed out of order. Some of these have now been preced together. (See the illustration facing page 4.)

This grouping is not final because some of the fragments consist of portions of two or more leaves stuck together, and until these are separated no exact order can be achieved.

We should naturally expect the first leaves of the manuscript to be comparatively more damaged than those in the middle of the book, and the 'find order' and the writing indicate that these fragments are probably portions of early leaves but neither of these criteria is rigorous and it is quite possible that we have placed the fragments in their wrong places.

^{[38-40} recto.] These fragments appear to relate to a geometrical problem concerning an area whose width (naipulya) is increased.

^{[38-40} verso.] A fragment of a problem connected with the area of a circle or the surface (tala) of a sphere. The phrase saka valuage kinds promise on the change-ratio 64 is possibly connected with a "square measure." See Part I §108(b). The number 6210=33-230 is said to be the product of certain quantities.

A 2.

ksh			. daśa	chatur-daśa triti-	39º recto.
yasya chaturthasya		. bhāgās ta	syaiva pamch	ama	40º recto.
bhāgā vimsas cha da yam satam sarve misrāp				jna	38° recto. 40° recto. 39° recto.
				unitā jā trairāsikena 00	
dhanam 1200			1		
	•	pha° 144			38° verso.
	•	pha° 16.			39 ^d verso.
		pha° 180			40° verso.
	20	pha° 200			

A 2. [38-40.] The writing on the two sides differs (recks α₁, verso α₈) and there are other indications that the fragments consist of portions of two leaves at least.

A 3.

whence $(x+y+z)^2=225$ and x+y+z=15. The answers are x=4, y=5, z=6. The writing is classed as α_2 .

A 3. [38-40 recto.] See the plate facing page 4. The meaning is not clear, but x(x+y+z)=60 y(x+y+z)=75 x(x+y+z)=90

A 3-contd.

sthāpya 4 pa 5 ain 6 15 15	39 recto.
$egin{array}{c c c} 4 & 5 & 6 \\ 15 & 15 & 15 \\ \hline \end{array}$	
4 5 6	
15 15 15 15 15 15 15 15	
kriyate chaturbhi	panichabhish shadbhi g prathama
rāśi yoga 60 vartyam 4 madhū gh	ata dvitiya pańktyā yoga 75 38° meta
vartyam 5 pānīyam tritīya par	nktya kriyate yogani 90 vartyani jātani 15
6 payasām	
	gunetu eko kritam 40' verso.
śatatraya m pamchabhi ≠ purushair la	bdhaii kim adyaii prathamaii dhanam
120 2257 n	aii t śeshe kshepa
16 anenātra bhāga 32 labdha	2 40 pha 39 verso. 12 pha 120
labdher bhāg . $\begin{array}{cccccccccccccccccccccccccccccccccccc$	abdha kshepam d <u>ii 60</u>
prakshepa yukti 30 vibhaktam 1 30	
28 evam 60	

A 4.

i.	dvigunam cha tri-ūna cha tritīvasva dhanam bhavet 54 veno.
	samyutam eka-vimshatibhi z . krito dināraistu rai ya
	tu dani sā prithag vachah :
	karanam 📗 yasya padam na jñāyate etat prathamasya
	dhanam
ii.	
	2+
	dhanam 1 2 4 8 1 1 1 1
	yātā tayor yogaviyo kṛitāni rāshayaḥ
	2 1 2+ 9+ dri° 82 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	bhājyā hitveti tatra uttara rāśi uttaram riņam jātam
	(b) sūtram (c) jatam 76 esha prathamasya
A 4.	[54.] I colo 54 possibly consists of two leaves, or rather fragments of them, for there are ten pieces. The writing on the two sides differ—that on 54 recto may be classed as a_1 and that on the left side as a_2 and in this respect the leaf resembles fol. 35°. There is a characteristic ye at the bottom of 54° verso which is also found on 29° recto et verso. [54° verso.] Seems to contain portions of a sitra, an example and solution. The phrase diagnam cha triuma seems to be referred to on fol. 35° recto but there we have tryuna with a particularly notoworthy conjunct tryu (see table IV, 5 part ii). The term hasing(atam) on 54° recto (not necessarily connected with 54°) occurs only once more on fol. 1 recto. [54° recto.] The phrase tayor yogaviyo also occurs on fol. 35° verso.
	A 5.
	kasmat kāranā tayor yogaviyogasy āviyogas
	bhājitā purusha 15 anena bhaktvā dhanani 9 padvaya
	sahitam
	"
	eta dviguņam 3 dviyuta yasya 35' verso.
	dhanam tadeva svārdham 3 asyārdham 1 yutam nyāsa 1 2
А Б.	[35'.] The writing is different on the two sides (α ₁ and α ₂) and possibly the fragment is a portion of two leaves stuck together. The phrase bhājitā purusha occurs on 51' recto.

A 6.

bhājitā	hitvā ta	trottarā 1	1	yutanı	2	$\begin{array}{ccc} 1 & 3 \\ 4 & 2 \end{array}$	3 1		· 51º recto.
9 .	$\operatorname{esh}ar{a}\phi$.	ītha bhājitā	pur	ıshah 1	3 2	$\begin{pmatrix} 3 \\ 1 \end{pmatrix}$	eshān	h sadriś	9 35° recto.
19	dhanam 19 1	anena guņi	itam jā	itam	esh	a pratha	ımasya	dhanari	1
	. dvigunan	dvi-y	utani	14	eta o	lvitīyasy	7a		•
g uņam	21 dvi-	guņam 42	try-	ūņam 3	9 _	eshah n	yāsah		
pratya	d	laśam agravrin	dānāri	chatur-da	śa ek	onachat	āri msa	l ta	t
pād	-ārdha tri-bl	nāgā		,					
	1 pha°	4 evam di	° 21	esha pra	shņa (etair .			
with folio 54. The frag Apparently a	Fol. 35° is in α_1 we mentary contents are	nition is uncertain but the riting. See the plate face not clear. We have 1 on which the solution cleaner.	cing page +1=2; }	4. (Read 51 resto + 출 + 8 = 및 ; 19/4 =	B, not t = 4 and	$\frac{2.3.\ (12+2)}{2}$	- 3 - 39		
udā			<u>. 1</u>	<u>6 .</u> .		yoga	111	śeshā ¢	51° verso.
purusha	bhājitā pur	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1 5 es	hāṁ sad ri sl	ne yut	im kritv	ā yutā	37 60	35° verso.
b hā jitā	60	esha	gavāsv	a mahishī	praty	aika śāl	leshu b	hāga	•
	1 śā°	180 gā°	1 4	phalam	45		• •		
	1 śā° 1	180 asvā° 1	1 6	phalam	30	4+	26		
	1 śālā 1	180 mahi°	1 5	phalam	36	5+	9		
				1					

[51] & 35] useso.] The writing is of the α_1 class. The 'find order' of folio 51 is 37 while that of 35 is not known. The position is vary uncertain. What remains of the problem is $\frac{1}{2} + \frac{1}{6} + \frac{1}{6} = \frac{1}{11} \times \frac{1}{4} = 180$ 1 enclosure: 180 cows :: $\frac{1}{6}$: 45? subtract 6=38.

1 , : 180 horses :: $\frac{1}{6}$: 36 subtract 4= 26.

1 , : 180 buffaloes :: $\frac{1}{6}$: 36 subtract 5=29?

A 7.

purusha sa 4 anena bhājitā-r-labdhā sya bhavati 12 14 15 ekatram 54 udā° kaśchid rājā dade dānam sapta – pamchāśakam budha pamchā pravakshyāmy = anupūrvaśah dvi-guṇa dvi-guṇam chaiva rūpa rūpottare prathame prāptam kim prāptam apare jane 0 1 2	51*
purusha sa 4 anena bhājitā-r-labdhā sya bhavati 12 14 15 ekatram 54 udā° kaśchid rājā dade dānam sapta – pamchāśakam budha pamchā pravakshyāmy = anupūrvaśah dvi-guṇa dvi-guṇam chaiva rūpa rūpottare	1 1 1 1
14 15 ekatram 54 udā° kaśchid rājā dade dānam sapta - pamchāśakam budha pamchā pravakshyāmy = anupūrvaśah dvi-guṇa dvi-guṇam chaiva rūpa rūpottare prathame prāptam kim prāptam apare jane 0	m yuta 6 48 seshāφ
udā° kaśchid rājā dade dānam sapta – pamchāśakam budha pamchā pravakshyāmy = anupūrvaśah dvi-guṇa dvi-guṇam chaiva rūpa rūpottare	-labdhā sya bhavati 12 13
paṁchā	
dvi-guṇa dvi-guṇam chaiva rupa rupottare	apta-pamchāśakam budha
	pravakshyāmy=anupūrvaśah
0 1 2	rūpa rūpottare
dri 329	kim prāptam apare jane
1 3 9 27 81 karaņam uttar tatrottara rāśīnām yoga 87 esha dha drishyā śodhanīyā jātā 242 purusha 1 3* 9 27 81 yoga 121 anena jātā 2 esha dv prathamasya dhanam 2 6 18 54 162 uttara rāśī samyutam jātam	2
1 3 9 27 81 karaņam uttar	dri 329
drishyā śodhanīyā jātā 242 purusha 1 3* 9 27 81 yoga 121 anena jātā 2 esha dv prathamasya dhanam 2 6 18 54 162 uttara rāśī samyutam jātam	11
drishyā śodhanīyā jātā 242 purusha 1 3* 9 27 81 yoga 121 anena jātā 2 esha dv prathamasya dhanam 2 6 18 54 162 uttara rāśī samyutam jātam	rottara rāšinām voga 87 esha dhanā
27 81 yoga 121 anena jātā 2 esha dv prathamasya dhanam 2 6 18 54 162 uttara rāšī samyutam jātam	
prathamasya dhanam 2 6 18 54 162 uttara rāšī samyutam jātam	
2 6 18 54 162 uttara rāšī samyutam jātam	java 2 esila uyau
2 15 48 147 444 eshām	

^{[5]°} verso.] expressed by

 $[\]begin{array}{l} t_1 + 3t_1 + 3t_1 + 3t_1 + 3t_1 \\ t_1 + \frac{3}{2}(t_1 + t_1) + \frac{3}{2}(t_1 + t_2 + t_1) + \frac{3}{2}(t_1 + t_2 + t_1 + t_2) \end{array} \} = 329 \\ \text{Set } t_1 = 2 \text{ then the first series becomes } 242 \text{ and the second } 87 \text{ and the combined series is } 2 + \frac{1}{4} + \frac{1}{4} + \frac{1}{4} + \frac{1}{4} + \frac{1}{4} = 339. \\ \text{See also page } 47. \\ \end{array}$

A 8.

. tvedam jātam 3 anena chālimsa guņaye 52 recto. jātā 120 vam śurānām 11 pratyaya trai-rāśikena 1 vam 120 1 1 10 1 120 vam 1 vam 120 30 1 1 dhanā sva-m-ardho sanisoddhya . . . chottariyakam udā° tat seshā paṁchamo bhāgo śata dvayaṁ 📗 aśītyādhikam dhanam chaiva kim ādyam prathamam dhanam 11 · · · . . . asya dvayānām śatānām pāda . . . rdham 52 verso. śatam bhavati 150 atrāpi pamcha bhāga 30 || evam pamchamī jātī karaņam krita . . . 280 | amśa vuti bhaktam 28dhanu 280 gunitam jātam 400 esha phalam bhavati | [52 reto.] i. The writing on both sides is α_1 and exhibits examples of the 'sickle-shaped' medial I and I. The 'find order' is 57. It is possible that 52 reto gives parts of the solution of the example on 51 reto which would make that page the reverse, but I doubt the connexion. What is left of the solution means $\mathbf{x}(\frac{1}{16} + \frac{1}{4} + \frac{1}{4}) = 57 \quad \text{or } \mathbf{x} + \frac{1}{4} = 57 \quad \text{$ ii. The example, which is continued on 52 mass, may be expressed by $x(1-\frac{1}{2})(1-\frac{1}{2})(1-\frac{1}{2})=x-280$ whence $x=\frac{280}{38/40}$

A proof follows: *\frac{10}{5} = 200 and 400 - 200 = 200; \frac{100}{5} = 50 and 200 - 50 = 150; \frac{120}{5} = 30 and 150 - 30 = 120; and 400 - 120 = 280. Again $\frac{1}{2} + \frac{1}{4} (1 - \frac{1}{2}) + \frac{1}{4} (1 - \frac{1}{4}) (1 - \frac{1}{4}) = \frac{1}{2} + \frac{1}{8} + \frac{1}{40} = \frac{16}{66}$ and $280 \times \frac{1}{2} \frac{1}{6} = 403$.

A 9.

	· · · · · · · · · · vinirdiset	recto.
udā°	dhana	
	ādya dvitīya yonmiśram dhanam tatra ttrayodashah	
	dvitīya tritīya yonmi	
	ādya tritīya yonmiśram dhanam pamchadaśa smritah	
	ekaikasya dhanam chchhiche katthyatām mamah	
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
	. prathaman yasya tatrechhā pamchah 5 tat prathama 29	recto.
	14 15 tadādīś† śodhayet kramāt † àdi eta	
chatur-das	śabhi śodhya śesham 6 etat pamcha 29°,	recto.
• • •	dvitīya yonmiśram dhanam 294	ver so.
dvitīy	a tritīya yonnuśram dhanam sapta-dasha smritah	
tritīy s	aś chaturthayo	
chatu	φ pamchaka miśram tu dhanam ekona-vimśati	
prath	ama tatra cha	
ekaik	asya dhanam kimssyād vechchhi	
	16 17 18 19 20 1 1 1 1 1 1	verso.
karanem	ichchhā dani†sodhayet kramat† tatrādi 16	
śud	tritīyāyam śoddhya 7 chaturthāyam śoddhya 12 pam 28 ·	V6r≱o.

The phrases ichchhā . . . and śodkayst kramāt are quotations from a lost sière.

 ^[29.] Folio 29 consists of six fragments, of which only the four larger ones need be considered at present. The correct order is d, b, c. Fragment b fits under d and c under b while a goes with folio 27. See the plate facing page 4.
 [20 d, b, c recto.] The problem and its solution here partly preserved may be represented by x₁+x₂=13, x₂+x₃=14, x₂+x₁=15. If x₁=5 then x₂=8, x₃=6 and x₁+x₁=11 and the correct values are found from x₁=5+¹⁶⁻¹¹/₁₃=7, x₂=13-7=6, x₃=8. The phrase " sodhayet kramat " recurs in the next example and is a quotation from a lost stars.

The phrase somework remains recurs in the rest example and is a quotested from a not seed of the same phraseology as the previous one. It may be represented by $x_1+x_2=16, x_2+x_3=17, x_3+x_4=18, x_4+x_5=19, x_5+x_1=20. \text{ If } x_1=10, x_2=6, x_3=11, x_4=7, x_5=12 \text{ and } x_5+x_1=22 \text{ Therefore the correct value of } x_1 \text{ is } 10+\frac{20-23}{2}=9, x_2=7, \text{ etc.}$

A 10.

masya dhanam esham anukkramena 27 verso.
pūrvokt
9 pra° 7 dvi° 10 tri° 8 cha° 11 pam° 7 dvi° 10 tri° 8 cha° 11 pam° 9 pra°
yutam jātam pratyaik 16 17 18 19 20
evam sarvatra kārayet
karaṇam †pṛithak rūpam vinikshipya+ pṛithak rūpam kshiptam jātam .27 recto. † bhyāso† tatra guṇa 3 4 abhyāsam 12 † rūpahīnam † 1
abhyāsā chatuφ pamchakā atra kshiptani jātani 15 16
eśa trigun $t ilde{a}$ mūla ni chatu ϕ pamcha $oxed{5}$ 4 $oxed{4}$ esha .
• • • • • • • • • • • • • • • • • • • •
sūtram guṇau ka dhanam 29 recto. guṇ ābhyāso rūpa hīnam labdhan rū

A 10. [27 verso] gives the answer of the problem given on fol. 29 verso, namely x₁=9, x₂=7, x₃=10, x₄=8, x₅=11, and the sums of the pairs are 16, 17, 18, 19, 20. (For general discussion see § 78, Part I.)

^{[27} recto.] Solution of a lost problem which may have been $xy-3x-4y\pm 1=0$ of which solutions are: $x=\frac{3^44-1}{2}\pm 4=15$ y=3+1=4; x=4+1=5, $y=\frac{34+1}{2}+3=16$. The quotations are from a siltra very much like the one that follows.

The phrase prithak rūpam vinikshipya 'having added unity in each case' appears to be a quotation from a lost sūra.

[29a] is wrongly placed on plate XX. It should some directly under 27, for of the letters—num sarraira kāraysi, the top portions are on 27 verso and the bottom on 29a recto.

A 11.

```
bhyasa
                                                                 rū . . . . . . chaturguņam pamchaguņam hastagatam 1 moto.
                                                1
              dhanam ja
                                                                                           . . . . . . pamchagunam 25
              navama sütram 9
    u sūtram || guņau prithag rūpayutau yāchanā yukti samguņāh ||
                                                     guņanena guņe . . rūpahīnena bhājitau
                                                      viparīta yāchanā kshiptau guņaśāster ayam vidhih
                                                                                                                                                                                                                     II
             evam sūtram || dvitīya patre vivaritāsti ||
             dasama sūtram 10 jį
                                       amśām viśoddhya chchhedebhya kuryātat parivartanam
                                                                                                                                                           dhanānviśa vinirdiśet
                                                    . . . sāsyam tata projihya
            udā°
                                   ll pamchānām vaņijā madhye
                                                                                                                                            mani vikriyate kilah
                                              tatroktā maņi vikrīta maņi mūlyam kiyad bhavet
                                              ardha tri-bhaga padansam pamcha-bhaga sodamsa cha
                                                      . . . . tato projjhvah | sadrišam krivate . . jātā 1 verso.
            | 120 | 90 | 80 | 75 | 72 | tatra projjhya† jātam | 120 | 90 | 80 | 75 | 72
            60 60 60 60 60
            eshām yoga krite jāta 437 ato . . . sesham 377 esa mani mūlyam l
            [1 recto.] The position is uncertain. The 'tind order' (33) places this leaf next to the fragments of folios 27, 29, 38, 39, 40. The writing is \alpha_s (there is a 'sickle' i). The numbered sitras seem to place the leaf fairly early but they are not a very safe criterion. Note (ii) below seems to connect folios 1 and 27.
                     (i) Nothing intelligible. It ends the earliest numbered sutra preserved.
                     (ii) I have not yet made out the meaning of this satra. Compare the opening phrase with the quotation on 27 recto. The metre
             is irregular. The reference to the second leaf is possibly to folio 27.

(iii) The silva means change \frac{a}{b} to \frac{b}{b-a} and quotations from it are given on folios 1 verso and 2 verso.
                      (iv) The example is solved on 1 verso and 2 recto and appears to have been somewhat as follows:
                              The combined capitals of five merchants less one-half of that of the first, one-third that of the second, one-fourth that of the
                                      third, one-fifth that of the fourth, or one-sixth that of the fifth is equal to the cost of a jewel. Find the cost of the iewel and the capital of each merchant.
                    [1 verso.] This appears to give part of the solution and proofs of the question on 1 recto. Since < \sum x - \frac{1}{4}x_1 = \sum x - \frac{1}{4}x_2 = \sum x - \frac{1}{4}x_1 = \sum x - \frac{1}{4}x_2 = 0, we have \frac{1}{4}x_1 = \frac{3}{4}x_1 = \frac{1}{4}x_2 = \frac{1}{4}x_3 = \frac{1}{4}x_4 = \frac{1}{4}x_5 = \frac{1}{4}x_
A 11.
                              If k=60 then c=377 and x_1=120, x_2=90, x_3=80, x_4=75, x_5=72.
                      Then follows a 'proof' which may be expressed by
                                                                                     90+80+76+72=317 and 317+1*0=377

120+80+75+72=347 , 347+\frac{1}{2} = 377

120+80+76+72=387 , 357+\frac{1}{2} = 377

120+80+80+72=382 , 362+\frac{1}{2} = 377

< 120+90+80+75=365 , 365+\frac{1}{2} = 377 >
                      † Compare with entra 11 on 1 recto
```

A 11-contd.

chaturthām sanka sarvasvam prathamasya sanka ardham . . . 90 | 80 75 | 72 chaturnām yoga 317 prathamārdheņa sashtibhir yutam 377 esa prathamasya dhanam prathama dhanam tritiva chaturtha panichamasya dhanam sarvasvam 347 dvitīyā tri-bhāgam 30 eśa yutam 377 esa dvitīyasya dhanam bhavati puna prathama dvitiya chaturtha pamchama . . sarvasvam 357 tritiyasya pādam 20 esa yutam 377 esha tritivasya dhanam bhavati punar api prathama dvitiya tritiya pamchamasya 362 chaturthasya pamchabhāga 15 esa yutam 377 esha chaturthasya dhanam bhavati |

A 12.

Sya dhanam bhavati atha pratha . . . · · · tyaniśashti śesharh 377 2 recto. 120 atha dvitīyasya evam 377 dvitivasya bhavati 11 30 80 **7**5 120 evam 377 tritīvasya dhanam bhavati atha tritiyasya krivate 90 20 75 72 120 evam 377 chaturthasya dhanam bhavati chaturthasya kriyate 90 80 15 72 pamchamasya kriyate | sthapanam 120 evam pamchamasya 90 80 75 12

A 12.

^{[2} recto.] i. This appears to be another 'verification' of the example on 1 recto et verso; and means

A 12—contd.

esh			
udi	ā°	anyonya vidita vibhavam vanikdvayam	
tŗi		dalam tatha	
		$egin{bmatrix} 7+&3+&5+\ 12&12&6\ 12&12&6 \end{bmatrix}$	2
†aı	mśām	viśoddhya† visodhayet rinam sthitam esha kriyate	
1	19 12	7 11 †kuryātat parivartanam† 12 4 6 chchhede 4 6 19 7 11	
٠		jātam asya 924 836 798 projjhya jātā 924 836 798 1463 1463	
		handan harm and an all and an all and an all and an all and and an all an all and an all and an all and an all and an all an all and an all and an all an all and an all an	
esl	hām yu	tim kriyate jātā 2558 chchheda projjhyam 1095 etan	
ms 	ii. This is [2 verso.] (x-(1+2)x	tim kriyate jātā 2558 chchheda projjhyam 1095 etan lyam possibly the question solved on 2 verso. The general meaning is: since $x_0+x_0-(\frac{1}{2}+\frac{1}{4})x_1-x_1+x_0-(\frac{1}{2}+\frac{1}{4})x_2-x_1+x_1-(\frac{1}{2}+\frac{1}{4})x_2-o$, or $\Sigma x-(1+\cdot)x_1$, $\Sigma x-(1+\frac{1}{4})x_2-c$, whence $\frac{1}{4}x_1-\frac{1}{4}x_2-\frac{1}{4}x_3-\frac{1}{$	_
ms ——En	ii. This is [2 verso.] (x-(1+2)x x x ₁ -924, I do not,	tim kriyate jātā 2558 chchheda projjhyam 1095 etan lyam cossibly the question solved on 2 verso. The general meaning is: since $x_0+x_0-(\frac{1}{2}+\frac{1}{4})x_1=x_1+x_0-(\frac{1}{2}+\frac{1}{4})x_2=x_0+x_1-(\frac{1}{2}+\frac{1}{4})x_2=0$, or $\Sigma x-(1+x)x_1=\Sigma x-(1+\frac{1}{4})x_2=0$, whence $\frac{1}{4}x_1=\frac{1}{4}x_2=\frac{1}{4}x_3=\Sigma x-0$ and $\frac{\sum_{k=0}^{\infty}x_k=\frac{1}{4}+\frac{1}{4}+\frac{1}{4}\frac{1}{4}=\frac{1348+1}{1463}}{\frac{1348+1}{4}}$. Settling $\Sigma x-0=1463$ we $x_0=836$, $x_0=798$; $\Sigma x=2538$ and $c=1095$ 'which is the price of the jewel.' lowever, understand the form of the first statement: but see fol. 65 verso where $\frac{190}{40}$ means $\frac{190}{42}$. is deadly a and kuryatat parivarlanam are quotations from saltra 11 on fol. 1 recto.	_
ms ——En	ii. This is [2 verso.] (x-(1+2)x x x ₁ -924, I do not,	tim kriyate jātā 2558 chchheda projjhyam 1095 etan lyam possibly the question solved on 2 verso. The general meaning is: since $x_3+x_3-(\frac{1}{2}+\frac{1}{2})x_1=x_1+x_3-(\frac{1}{2}+\frac{1}{2})x_3=x_3+x_1-(\frac{1}{2}+\frac{1}{2})x_1=0$, or $\Sigma x-(1+\tau)x_1=\Sigma x-(1+\frac{1}{2})x_3=0$, whence $\frac{1}{12}x_1=\frac{1}{12}x_2=\frac{1}{12}x_3=\frac{1}$	_
ms ——En	ii. This is [2 verso.] ix—(1+2)x o x,—924, I do not, † amidm :	tim kriyate jātā 2558 chchheda projjhyam 1095 etan lyam cossibly the question solved on 2 verso. The general meaning is: since $x_0+x_0-(\frac{1}{2}+\frac{1}{4})x_1=x_1+x_0-(\frac{1}{2}+\frac{1}{4})x_2=x_0+x_1-(\frac{1}{2}+\frac{1}{4})x_2=0$, or $\Sigma x-(1+x)x_1=\Sigma x-(1+\frac{1}{4})x_2=0$, whence $\frac{1}{4}x_1=\frac{1}{4}x_2=\frac{1}{4}x_3=\Sigma x-0$ and $\frac{\sum_{k=0}^{\infty}x_k=\frac{1}{4}+\frac{1}{4}+\frac{1}{4}\frac{1}{4}=\frac{1348+1}{1463}}{\frac{1348+1}{4}}$. Settling $\Sigma x-0=1463$ we $x_0=836$, $x_0=798$; $\Sigma x=2538$ and $c=1095$ 'which is the price of the jewel.' lowever, understand the form of the first statement: but see fol. 65 verso where $\frac{190}{40}$ means $\frac{190}{42}$. is deadly a and kuryatat parivarlanam are quotations from saltra 11 on fol. 1 recto.	
ms 	ii. This is [2 verso.] ix—(1+2)x o x,—924, I do not, † amidm :	tim kriyate jātā 2558 chchheda projjhyam 1095 etan lyam possibly the question solved on 2 verso. The general meaning is: since $x_0 + x_0 - (\frac{1}{2} + \frac{1}{4})x_1 = x_1 + x_2 - (\frac{1}{4} + \frac{1}{4})x_2 = x_2 + x_1 - (\frac{1}{4} + \frac{1}{4})x_2 = 0$, or $\sum x - (1 + \tau)x_1 = \sum x - (1 + \frac{1}{4})x_2 = 0$, whence $\frac{1}{14}x_1 = \frac{1}{4}x_2 = \frac{1}{4}x_1 = \frac{1}{4}x_2 = \frac{1}{4}x_1 = \frac{1}{4}x_1 = \frac{1}{4}x_2 = \frac{1}{4}x_1 = \frac{1}{4}x_2 = \frac{1}{4}x_1 = \frac{1}{4}x_1 = \frac{1}{4}x_2 = \frac{1}{4}x_1 = \frac{1}{4}x_2 = \frac{1}{4}x_1 = \frac{1}{4}x_1 = \frac{1}{4}x_2 = \frac{1}{4}x_1 = $	
ms 	ii. This is [2 verso.] ix—(1+2)x o x,—924, I do not, † amidm :	tim kriyate jātā 2558 chchheda projjhyam 1095 etan lyam possibly the question solved on 2 verso. The general meaning is: since $x_0 + x_0 - (\frac{1}{2} + \frac{1}{2})x_1 = x_1 + x_0 - (\frac{1}{2} + \frac{1}{2})x_2 = x_0$, or $\sum x - (1 + \frac{1}{2})x_2 = 0$, whence $\frac{1}{12}x_1 = \frac{1}{12}x_2 = \frac{1}{12}x_2 = \frac{1}{12}x_2 = \frac{1}{12}x_1 = \frac{1}{1$	
ms 	ii. This is [2 verso.] ix—(1+2)x o x,—924, I do not, † amidm :	tim kriyate jātā 2558 chchheda projjhyam 1095 etan lyam possibly the question solved on 2 verso. The general meaning is: since $x_0+x_0-(\frac{1}{2}+\frac{1}{4})x_1=x_1+x_0-(\frac{1}{2}+\frac{1}{4})x_2=x_0+x_1-(\frac{1}{2}+\frac{1}{4})x_2=0$, or $\Sigma x-(1+\cdot)x_1=\Sigma x-(1+\frac{1}{4})x_0=c$, whence $\frac{1}{4}x_1=\frac{1}{4}x_2=\frac{1}{4}x_3=\Sigma x-c$ and $\frac{\sum_{X=0}^{2}-\frac{1}{4}+\frac{1}{4}+\frac{1}{4}}{\frac{1}{4}}=\frac{034+350+709}{1463}$. Settling $\Sigma x-c=1463$ we $x_0=836$, $x_0=798$; $\Sigma x=2538$ and $c=1095$ 'which is the price of the jewel.' Nowever, understand the form of the first statement; but see fol. 65 verso where $\frac{360}{40}$ means $\frac{360+40}{42}$. is isoddhya and kuryātat parivarlanam are quotations from sātra 11 on fol. 1 recto. A 13. dvitīyasya hayān navah üshtrā dasa trītīyasya	

w mornes (no = naya) and a third 10 camels (a" = sek/ra). Each gives one of his animals to both the others (and then their possessions are of equal value). It is required to find the capital of each merchant or the price of each animal. If thou art able, solve me this riddle.

We have $(7-2)x_1+x_2+x_3=(9-2)x_2+x_3+x_4=(10-2)x_3+x_1+x_2=0$ or $\Sigma x-(7-3)x_1=\Sigma x-(9-3)x_2=\Sigma x-(10-3)x_3$, whence $4x_1=6x_2=7x_3=k$ and $2x=\frac{4x_1+3x_2+3x_3+3x_4}{100}$ k. If k=168 then $x_1=\frac{4x_1+3x_2+3x_3+3x_4}{4}=28$, $x_2=\frac{4x_1+3x_2+3x_3+3x_4}{4}=28$. Also $7x_1=294$, $9x_2=252$, $10x_3=242$ are the original capitals, and 0=202.

Mahāvira gives the following . example.

Rule.—The number of gems to be given away is multiplied by the total number of men. This product is subtracted from the number for sale: the continued product of the remainders gives rise to the value of the jewel provided the remainder relating to it is given up.

Esample.—The first man had 6 sapphires, the second had 7 emeralds and the third 8 diamonds. Each by giving to each the value of a single stone became equal (in wealth to the others). Answer 20, 15, 12.

A 13-contd.

9 hac 10 vanijjakā 3 deyam vanik pinda hatam | pinda 7 | 9 | 10 deyam 3 śuddha śesham 4 6 7 tata śesham paraspara kritam gunita jātam | 168 | 168 | 168 | svašeshena tu vibhaktam 168 168 168 labdham 42 | 28 | 24 | esha pratyaika mulyam ekaikasya . . . gunitā jātāni asvai hayai ushtrebhyah 294 | 252 | 240 ekaikasya . . . jātā 262 | 262 | 262 | etes sama dhanā datvā ssamadhanā jātā prasta mūlyam tad uchyatām 3 recto. evam prasta mūlyam 2 | 3 | 6 dattais samadhanā jātā 17 | 17 | 17 trayodasama sütram 13 dvi . . . hīnā cha sūtram | ekayutānām samkhyā evam tāvat kāryam yāvat purushai samā bhavati saptama patre bhilikhita sthita chatur-daśama sūtram sūtram || gatisvaiva višesham cha vibhaktam pūrva gamtunāh tenaiva kālam bhavati stha . . . kena tu ll addhvardha vojana gate sata udā°

^{[3} recto.] This is the reverse because sutra 15 obviously begins a new section (B). **A** 18.

i. This appears to be a companion example to that on 3 -erao. The abbreviations are possibly ua° for uava 'barley,' ga° for gadhama 'wheat,' as for alls 'rice.' Here $(4-2) x_1 + x_2 + x_3 = (5-2) x_2 + x_3 + x_1 = (6-2) x_1 + x_1 + x_2 = c$ whence $x_1 = 2x_2 = 3x_3$ and $x_1 = 6$, $x_2 = 3$, $x_3 = 3$, $x_4 = 2$ and a = 17.

ii. Est understood. 'the reference to the seventh leaf is now only tantalising. No recognisable quotations from the sizes are served. The phrase that untuit 'so much as much' does not recur anywhere. In Bhaskars that and unus (ties and yd") are used as algebraic quantities.

iii. The rule means $t = \frac{r_1 D}{r_2 - r_3}$ where r_1 and r_2 are rates of progress and D is a given time. (See § 83, Part I.) The rule is quoted on 4 recto where gatisyaira viscaham cha and phron gata occur.

B 1.

i.	sūtram dviguņam prabhavam suddhā dviguņam niyatham tathā	recto.				
	uttarena bhajech chhesham labdham rūpam vinirdišet 📗					
ii.	udā° vartate bhritakax kaschi tatraiko dasha māśakam					
и.						
	pratyaham kurute tatra karmam bhattika mānavah					
	dvitīyam kriyate karmam — dvyādi tritayar uttaram					
	padam tatra tu bhavati kena kālena sāsyatām					
	$egin{array}{c c c c c c c c c c c c c c c c c c c $					
	‡dviguņam prabhavam suddh⇠prabhavam 2 dviguņam 4 niyata puna dvi					
	16 [uttarārdheṇa bhājayet] uttaram					
i.	sūtram hayor vibhajya gantavyam ato bhāga . gantata s	Vorec.				
	ekas cha gamana jñeya vutās samgunva					
	udā° niyo rathośvair daśabhir yujyate haya pamchakam					
	gamtavvam yojana satam kim udbhavet					
	ha 10 hava lagna rathasva 5 gantavyo vojana 100					
	†hayor vibhajya gantavyam† tatra havā 10 gantavyam yo° 100 †ato					
B 1.	[8 recto.] The position of folios 8, 9 and 7 is very doubtful. Then fit in nowhere perfectly. Their find orders are 48, 43 and 45; but 7 recto indicates that this find order is not of much value here. See the notes on fol. 7 recto. The writing is $\alpha 4$. i. The rule is another variation of that given on 7 verso and means $t = \frac{2}{3} \frac{1-2a}{4} + 1$ where A is a fixed rate and $t = A = (t-1) \frac{d}{2} + a)t$. ii. The example is $A = 10$, $a = 2$, $d = 3$ whence $t = \frac{2}{3} \frac{1-2a}{3} + 1 + \frac{1}{3} = 6 \frac{1}{3}$ and $a = \frac{1}{3} \frac{1}{3} = 6 \frac{1}{3} \frac{1}{3} = 1$. The phrase diagrams problems is quoted from the siltra above; while the phrase uttardidhens bhdjayet was wrongly quoted and was afterwards cancelled: Compare with the uttardidhens bhdjidens bhdjidens on 7 verso.					
B 1.	[8 rerso.] i. The soltra is partially reconstructed from the quotations in the solution below. ii. The example is: There are ten horses of which five are voked at a time to the chariot. How many changes should there be in a journey of one hundred vojanes and how much will each horse do? The solution is 100 = 10 stages and 10 5 = 50 Proof. 5 × 100					
	Mahāvīra give- a similar example (vi. 158). ravi-ratha turagās sapta hī chatvāro (vā vahanti dhūryoktā).					
	yojana-zavtati gatya'i ko rijidha'i ko chaturyoqa!					
	'It is well known that the horses or the Sun's chariot are seven. Four horses are yoked at a time. They have to perform a journey of 70 youngs. How many times are they unyoked and how many times yoked Mahāvīra's solution is expressed thus					
	The number of the total noises divided by the total number of horses gives the measure of the distance to be travelled over by each horse. That is \$\frac{1}{2} = 10\$ is the length of each stage, and \$10 \times 4 = 40\$ gives the distance cash horse works.					
	The solution is rather cryptic, but the interesting point is that the problem was a traditional one. Probably something of its original quality has been lost.					

B 1—contd.

bhāga† hrite labdha 10 tatra yuktāśva 5 etais saingunya pariyoga jātam . . . yojanānyaikośva rūdha | pratyayah panichabhis sata samgunya jātam . . . kriyate | yadi da . . yojana pamcha . . B 2. | tat samāptam dvijanmabhi | 9 recto. tat punas te samam bhaktvā daśa . . samāptavān samkhyāya x kati māchakshu kati viprā x kati prashtani 10 karanam dvigunam tathādvyūnam 18 ‡uttareņa vibhājitam‡ 1 1 1 atrottaram 1 anena bhaktvā jātam tad esha rūpādhikam $\begin{vmatrix} 19 \\ 1 \end{vmatrix}$ ayam preshņā brāhmaņā ekonavimsati sthāpa . . . \ddot{a}° 1 \ddot{u}° 1 \ddot{a} 1 pa $^{\circ}$ 19 rūpoņā karaņena phalam 190 9 verso. [9 recto.] See the notes on fol. 7 verso. The writing is of the same style, a4. Possibly there are two leaves stuck together. B 2, The example is a=1, d=1, A=10, and $10t=((t-1)\frac{1}{2}+1)t$ whence $t=\frac{2^{10}-2^{1}}{1}+1=19$ and by the rupona method a=190. Dr. Hoernle gave the following restoration: "For a certain feast one Brahman is invited on the first day, and on every succeeding day one more Brahman is invited. For another feast 10 Brahmans are invited on every day. In how many days will their numbers be equal; and how many Brahmans were invited." The use of the term labdham is here rather curious. The phrases labdhum dviquintam kritva, tabbhuqinam, uttarem imbantam and rūpādhikam are probably quotations from a sūtra. [9 verso.] The example probably meant: 'A and B start for a place 70 yojanas distant. A travelled at the rate of 1 yojana a day and B at the rate of 6. At what point on his return journey did B meet A''. B 2. Simply $\frac{x}{1} = \frac{270-1}{6}$, where x is the distance traversed by A, we have $x = \frac{x-1}{6+1} = 20$ as given in the text, and since A travels at the rate of one yojana a day, this is also the time.

Proof by the 'rule of three' 1 day : 6 yo' :: 20 days : 120 yo', and 70-20=50 and 70+50=120. Also 1 day : 170° :: 20

B 2-contd.

•	a(la)bdhe samyoga 7 vibhaktam 1 gantavyena gunitā jātān labdha
1	10 dviguņam 20 eshālpasyah
8	atha ayam kālo jñeyah anena kālenash shat yojanāni gantavyam
	. bhyām ekayojanikasya samāgamo bhavati
1	tadyathā trai-rāśikena pratyaya yady ekasya shat yojanā tadā vimsānām kim
	1 6 yo° 20 pha° 120 1 1 1 1 1
ł	atha saptati śoddhya śesha atra ssaptati 70 āgata pamchāśa 50 adhve
•	1 di° 1 yo° 20 di° pha° yo° 20 1 1
	В 3.
	· · · · · · · · · · · · · · · · · · ·
	$ar{\mathbf{a}}^{\circ} 3 \mathbf{u}^{c} 4 \mathbf{pa}^{\circ} 0 \text{nitya datta} 7 1 1 1$
	ādim viśoddhya† ādi 3 niyatam 7 viśoddhya 4
†	uttarārdhena bhājitam + uttaram 4 anena bhājitam 4 jātam 2
1	labdham sarupa† esha rūpādhikam 3 eśa kāla
_	a° 3 u° 4 pa° 3 rūpoņa karaņena phalam rū° 21
٠	lvitīyasya trai-rāsikena 1 $\mathrm{di^\circ}$ 7 3 $\mathrm{di^\circ}$ pha $^\circ$ r $\mathrm{\bar{u}^\circ}$ 21

gennicity disconnected by their contents and the right side has now been definitely located between folios 6 and 65. Folios 7 (verso), 8 and 9 are difficult to place. Indeed there seems to be some duplication. Folio 5 certainly follows folio 4 and section C cannot very well include folios 7 (verso), 8 and 9.

i. The problem is $7t = ((t-1)\frac{1}{2} + 3)t$ whence $t = \frac{2(7-3)}{4} + 1 = 3$. By the rüpone method $s = [(3-1)\frac{1}{4} + 3]t = 21$ and by the 'rule-of-three' 1:7:3:21.

The phrases ddim risoddhya, uttarārdhena bhājilam and labdham sa rūpa are quotations from a lost suira. Compare with fol. 8 recto.

B 3-contd.

ıdā°	adyeka uttara dvayam dvitīya pameha pratyaham
	kena kālena samatām - vada me gaņakottama -
	$egin{array}{c ccccccccccccccccccccccccccccccccccc$
†ādi	im viśoddhyā†
ii. The pr	roblem is $\delta t = ((t-1)^{\frac{5}{4}} + 1)t$ whence $t = <2\binom{t-1}{2} + 1 = 5$ and $s = 25 >$.
	В 4.
	yojana pariichakani sapta dinäni
asyaiva	gatasya parata dvitīya nava yojanaika gatake tam
1 di°	5 yo° dina 7 gatasya gata yojana 35 dvi' 1 di' 9 yo° 1 1 1 1
	iva visesham cha† yate guti 5 9 višesham 4
ib hak ta	$\begin{array}{cccccccccccccccccccccccccccccccccccc$
inai san	na gati bhavanti nava yojanam 📙
r atya ya	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
.dā°	ashtā-dasa yojanā ekena dine yātī
	tasyāshţa dinā gatasva

is closely connected with fol. 3 recto and with fol. 5.

i. The example may be restored: One goes at the rate of 5 mounts for 7 days and then a second starts at the rate of 9 mojanus a day. When will they have traversed equal distances?

The solution is $t = \frac{7.5}{9-6} - \frac{17}{9}$ days. 'Proof by the rule of three' 1:5: '\frac{1}{2} \tag{1.75} and 1:9::\frac{1}{2} \tag{1.75} \tag{1.85} and \frac{3}{2} \tag{1.85} \tag{1.85}.

One travels at the rate of 18 yojunas in one day for a period of 8 days. A second goes at the rate of 25 yojunas in one day. Determine in what time.

The eleventh leaf must have been close by ; indeed pareeps seems to indicate that it was ' just before.

B 4-contd.

	kena kālena sāsyatām 📗				
	evam ekā-daśama pattre bhilikhita purvepi				
	paincha-dasama sūtrani 15				
į i i.	sūtram $\parallel = \bar{a}d$ yor višes 1 a kartavyam $=$ uttarasya viseshatab				
	vibhaktam muttare				
Ĺ	• • • • • • • • • • • • • • • • • • •				
	uttaram 2 vibhaktan 1 ādi šesha 2 jātā 1 dviguņam $\frac{1}{2}$				
	2 rūpa sarnyutarii 3 esha sarikalite				
	pratyaya padam . Inā ubhaye sthāpitavyā rūponā karane phalam 21 21 dvi				
	kim prabhūtepi likhite shodašama sūtraii 17 sūtre bhrāntim astı				
i i.	sūtram ādyor višesha dviguņam chaya suddhir vibhājitam				
	rūpād <i>hikam tathā</i> kālam gati sāsyam tadā bhavet				
fii.	udā° dvayādi tri chayaś chaiva dvitīya tryādi-k-ottaraḥ				
	dvayo cha bhavate painthii kena kālena sāsyatām				
	sthāpanam krivate				
	$egin{array}{cccccccccccccccccccccccccccccccccccc$				
	karanam ‡ advor višesha‡				

iii. The rule means (?) $t=2\frac{(c_1+c_2)}{c_1+d_1}+1$. Note that the next $s\bar{u}tm$, on the reverse, commences with the same phrase $\bar{u}dy\sigma$

^{[4} verea] 1. The example was $a_1 = 4$, $d_1 = 3$; $a_2 = 6$, $d_2 = 1$. Where a_1 and a_2 are the first terms and d_1 and d_2 are the moreoments of arithmetical progressions, the sums of which were equal. Therefore $(t-1)\frac{1}{2}+4=(t-1)\frac{1}{2}+6$ whence $t=2 \cdot \frac{6-4}{3-1}+1=3$. The proof is by the r^2 -poin method, namely, $a_1 = ((3-1)\frac{1}{2}+4)3=21$ and $a_2 = ((3-1)\frac{1}{2}+6)3=21$. But 'why should it be written out in full 7' See Part 1, § 73.

out in full? See Part 1, 9 (3).

The remark that the subra is wrongly numbered was probably added later by some one other than the original scribe. The next subra is numbered 18 (fol. 5) and so on. This is not a copyist's error: it is one of an original MS.

ii. The rule is much the same as the previous one and means that t=2 $\frac{(a_1-a_2)}{(d_1-d_1)}+1$ when $((t-1)\frac{d_1}{2}+a_1)t_{n=0}((t-1)\frac{d_1}{4}+a_2)t_n$.

The rule is quoted below and on fol. 5 recto. *

iii. The example gives $a_1 = 2$, $d_1=3$; $a_2=3$, $d_2=2 <$ whence t=3 and s=15 >.

C 1.

	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	5 recto
	karanam ‡adyor višesham ‡ adi ‡chaya śuddhi‡ chayam	
	6 3 śuddhi 3 adi śesha 5 dvigunam 10 uttara višesha 3 $\frac{1}{2}$	
	vibhaktari 10 sa rūpam 13 anena ka samadhana bhavanti 3 3	
	pratyayam rūpoṇā karaneṇa phalam 65 esha padam dvi 65	
,	ashtādaśama sūtrani 18	
i.	(sūtram) dina gamanam ādi rahitam drīguņam tachchottarena samyutam pratinihita ātmaganam jūc ņam kshepa samjūako rāši ashtottara guņite kshepa samjūako datvā mūlam pratinihita yutum drīgunottara bhūjitam	
	hatan 30 †dina gama-	5 verse
	nam ādirahitam‡ dina gamana yojar vo paneba 5 adi 3 rahitani	
	jātam 2 †dviguņam† 4 †tachchottareņa samyutam† 8	
	†ātmaguṇam† 64 ; esa †kshepa samjhako raši† ashtottara samgu	
	labdha rāshi 30 ashta gunaib 240 uttarena gunaib uttaraib 4	
	guņitam jātam — 960 — † †kshepa sam jūako datv↠† tatra kshepa samj ň	
	64 yutam jātam 1024 asya mulam 32 (pratinihita †	
	8 yutan jatan 40 u	
C 1.	[5 recto.] The writing is the same as that on folio 1, namely 23, but it changes again in the middle of 5 recto. i. The example is $\mathbf{a}_1 = 5$, $\mathbf{d}_1 = 6$; $\mathbf{a}_2 = 10$, $\mathbf{d}_2 = 3$, where $(A - 1)_+^0 + 5$) to $2(10 - 5)/(6 - 3) + 1 = \frac{1}{2}$. Proof by the raponal method $\mathbf{a}_1 = <((-\frac{1}{2} - 1)_+^0 + 5)/(((-\frac{1}{2} + 1)_+^0 + 10))/(2) = 65$. The satiral number should probably be 17. See fol 3 recto. ii. The writing now changes to what may be termed the α 4 style. The rule means that $<$ if $DT + Dt = ((t-1)_+^0 + a)/t >$ then $t = -\frac{1}{2}(d - 2(a - D))^2 + 8dDT + d - 2(a - D)$	
	where D and T are fixed quantities and a , d and t are elements of an arithmetical progression of which a and d only are given. The quantity designated pratinihila 'set aside' is $d \cdot 2(a-D)$, while the kshepa samphake rdh 'the quantity known as kshepa' is $\{d-2(a-D)\}^3$ [5 gerso.] Writing a 4. Notice a semi-looped medial c near the end i. The example is $d = 2a$ 5. The solution proceeds step by $d = 2a$ 6. The solution proceeds step by $d = 2a$ 7.	
	step thus: DT=5.6=30, D=a=5-3=2, 2(D=a)=4, 2(D=a)+d=4+4-8; (2(D=a)+d)=64 and 'this is known as the ksheps quantity'; 8DT=240, 8DTd=960; 8DTd+(2(D=a)+d)==1024, $\sqrt{1024}=32$; 2(D=a)+d+32=40; and < $\frac{40}{8}=5$. Almost the whole of the stars on 5 recto is quoted here and on the following pages.	

C 2.

L	śike pratyayam $\begin{bmatrix} 1 & 5 & 5 \\ 1 & 1 & 1 \end{bmatrix}$ phalam anenas saha 55 eśa 6 rece
	samābdhānam II
u.	udā° ādi pancham uttaram trīni naro yojana gamyate
	dvitīya pratidinams sapta gatasya dina pamchakam
	kena kālena samatām katthyatam gaņakottama
	ā° 5 u° 3 pa° 0 prati° gati 7 dina 5
	pamcha dina ga yojanikam yojana 35
	karanam †dina gamanam adi rahitam+ tatra dina gamanam 7
	†ādi rahitam† ādi 5 rahitam
i.	anena guņitam jātam 840 †samjnako datv↠tatra kshepa rashi 49 6 vers
	datvā jātam 889 dāna dadāti samani karaņī kriyate
Ħ.	sūtram akrite sli <i>shtha krityūnā šesha</i> chchhedo dvi-samguṇaḥ
	tad vargah dala samslishtha hviti śuddhi kriti kshayah
	anena sutrena slishtha mulam anaya svamatima
ù.	labdham mūlam 29 †pratinihitam† 7 anena yutam 36 48 58 58
	2136 †dvigunottara bhājitam tato
٠.	[6 recto.] i. Continues the example. 'Proof by the rule of three' 1:D::t-Dt or 1:5::5:25 and DT+Dt=30+25=55.
C 2.	ii. The next example is D=7, T=5, a=5, d=3; hence t=\frac{\sqrt{2\frac{12}{1}\cdot 5\frac{1}{2\frac{1}{2}\cdot}} = \frac{2\frac{1}{2\frac{1}{2}\cdot} + \frac{2\frac{1}{2}\cdot 2\frac{1}{2\frac{1}{2}\cdot}} = \frac{2\frac{1}{2\frac{1}{2}\cdot} + \frac{1}{2\frac{1}{2}\cdot}} = \frac{2\frac{1}{2\frac{1}{2}\cdot} + \frac{1}{2\frac{1}{2}\cdot}}}{2\frac{1}{2\frac{1}{2}\cdot}} = \frac{2\frac{1}{2\frac{1}{2}\cdot} + \frac{1}{2\frac{1}{2}\cdot} + \frac{1}{2\frac{1}{2}\cdot}} = \frac{2\frac{1}{2\frac{1}{2}\cdot} + \frac{1}{2\frac{1}{2}\cdot} + \frac{1}{2\cdot} + \fr
	titles is $\binom{h}{2A}P$; and that by continuing the process closer approximations can be obtained. For a discussion of this rule see Part I, \$\frac{1}{2}68, 69, 85. The three versions as they now stand are — akrite \$\frac{8}{1} \cdot
	tad varga . Alishthah briti suddhi kriti kahayah 57 Verso. skrito siishtha krity una seesa chehhedo dvi

C 3.

6 1 8		447 dalitā 447 sāsye yutam 737 pada 7 100 58 58
60* 16 60*	${ m cha}^{\circ}$	ghnā tatra padam 178 anena guņitam jātam 65593 841
33 60* 6	li° vi ^c	śli tya śeshań kriyate 65569 bhage hrite 841
60* śe°	6 29	pratyayam trai-rāśikena 1 7 yo 178 phalam 1 1 29
ojana	42	se 28 nivatam tena

ekona-vimsatima sūtram 19 ||

[7 recta.] This continues the example started on fol 6 recta. [The numbers marked with asterisks are change-ratios (see Part I, §§ 103-105).] The set of figures on the left expresses $\frac{1}{4}$, as a sexagesimal fraction (see Part I, § 58), i.e., $\frac{1}{5}$, =6+8×16°+33°+6 $\frac{4}{5}$ °. The portion of the statement above the 16 is missing but the restoration is certain. Of the above intrins cha^{\dagger} has not yet been identified; h^{\dagger} stands for hipta (6k, kears), v^{\dagger} for v^{\dagger} for v^{\dagger} for v^{\dagger} for solution. In Hindin astronomical works hipta means a 'minute of arc,' and vihipta' a second of arc. This use of the sexagesimal notation for arithmetical purposes in an Indian work is unique. The solution proceeds to find the approximate value of v_1 which depends on v_2 and ultimately v_3 . We have v_4 and v_4 and v_4 . Now v_4 have v_4 and v_4 and v_4 have v_4 and v_4 have v_4 and v_4 have v_4 hav

But DT + Dt₁ + 7(5 + \frac{1}{1}) = \frac{8}{2}\frac{6}{4} = 77(\frac{1}{2}).

* Proof by the rule of three \(\text{1.7} \) 1. 7\frac{1}{2}\frac{1}{1} = \frac{48}{2}\frac{1}{1} = \frac{48}{2}\frac

The satra number should probably be 18. See fol. 4 rerso.

65 verse.

	MARKET IN N
ghana .	†ashtottaraghne guņite ashta ghanam 480 uttara dvi-ghnam adi ādi dvi-guṇa 2 chayojjhitam cha uttaram ato uttaram pātayitvā ekam bhavati 1 va
nikshipya	dhanasya 481 mūlam ślishtha karanyā 21 40 42
vamśam	882 sesham chatvārimsa prithak sthāpya 40
yojyam	922 tan mūla varjitam tan mūlam

C 4. [65 verso.] Folio 65 consists of two leaves stuck together. The writing on both sides may be classed as α4. The left side has no direct connexion with fol. 7 recto but it belongs to the same section.

The given here quoted from is lost, or hidden, for possibly when folios 7 and 65 are separated it may be discovered. It may be said to knone of the most important sitras of the whole work judging by the care and elaboration with which it is illustrated. It must mean that < when s=((t-1) \frac{1}{2} + a)t then t=\frac{1}{2a} \frac{1}{2a} \frac

common difference, the number of terms and the sum of an arithmetical progression.

The example is a=1, d=1, s=60; hence t= $\sqrt{(2-i)^3 \cdot 8i \cdot 1.60 \cdot (2-1)} = \sqrt{461-1}$ The solution proceeds 80s = 480, 2s = -0.1, $(2s = -0.1)^3 \cdot 80s = 481$; by the square-root method (see fol. 6 verso) the first approximation is $21\frac{40}{85} = \frac{80}{45} = \frac{912}{49}$ and $< t_1 = (\frac{912}{42} - 1) \div 2 = \frac{800}{84} >$

C 5.

C 5.
880 964 guņita jātam 848320 chatvārinsa prithak sthānām vargam 56 vana. 84 168 14112
1600 esha uparā pātya śesham 846720 vartya jātam 60
akrite ślishtha krityūnān śesha chchhedo dvi-samgunam
tad varga dala samślishthah hriti śuddhi kriti kshayah 📗
†śesha chchhedo dvi-samguna† kri
21 21 bha 20 400 dala 1 samslishthah 20 21 441 2 21 +
śesham pātya dvā bhājita †adham upare uparam†
guņitavyam vargam yāva marjaye
425042 400 sesham 424642 19362 19362 19362
0.5. [56 verso.] Continues the example. $s_1 = ((t_1 - 1) \frac{1}{2} + 1) t_1 = t_1 \frac{(t_1 + 1)}{3} = \frac{850}{54} \cdot \frac{064}{160} = \frac{36520}{16112}$, but $< \frac{51}{64} = (\frac{40}{2.31})^3/8$. $> = \frac{1600}{14112}$ and $\frac{546350 - 1800}{14112} = 60$. The bottom half of fol. 56 verso is blank but the example is continued on 56 recto. [56 recto.] This continues the example given on fol. 65 verso. The top part of the leaf is much broken up; but the square-root rule (see fol. 6 verso) is given. Why this rule is repeated is not quite understood nor is it understood why it comes between two approximations of the same surd. Anyhow the general aim is clear: since the first approximation is $21\frac{3}{4}$? the second is given by $q_7 = 21\frac{3}{4}\frac{3}{4} - \frac{1}{4}(\frac{3}{4}\frac{9}{4})^2/21\frac{3}{4}\frac{9}{4} = 21\frac{3}{4}\frac{9}{4} - \frac{1}{444} \times \frac{401}{461} \times \frac{31}{1661} = \frac{424}{1662}$
C 6.

	405280 444004 38724 38724	ardham kartavyam
	405280 444004 38724 77448	samgunya jātam a hrarā hareshu gun
	179945941120 2999096352	asya ürdham 160000+
06.	[64 recto.] and $t_0 = (\frac{484645}{19969} - 1) + 2 > 4$	$\frac{408290}{38794} \text{ Also } s_1 = \frac{t_1(t_1+1)}{5} = \frac{608290}{39794} \cdot \frac{444004}{77444} < \frac{179,944,941,190}{8,909,004,881} > \text{ and } s_2 - \frac{189,000}{8,909,004,863} = \frac{179,948,781,190}{2,009,006,863}$

C 6-contd.

† śesha chchhedo dvi-sangunam 6			
ansās vamsam 77 tan mūla varjitam tan mūlam			
dvi-gunottara sambhaktam 65 esha padam 1 yanam			
\bar{a}^{\circ} 1 u^{\circ} 1 pa^{\circ} 65 r\bar{u}pon\bar{a} 41 dalita 41 1 1 24 24			
ādi samyutam			
C 7.			
†ashtottara-gline gunite† 40 dvi-ghnam ādi cha			
nikshipya 41 mūlan 6 † sesha chchhedo dvi-samguna† 5			
śuddhah tasmāt			
akrite ślishtha krity unā šesha chchhedo dvi samgunah			
tad varga dala samslishthah hriti suddhi kriti kshayah			
†akrite slishtha† tada dvi-samguna krita			
6 tad vargatam 6 5 25 dala			
25 . 11833 hri 1848 kriti kshaya kritam : eśa 57 recto. 1848 ———————————————————————————————————			
mūlam tan mūlam mūlam ekam 1 esha sadriśe pātita jāta			
9985 sambhaktam uttaram dvi-gunam 2 anena bhaktvā 9985 1848 — 3696			
esha pamchakasya padam 📗 asya pra			
sūtram eko rāśi dvidhā sthāpyaś chayase			

^{0 6-7. 64} verso 57 verso and 57 recto are all (except the last line) concerned with one example the beginning of which is lost. The example is < a=1, d=1, s=5; therefore t= \(\frac{\psi_1}{2} = \frac{1}{2} \frac{\psi_1}{2} = \frac{1}{163} \frac{\psi_1}{2} = \frac{1}{164} \frac{\psi_1}{2} = \frac{1}{164}

Apparently a proof followed introduced by a salva of which, unfortunately, only a fragment remains.

C 8.

L	10225 dalitā 10225 ādi yutah 108625 padaghnā 45 recto. 65600		
	pada <i>samyu</i> tā . 6455040625 ato panicha-vińśa uparāḥ 3227520000		
	6455040000 labdham 2 esha dhanam [] 3227520000		
iL.	$egin{array}{ c c c c c c c c c c c c c c c c c c c$		
	384 asya varga 147456 akri 21743271936 45 verso.		
	esha sarva gunitā karani kritvā bhājita jātah 1158 + amśair 671250		
amśā guņaye raśi varjya jātaḥ			
579 579 768 294912 515520000 294912 + 1158 777307500 777307500 777307500			
éesham 579			
	dvayena mūle		

^{[45} resto.] i. The greater portion of this example is lost, but can be restored. The example was $< a = \frac{1}{4}$, $d = \frac{1}{4}$, s = 2; whence $b = \frac{\sqrt{10}-3}{6}$. The first approximation to $\sqrt{10}$ is $q_1 = 10\frac{1}{4}$ and the second is $q_3 = 10\frac{1}{4} + \frac{1}{4}(\frac{1}{4})^9/10\frac{1}{4} = 10\frac{81}{850}$. This gives $t_2 = \frac{1000}{1000} + \frac{3}{4} = \frac{100}{6} = \frac{1000}{4000}$ and $s_3 = (\frac{6045}{46200} - 1)\frac{2}{4} + \frac{3}{4})\frac{50425}{46200} = \frac{10035}{10000} + \frac{1000}{4}\frac{1000}{4000} = \frac{1000}{60000} + \frac{50425}{4000} = \frac{6435,000435}{5,227,530,000} = \frac{6435,000435}{5,227$

⁴⁵ verso. The second approximation is given by $q_1 = 579 \frac{768}{1186} - \frac{184}{6879} \frac{1879}{1186} = 579 \frac{768}{1186} - \frac{184}{670} \frac{1188}{671260} = 579 \frac{768}{1186} = 579 \frac{768}{671260} = 579 \frac{768}{1186} = 579 \frac{768}{$ 579 \$15,880,000 -204,913 = 579 \$15,225,000 \\
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C 9.

448244345088 4663845000 443580500088 4663845000	221790250044 dalitā e . 46 recto.
110895125022 ādi samyuta 113227047522 1554615000 1554615000	pada-ghna 50753383762746743271936 ; 7250483394675000000
	pātita jātā uparānyāsa sthāpa .
507533837627250000000000 bhā 7250483394675000000	7000

^{0 9. [46} resto.] $\frac{7}{6}$ minued from 45 v-rso. $t_2 = \frac{450,1870,381,689}{1777,207,800} - 3) + 6 = \frac{460,244,548,090}{4,623,845,000}$ and $t_2 = 1 = \frac{448,580,501,088}{4,613,845,000}$. $(t_2 - 1)$ d = $\frac{211,790,280,046}{1,584,618,000}$, $(t_2 - 1)$ d = $\frac{11,790,713,891,032}{1,584,618,000}$, $(t_2 - 1)$ d = $\frac{11,790,713,891,032}{1,584,618,000}$, and finally $t_2 = \frac{8}{1} = \frac{8}{10}$, $t_2 = \frac{8}{10}$, $t_3 = \frac{8}{10}$

D 1.

a i e vīhujaņa vī ha hai na gore jā ma cha uppaņe	
sā male a dha pa . dhale āpot dine āgaņe vīhujaņa ehu vī	
karaṇam trai-gore varehahipaṇehi sā	
[46 verso.] Writing α 4. Find order 9. This is quite unintelligible to me.	
D 2.	
tola 5	70° re
•	70° n
17 117	
2 . 0 rītā 7 pala 2 tola 1 pala 6	70° r
udā° samā napešī kritāni cha	
dvecha tisraś	
tisra samādāya] tulitāni trayo-daśe	
ekaikasya sārdhayah	
$egin{array}{cccccccccccccccccccccccccccccccccccc$	
prakshepa yuktyā phalam	70° 1
ri ri	70° 1
gunya phala rāśi	
katram pala 8	70° v

D: 70 recto is mostly unintelligible but $x(\frac{1}{2}+\frac{1}{4}+\frac{1}{4})=13$ and x=12 is a solution.

⁷⁰ earso. Here $x(\frac{1}{2}+\frac{1}{4}+\frac{1}{4})=65$ and x=60 is obviously connected in some way with the example on 70° recto but they are two separate examples.

D 2-contd.

8eva	ānāmi tu dī	
	$egin{array}{c ccccccccccccccccccccccccccccccccccc$	ı
•		
	D 3.	
2 5	2 2 drishya ato sadrisha hakam 6 7	69 re
upai	māmsam tamdulā bhavanti chatvālimsa dūnā chau	
rāśi	eta tamdulā dvā-chatvārim vanti ete vrīhakā .	
	trah sthāpanam asya	
	1.	
prat	aya trai-rāśikena 5 ā° 2 taṁ° 210 pha° taṁ° 84 1	
	yasya kriyate 6	
	yate $rar{a}sih$ 7 2 210 phalam 1 1 1	
	katram 105	69 v
ud ā °	tribhir dattai triguņā triguņena tu	
	tad uchvatām	
1 1	3 9 drishya 130 prakshepa 10 30 90 ekatram 130 1 1	
	. vān 📗 tam satam tribhir datyai paravaptrā pavaptri kai	
4 1	6 9 dri° 190 40 60 90 ekatram	
Fo (8)	.69 consists of four pieces but is not quite so shabby as folio 70, for the two larger pieces fit together. Sciol. The statement means $x(\frac{1}{4}+\frac{1}{4}+\frac{1}{4})=216$ whence $x=210$. The 'proof by the rule of three' is $6^{\circ}: 2 \text{ tam}^{\circ}: :210: 84 \text{ tash}^{\circ} < \text{and } 84+70+60=214 >$	

D 4.

	168 deśa dvātya pātya jātā	68 rect
	śesham* 21 ekatram 29 dram 2	
	· · · · ·	
D	 [68 recto.] Consists of small fragments which probably belong to folio 67. Writing α_s. The phrase pdiya šeskam occurs on some six other occasions (on folios 31, 62, 63, 58). 	
	D 5.	
i,		81 recto
	tiyasya kriyate . 3 di° 2 dram° 168 dinā phalam dram° 1 1 1 11	
	prathamena dattam saptah dattais samadhanā jātā	
	varióam 77 294 pātya sesham † 217 dvitīyasya 11 11	
	datta	
£.	punānyam sarva bhā 4 dine dram° 15 jīvyā 1+ 4	
	dvitīyasya bhā 3 dine dram'	
D 5.	Folio 31 consists of two leaves stuck together and the writing on the two sides differs. The leaf is very ragged. [31 recto.] The writing may be classed as α_3 i. The example may be restored with some uncertainty: A carns $3\frac{1}{4}$ drammas in 2 days, B ² carns $2\frac{1}{4}$ in 3 days. A gives B 7 drammas and this makes their possessions equal. How long had they been earning? 8 Since $\frac{34}{2}$ t-7 = $\frac{34}{3}$ +7 we have $t = \frac{14}{7/4} = \frac{15}{17}$ days. Proof by the rule of three 2 days: $\frac{34}{4}$ drammas: $\frac{14}{17}$ days: $\frac{34}{17}$ drammas and 3 days: $\frac{34}{17}$ drammas: $\frac{34}{17}$ days: $\frac{34}{17}$ drammas $\frac{34}{17}$ days: $\frac{34}{17}$ days: $\frac{34}{17}$ drammas $\frac{34}{17}$ days: $\frac{34}{17}$ days: $\frac{34}{17}$ days: $\frac{34}{17}$ drammas:	

D 5-contd.

• • • •	kāraņam chchheda sam-guņe dr	am 1 4 ya 31 vers 1 1 2
dram° 1 6		guņākāro dvay āna
$egin{array}{ c c c c c c c c c c c c c c c c c c c$	†uparani guņave† adau tāva dv	
sūtram		
[31 verso.] Sommultiplication ' occur	me of the lower writing shows through and it is very difficult to differentiate. 'I are again on fol. 42 verso.	'he word gunākāra i ' form of
	D 6.	
	chchhesham ta dviguna . tā	67 verso.
nirgachchha	praviśa māne chatvāri dattah	
puna dvi-gun	nam	
süņya hastam	n gatam tasya kim atra mūladhana syāt	
1 2 bhā° 1 1	1 1 2 bhā° 2 2 2 bhā° 3 1 1 1 1 1 1 1	3 2 bhā° 4 1 1 1

D 6. 67. The surface of the leaf is much worn and the writing is in some places rubbed off. The writing is 22. [67 recto.] i. The example seems to relate to a game at which a certain quantity was staked and eventually all lost. The statement means 1+½ (3+½ (3+½ (4+¾ (5+½ .½)))=< ½ >

D 6-contd.

49 . 12 jāta 61 . sadrišan 8 . 11 puna
16 61 jātā 77 sadrišam ekasya 16 yutam 77 8 8 16 16
jātam 93 esha phalam bhavati
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
hundikā samānayana sūtram
dina bhakta višesham cha dvi-gunam krivate chaiva
kālam eshām vinirdišet trai-rāšika vidhānena
. dattam cha pātavyam‡ sūkshme dattam cha tatsamam 👖
udāharaṇaṅi dvi-guṇa
[67 verso.] Worked out by steps - \(\frac{1}{3}\) (5+\frac{1}{4}\) - \(\frac{1}{3}\), \(\frac{1}{3}\) - \(\frac{1}{3}\), \(\frac{1}{3}\) (4\), \(\frac{1}{3}\) - \(\frac{1}{3}\), \(\frac{1}\), \(\frac{1}{3}\), \

D 7.

E 1.

	nam kr									
	1 1	dram'	1 2 1 1	drain°	$egin{array}{cccccccccccccccccccccccccccccccccccc$	drain° 1	4	dram°	1 6 1	
									;	
pra tyay	ja trai-:	rāśikena								66
	1	dram°	1 rū' 1	12	dram°	phalam	rūpa	12	ı	
	1	dramo	2 rūj	ра 6 1	dram°	phalam	rūpa	12		
	1	dram°	3 rūj 1	pa 4	dram°	phalam	rūpa	12		
	1	dram"	4 rūj	pa 3 1	dram°	phalam	rūpa	12	1	
	$\begin{vmatrix} 1 \\ 1 \end{vmatrix}$	dram	$\frac{6}{1}$ $r \tilde{u}_i$	pa 2 1	$d\tau am^{\circ}$	phalam	rūpa	12		
The cos are 12, 6, 4,	t of one of		1 dram ^o : 1 , ; 1 , ; 1 , ;		2 dram": 12 rs		mmss, and	the numbers	of articles	
				E	2.					
•	• •	. 1 yo	° 1	di°	6				•	53
	m tu ta	atra gatim	3 2	2	viśeshań	1 2		sarva g	atī	

E 2—contd.

	ai-rāśikena	1 di°	yo° 27	d ina 6 ād	au yoja	na 9 .	
. 1 1	1 di° .	. y o°	phalam y	ojana			
	18	20	dina ghatike gha° dina	phalam yoʻ	27 7	53 verso	58 veru
	27	,	ghatike ghatike dina	pha° yo	36 7		
Proof 96 da	or 20 days 20 ghatikas. ys: 18 yo°:: 20d. 20 ys: 27 yo°:: 20d. 20) gha°: ∜ yo° and ₹ 0 gha°: Ψ yo.	7 + ** − 9. 3.				
				vacha			,
udã°	śad-vimśas ch	ıa eti-bamenasa					58 rec
udā°		ia tri-pamenasa . śad-vi msa cl	ıatu ś-chatvāli :	msa saptati	. 1		58 rec
udā°	dvā-śa	•		•	. t		58 rec
udã°	dvā-śa chatush-shasi	. śad-vimśa ch	miśa na	•	. 1		58 rec
udā° ·	dvā-śa chatush-shasi	. śad-vi mśa ch hti na <i>va</i> rimśa ashta .	miśa na	amtaram	. 1		58 rec

E 3---contd.

56 Vector. drishya 20 sthāpanam kriyate . yuvi 1 sūdha main 1 1 2 . . . 3 mamda 1 mamde 20 . . . ta datta jātam mamda 2 yu 5 sūdhe 1 [58 verso.] There is basis for the following restoration--A man earns 3 in one day, a young woman 1½ in 1 day and ½ in one day. If 20 earn 20 mandas in one day, how many of each will there be " Let x, y, z be the numbers of each class, then x+y+r=20 individuals

3x+3y+3=20 mandas of which the only solution in positive integers is that given in the text, namely x=2, y=5, z>13. This problem known as the "Hundred Hens" problem in China, and as the Regula Virginum, etc., in Europe is noted upon in Part I, §80 (a).

E 4.

. dine tatha | tri rūpa pamchabhi dinai | 21 recto.

rū°	1	rū	° 1	rū	° 3	drishya	100 1	
1 0	di°	1 2	di°	5 1	di			_

karanam | kritvā 3 2 3 dri° 100

E 4. Folio % consists of 7 scraps of which the largest piece is partly intelligible. The find order is 55 and the writing α1, 4 [21 redo.] Apparently this means: 1 rao is given or obtained in ½ days, 1 in ½ day and 3 in 5 days by three separate individuals (or classes) and the total amount given or obtained is 100.

In one day $\frac{1}{4} + \frac{1}{4} + \frac{2}{8} = 3 + 2 + \frac{2}{8} = 5\frac{2}{8}$ is given, so that one is given in $\frac{2}{18}$ days and 100 in $\frac{500}{28} = 174$ days.

E 4-contd.

. . . vārdham tritiyasya 21 verso. jīva-lokāt eshām dīnār kasya kim bhavati 2 1 2 1 dri 500 parivartanam kriyate 10 36 10 1 prakshe . .

E 5.

473500 | vartita jātā phalam dī 500 | 22 recto. asya pratyaya trai-rāsikena 100000 dīc phalam di 60000 947 947 2 2 $\mathrm{d}\mathbf{i}^{\mathrm{o}}$ $d\bar{\iota}^{\circ}$ 157500 di° phalam di 60000 1 947 947 dio di° 216000 di° phalam di 60000 947 947

The gifts are therefore $\frac{100,000}{1047} + \frac{187,500}{947} + \frac{218,000}{947} > = \frac{678,500}{947} \mu - 500$ dindrus.

^{[21} verso.] Here the main elements of a problem are preserved and the problem is continued on folio 22. The problem probably was to the effect that: A gave 2½ dindras in 1½ days, B gave 3½ in 1½ days and C 4½ in 1½ days. In what time would they have given 500 dindras?

In one day $\frac{2i}{1i} + \frac{9i}{1i} + \frac{4i}{1i} = \frac{16}{6} + \frac{21}{8} + \frac{36}{10}$, $= \frac{947}{120}$ is given. Therefore 500 is given in $\frac{800 \times 120}{947} = \frac{80800}{947} = 63\frac{230}{947}$ days. Continued on fol. 22 recto.

^{[22} recto] continues the solution of the example on fol. 21 verso. E 5.

^{*} Proof of this by the rule of three ' $2\frac{1}{2} di'$: $1\frac{1}{2} days$: : $\frac{100,000}{947} di$: $\frac{60,000}{947} days$.

F 1.

	chaturguṇam chaiva chaturthe chaiva dattavān cha śatam ekam	
	dvayānvayam vadasva prathame dattam kim pramāṇām sya .	
	$egin{array}{c c c c c c c c c c c c c c c c c c c $	
	†śūnyam eka-yutam kritv↠1 2 3 4 †kshepa yuktyā†	
	phalam 20 40 60 80 evam 200 eshām	
	ā° 20 u° 20 pa° 4 rūpoņā karaņena phalom 200	
li.	sūtram yadrichchha pinyase sūnye tadā vargam tu kārayet	
	The problem was something like this: A certain amount was given to the first, twee that to the second, three it to the third, and four times to the fourth. State the amount given to the first and the shares of the others, if the total amount given was 200. The shares are represented by 0, 2, 3, 4. 'Having added one to the nought' the sum is $1+2+3+4=10$. Then the proper share of the first is $\frac{1}{10} = 20 > 1$. Having added in this value the series becomes $20 \cdot 40 \cdot 60 + 80 \cdot 200$.	
	The proof by the rapona method gives <((4 · 1)\% +20) 4 \(\times = 200\). For the method of solution, the regula jalsi, see Part I, \\$\frac{1}{2}\\$71 and 72, and for the rapona method see \\$73. The whole section is dealt with in \\$87, and the use of the symbol for 'nought' in \\$60. ii. The salra begins "Put what number you please in the empty place (or for the nought)." This is quoted on fol, 23 recto and so is lasta vargam to karayet, etc.	
	The proof by the rapona method gives $<((4+1)\sqrt[3]{6}+20)$ 4 $>=200$. For the method of solution, the regula falsi, see Part I, §§71 and 72, and for the rapona method see §73. The whole section is dealt with in §87, and the use of the symbol for 'nought' in §60. ii. The salra begins "Put what number you please in the empty place (or for the nought)." This is quoted on fol. 23 recto and	
ı.	The proof by the rapona method gives <((4 · 1)% +20) 4 · =200. For the method of solution, the regula falsi, see Part I, §§71 and 72, and for the rapona method see §73. The whole section is dealt with in §87, and the use of the symbol for 'nought' in §60. II. The salra begins "Put what number you please in the empty place (or for the nought)." This is quoted on fol. 23 recto and so is lada vargam to kdrayet, etc.	23 reoto.
ì	The proof by the rapona method gives <((4 · 1)% +20) 4 · =200. For the method of solution, the regula falsi, see Part I, §§71 and 72, and for the rapona method see §73. The whole section is dealt with in §87, and the use of the symbol for 'nought' in §60. In The salra begins "Put what number you please in the empty place (or for the nought)." This is quoted on fol. 23 recto and so is ladà vargam tu kdrayet, etc. F 2.	23 recto.
ì	The proof by the rapona method gives <((4 · 1) \(\frac{1}{2} \) \	23 recto.
Ĺ	The proof by the rapona method gives <((4 · 1) \(\frac{1}{2} \) \	23 reoto.
ì	The proof by the rapona method gives <((4 · 1) \(\frac{1}{2} \) \	23 reoto.

i. The example may be represented by $x+2T_1+3T_2+4T_3=132$. Where T_1 , T_2 , etc., represent the values of the first, second, etc. terms. Make x=1 then the terms are 1+2+6+24=33 and the proper value of x is $\forall y=4$ and the series becomes 4+8+24+96=132.

All the technical terms here employed are of interest and will be dealt with in due course: ichchhā 'an assumed number'; vargs 'a serice'; prakshepa 'something thrown in' or 'an interpolation'; variya 'cancelled'; drishya' the given number'; ota,

F 2-contd.

	esha varga krama ganitam 📗 atha yuti vargam kri	
L.	sūtram kāmikam suņye vinyastam tadā chaiva krame guņam	
	· · · · · kṛitvā chaturtha	23
	prathamasya tu kim bhavet	
i	‡kāmikam śūņye piņyastam‡ kāmikam 1 esha ņyastam	
	‡tadā chaiva krameņa guņitam‡ 1 2 9 48 eshām yu . 60	
1	anena drishvam bhājitam $\begin{bmatrix} 1 & 300 & \text{jātā} & 5 & \text{e} & \dots \end{bmatrix}$	
٦	varga ganitam	
t u	sa cha dvyārdha yuta dhanam dattam chaivā dhanam sa cha dvyārdha yuta dhanam ii. The term kdmika is practically synonymous with ichchhā or yadrichchhā 'what you please'; 'an assumed number.' Bhādhara is is ishta much in the same way. A good deal of the stira is quoted on fol. 23 verso. [23 verso.] i. The example may be represented by x + 2T ₁ + 3 (T ₁ + T ₂) + 4 (T ₁ + T ₂ + T ₃) = 300. Put x = 1 then the saries becomes	
t u	varga ganitam ndā° prathamasya na dattam chaivā dhanam sa cha dvyārdha yuta dhanam	
t u	sa cha dvyārdha yuta dhanam dattam chaivā dhanam sa cha dvyārdha yuta dhanam ii. The term kdmika is practically synonymous with ichchhā or yadrichchhā 'what you please'; 'an assumed number.' Bhādhara is is ishta much in the same way. A good deal of the stira is quoted on fol. 23 verso. [23 verso.] i. The example may be represented by x + 2T ₁ + 3 (T ₁ + T ₂) + 4 (T ₁ + T ₂ + T ₃) = 300. Put x = 1 then the saries becomes	
tu 1.	sa cha dvyārdha yuta dhanam ii. The term kdmika is practically synonymous with ichchhā or yadrichchhā 'what you please'; 'an assumed number.' Bhādhare ishka much in the same way. A good deal of the sūtra is quoted on fol. 23 verso. [23 verso.] i. The example may be represented by x + 2T ₁ + 3 (T ₁ + T ₂) + 4 (T ₁ + T ₄ + T ₅) = 300. Put x = 1 then the series becomes it. The example is solved on fol. 24 recto. F 3. Atam chatuś-chatvalimsā **dattam chaiva chaturguṇam**	4 rec
tu 1.	sa cha dvyārdha yuta dhanam	4 rec

^{[24} recto.] The example may be represented by

[x(1+1\frac{1}{2})]+[2T_1+2\frac{1}{2}x]+[3T_3+3\frac{1}{2}x]+[4T_3+4\frac{1}{2}x]=144\frac{1}{2}

Set x=1 and the series becomes \frac{1}{2} + \frac{1

F 3-contd.

	śūnyeśu 1 †yutam chaiva gunam† tatah	
	yutam chaiva gunam kritvā kāraye gana	
	uparam adhe adham gunaye $+$ $\begin{bmatrix} 10 \\ 2 \end{bmatrix}$ sārdha dv yutam . tīya rāśyā gunanam \blacksquare	
	sārdhais saptabhi trīņi 45 sārdha traya yutam chaturtha rāśi 2	
	guņayesh shadvimsatibhi jātā 208 sārdha chatvāri yu	
	289 evam driśyam sarvam tadeva jātam 2	
1,	tri-sārdha yu	34 verso
	chatur-guṇam chaturthena navārdha yutam dattam	
	dvišatā dvāvimsādhikā kim atra prathamasya dattāsit	
	$\left[egin{array}{c c c c c c c c c c c c c c c c c c c $	
	‡śūnya datv⇠ 1 yuta guņita yuta krameņa jātam	
	sthāpā	
	jātam 222 driśyāh 222	
íi.	udā° prathamam na jānāmi divardha yutam	
	[24 circo]. i. The example may be represented by	

^{[24} offso]. i. The example may be represented by $[x (1+1\frac{1}{2})] + [2T_1 + \frac{1}{4}x] + [3 (T_1 + T_2) + \frac{1}{4}x] + [4 (T_1 + T_2 + T_3) + \frac{1}{4}x] = 222.$ Set x=1 and the series becomes $\frac{1}{4} + \frac{1}{4} + \frac{1}{4} + \frac{1}{4} + \frac{1}{4} = 222.$ The same quotation fings shake rapus dated occurs on fol. 25 verso. See also at the bottom of fol. 26 recto.

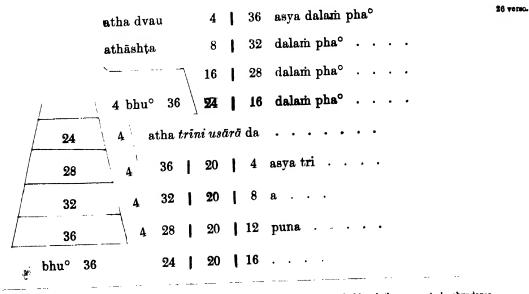
F 4.

	$\left[egin{array}{c c c c c c c c c c c c c c c c c c c $	25 recto.
	• • • • • yutam jātam $\begin{bmatrix} 5 \\ 2 \end{bmatrix}$ dvitīya guņam $\begin{bmatrix} 10 \\ 2 \end{bmatrix}$. tritīya ekatre	
	gunitam yutena yutam 10 23 yutam 33 gunitam 2	
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
	$egin{array}{c c c c c c c c c c c c c c c c c c c $	
i.	karanam †śūnya sthāne††rūpam datv↠1 yutā jātā 5	25 verso.
	chaturguņam navārdha yutam jātam $\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
	$egin{array}{c c c c c c c c c c c c c c c c c c c $	
	1anena sarvarii gunitain tadeva $\begin{bmatrix} 5 & 15 & 22 & 29 \\ 2 & 2 & 2 & 2 \end{bmatrix}$ ekatrarii $\begin{bmatrix} 1 & 15 & 22 & 29 \\ 2 & 2 & 2 & 2 \end{bmatrix}$	
	eshām aparo vidhih	
L	udā° prathama dhanam dattam najātam kim tu divardha yutam	
	tadā dvitīyena dvi-guņam dattam pamchārdha hīnam	
	tadā tritīyena triguņam dattam saptārdha	
	chaturthena chatur-gunam navārdha hīnam	
	dattam ekatram ta	
	$egin{array}{ c c c c c c c c c c c c c c c c c c c$	

F 5.

L.	karaņam †śūnya †rūpam datvāḥ† yutam jātam 5 26 recto.
	chaturtham chatur-guṇam navārdha rahitam sesham 11 e
	$egin{array}{c c c c c c c c c c c c c c c c c c c $
	bhaktam $\begin{bmatrix} 2 & 29 & \text{jātam} & 1 \\ 29 & 2 \end{bmatrix}$ gunitam tad eva
i	evam riņa rāśī bhavanti tri-prakāram samāptam śūņya sthāne rūpam datvā tadanu
	yuktam gunita
TF	5. [29 recto.] i. This is the solution of the example given at the bottom of fol. 25 verso. Let x=1, then the series becomes

F 6.



F 6. [26 verso.] This is, apparently, the beginning of another section, but it is isolated and although there seems to be abundance of material (compared with other leaves) I can make nothing of the problem.

G 1.

L	sūtram 24	10 resto.
ij.	sūtram kritvā rūpa kshayam pārtha dhānta samgunanam tatah	
	pravrittir gunanam tatah vinirdiset	
ШL	udāc tri-bhāga maladagdhasya tri-dhāntasy aiva	
	ashtottara-śatāni dattam kim śesham vada pandita	
	$\begin{bmatrix} 108 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ & 3+ & 3+ & 3+ \end{bmatrix}$	
	kritvā rūpa kshayam pārtha† jātā 32 sesha prathamab† dhānte	
	kshayam 36 śesham 72 dvitīyab dhānte kshayam 24 śesham 48	
	tritīyab dhānte kshayam 16 sesham 32	
	pratyayam kriyate sthāpanam	
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	
	sajāti kriyā	

G 1. Folios 10 to 15 form a fairly well defined section and the leaves are among the best preserved of the manuscript. The 'find order' is 42, 41, 40, 39, 7, 29 and the writing a2. The sitra numbers 24 and 25 cocur.

^{[10} recto.] i. The end of the effire is marked with the usual design and the stitra is numbered 24; so that from 10 recto to the end of 15 recto consists of one stitra (25) and its illustrative examples.

ii. Of suitra 25 the only complete word preserved is visirdeset. It is reconstructed from quotations and fragments of letters. The saltra is the most quoted one in what remains of the original text, the phrase kriter typa kshayem parha occurring some seven times. The last word of this phrase is, however, variously written parha (fol. 10 recto), pasham (10 verso), pasham (12 recto et verso), pasha (14 verso) and is rather curiously omitted on fol. 11 recto. This variation is very curious, because the ligatures riha, sta are so very unlike that the differentiation can hardly be one of carelessness in writing (and the writing is here particularly good). The meaning of the term is still obscure. Dr. Hoernle suggested prasts 'thrown out' or 'wastage'; but I would translate the whole phrase by 'Having calculated for unity the loss per term.' The following is Dr. Hoernle's translation of the siltra—

^{&#}x27;Calculate the loss in one; let the instalments of wastage be multiplied together; with the result let the original provision be multiplied; take the result to be the required remainder.'

iii. The example may be rendered:

The third part of the burnt bronze in three instalments (is lost). The amount given was one-hundred and eight. State the

The solution according to the rule gives $106 \ (1-\frac{1}{4}) \ (1-\frac{1}{4}) \ (1-\frac{1}{4}) = 32$. But proceeding by steps $^{10.6}$ = 38 and the remainder is 72; ψ = 24 and the remainder is 32.

The proof may be represented by $x^1 = \frac{31}{(1-\frac{1}{2})} \frac{32}{(1-\frac{1}{2})}$. Continued on the reverse,

G 1—contd.

í.	tribhi tryashta-bhāga samyutam	10 verso.
	$\begin{bmatrix} 1\\3\\1 \end{bmatrix}$ + tudashtottara-śatā χ kim $\begin{bmatrix} 27\\8 \end{bmatrix}$ $\begin{bmatrix} 1\\1 \end{bmatrix}$ $\begin{bmatrix} 108\\1 \end{bmatrix}$ pha se 32	
	3+ yadyekasya trayas traya ashta bhaga tadā dvā-	
	3	
ii.	udā ^c sakrid dhāntasya lohasya daśāmsha kshīyate-s-trayam	
	saptate dviguņā, cha kini sesham vada paņditah 3 140	
	† kritvā rūpa kshayam pāstham† iti rūpam — 	
	jātam šesha $\begin{bmatrix} 7 \\ 10 \end{bmatrix}$ mūlam $\begin{bmatrix} 140 \\ 1 \end{bmatrix}$ anena gunitam jātam $\begin{bmatrix} 96 \\ 1 \end{bmatrix}$ kshayam $\begin{bmatrix} 42 \\ 1 \end{bmatrix}$	
	evam 140	
	$\begin{bmatrix} 1 & 98 & \text{phalam} & 140 \\ 10 & 1 & 1 \end{bmatrix}$	
3 1.	[10 verso.] i. Gives further proofs of the example on the obverse, namely $\mathbf{x}^1 \cdot (1 - \frac{1}{2}) \cdot (1 - \frac{1}{2}) \cdot (1 - \frac{1}{2}) \Rightarrow \cdot \cdot 32, \text{ hence } \mathbf{x} = 108 .$ then two proportions in words and figures $\frac{\pi}{3}$: $1 \cdot 108 32$ and $1 : 3\frac{\pi}{3} : 32 108$. ii. Example.—Of from one refined three-tenths is lost. What is the remainder of twice seventy, tell me Pandit? The loss of unity is $\frac{\pi}{10}$ and the remainder is $\frac{\pi}{10}$. The original quantity is 140 and $\frac{\pi}{10}$ of 140=98. The loss is therefore 42 and Proof. $\frac{\pi}{10}$: 1: 98: 140. Continued on fol. 11 resto.	
	G 2.	
l,	pratyayah 0	ll recto.
iı.	udā° palā krīte pala tri-bhāgam kshya vrajati	
	ashtā-daśa thatām brūhi	
2.	[11 Feeto.] i. Continued from fol. 10 verso. 'Proof $x(1-\frac{1}{10})=-98$, therefore $x=140>$ ii. Example.—In purchasing one and a half palse the loss is one-third. State what would be the loss on eighteen. Since $\frac{1}{4}/\frac{3}{4}=\frac{3}{4}$, the loss on unity, the remainder is $\frac{1}{6}$. Now $\frac{1}{4}$ of $18=14$ and the loss is 4.	
	Proof by the rule of three:— $1\frac{1}{4}:\frac{1}{4}:18:4$ and $\frac{1}{4}:\frac{1}{4}:\cdot 4:18$.	

G 2-contd.

$egin{bmatrix} 1 & 3 \ 3 & 2 \end{bmatrix}$	bhā 18 1
karanam addhyardha	palam-s-chhedebhya idam 2 †kritvā rūpa 9
kshayam† rūpam1	kshayam kritvä jätam 7 18 gunitam jätam 9 1
14 kshayam 4	
pratyaya trai-rāśikena 📗	
addhyardha pala krīte	tri-bhāgani kshaya gachchhati
ashtā-daśa pala krīta	kim kshayam vada pandita
$\begin{array}{c cccc} 1 & 1 & 18 \\ 1 & 3 & 1 \\ 2 & & \end{array}$	phalam 4 1
puna tri-bhāga divardham	tadā chatubhi χ kim iti
$\left[\begin{array}{c c}1&1&4\\3&1&1\\2&2\end{array}\right]$	phalam 18 1
ш. udā° chatur-bhāga n	nala dagdha suvarna sata-pamchakam
	atha pratyay 11 verso.
0 158 su° 1 1 to°	phalam mūla 500 🚺 punar eva prastāra kramam
1 . 5*	$egin{array}{cccccccccccccccccccccccccccccccccccc$
1 4 1 4+	śesha 158 to° 1 śe° 1 64
The solution is lost. It amounted to severe $a > 0$. Continued on the reverse. [11 verse.] This appears to have continued in the fourth. The proofs are— i. Missing. ii. $x^2(1-\frac{1}{2})(1-\frac{1}{2})(1-\frac{1}{2})(1-\frac{1}{2})=1$ iii. $800(1-\frac{1}{2})(1-\frac{1}{2})(1-\frac{1}{2})(1-\frac{1}{2})=1$ iv. $x^2=(158^\circ$ ev. x^2+1 , x^2+1 , x^2+1 , x^2+1 .	x* and x = 105 M + 1 1/2 10°,

G 2-concld.

anyam chaturtha pratyayam kriyate

0 1	1 1 1 1 4+ 4+	1 1 4+	1 bh	ā° śesł 	158 1 5* 1 64	phalam	500	11	
ādyam	kshayam	125	śesham	375	dvitīye	kshayam	93	to° 3	māśa 9
śesham	281 1 4	ks	hayam	70 5 16	śesham	210 15 16	k	shayam	52 47 64
śesham	158 13 64	ess	a sarvatra	kartav	yā				

G 3.

12 recto.

prastha madhunās tathāh
ambhasa
†kritvā rūpa kshayam pāstam † iti : tatra kshayam : pāstam : iti : tatra kshaya :
$rar u pam gu$ nya sesham $egin{array}{cccccccccccccccccccccccccccccccccccc$
t-prastham pivet gadyūti yojanam chatu prasthai
ādhakam tadā dhāntasor gu tatah 81 āvritti pravrittir-gunanam tatah
4 anena guņitam jātam $\begin{bmatrix} 81 \\ 64 \end{bmatrix}$ eša maddhva bhāgā bhāge hrite labdham
madnu prastha 1 ku° 1 śe° 1 ambha bhāgā prastha 2 kudava 2
se $\begin{bmatrix} 15 \\ 16 \end{bmatrix}$ evam $\begin{bmatrix} 4 \\ \end{bmatrix}$ kudavokti prakshepake ādhakā sodasha kudavā
bhavanti 16 ato ma

G 3. [12 recto.] This is not directly connected with folio 11 but is probably correctly placed here. The find order places it between folios 11 and 13 and it is definitely connected with folio 13. Also it quotes from silira 25 on folio 10 recto. It has the same knot as folio 13.

Continued on the reverse.

The example may be conjecturally restored: A traveller goes a journey of 4 gavyatis and takes with him 4 prasthas of wine. After each gavyatis he drinks 1 prastha and then fills up his bottle with water. How much wine and how much water will there be at the end of his journey?

G 3-contd.

. prastha kudavā | 4 | 3 | śesha chatvāra . . . 12 veno. kudavah $\begin{pmatrix} 7 \\ 1 \\ 4 \end{pmatrix}$ šeshā cha kudavā pītā | mac chatvári kudavā bhuktam šesham | 81 | 175 | jala bhāgam | madhu kudava jala kudava 1 evam kudava 16 || datvā sulkam chatur bhāgam ashtau anita kumkumā | ี∟ udã° chatu sulka sālais tu kim sesham vada paņdita 👖 8 1 1 guņitam śulke śeshain jātam anena guņitam jātam 4 1 | datvā guņita jātā
1 1 + | 1

Continued on fol, 13 recto.

G 3. [12 virso.] i. The solution of the example on the obverse is now done by steps. The original amount of 4 prasthus is expressed in kudawa, namely 16.

Of these 16 kudavas of wine he drinks \(\frac{1}{2} \) and 12 are left and he adds 4 of water. He then drinks \(\frac{1}{2} \) of wine and there are 9 kudavas left and the water is made up to 7 kudavas. Then he consumes \(\frac{1}{2} = 2 \) of wine and there are 9-2\(\frac{1}{2} = 7 - \) and the water is made up to \(\frac{1}{2} = 7 - \) and there is left \(\frac{1}{2} = \) \(\frac{1}{2} = \) and the water is made up to \(\frac{1}{2} = 7 \). There is, therefore, finally \(\frac{1}{2} = \) \(\

ii. Example.—Having given one-quarter as toll at four toll-houses eight of saffron is brought in. State, O Pandit, what is left.

Solution. $8 \times \frac{1}{4} = 6$ and 2 is paid in toll; $6 \times \frac{1}{4} = 4\frac{1}{4}$ and the loss is $1\frac{1}{4}$: $4\frac{1}{4}(1-\frac{1}{4}) = \frac{1}{4} < -\frac{3}{4}$ and the toll is $\frac{1}{4}$; $\frac{3}{4}(1-\frac{1}{4}) = \frac{1}{4} + \frac{1}{4} +$

G 4.

For these measures see part I, §109.

Continued on the reverse.

ii. Example.—There is a quantity of molasses weighing eight bhdrakus. What will be left after giving away one-third, one-sixth and one-fifth i 8.4.4.4 m 3 and this is the answer.

iii. Example.—By a gain of five-fourths ten dronus are obtained. Let it be said, O best of calculators, what will be the gain by see transactions. (E) the term libbs seems to have meaning 'capital + profit,' what is termed the 'mixed quantity' midrates on folio 62.

^{10 . \$. \$. \$ = 1250 &}lt; = 19 1 = 19 dro +2 dd +0 pra +2 ku >

G 4-contd.

0 bhā° se° 19 phalam 10 0 phalam dro° 19 ā° 13 mar 1 1 2 pra° 0 ku° 2 1 2 pra° 0 ku° 2 1 ku° 2 4 ku° 4* prasthi	18 0.
udā° kasyāpyarjjakasya shashthi sva-dalena kshayam gata puna vriddhyā tri-bhāgena sva-pādena tatojjhitam vriddhyā tu pamcha-bhāgenas tathā vriddhi dvayo garam kā vriddhi syā kim vā sesham tad uchyatām	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	
punānyam pratyayam 60 phalam 36 mūlam na jñāyate 1	
+ + + phalam .	

G 4. [13 verso.] i. Continued from the obverse.

⁽a) $\lambda^1 = \frac{10 \text{ dom} + 2.8 + 0 \text{ pm}^2 + 2.8 u}{(1+\frac{1}{4}, 0+\frac{1}{4}) (1+\frac{1}{4})} = 10$.

(b) $\lambda^1 = \frac{10 \text{ dom} + 2.8 + 0 \text{ pm}^2 + 2.8 u}{(1+\frac{1}{4}, 0+\frac{1}{4}) (1+\frac{1}{4})} = 10 \text{ dow}^2 + 2.6 \tilde{u} - 0 \text{ pr}a^2 + 2.8 u^2 < \text{whence } x^1 = 10>$. See Part I, p. 62.

ii. Example.—The capital of a certain banker is sixty. One half of it goes in loss and then he gains by one-third; next he loss one-fourth of it and finally gains one-fifth; so that he has two gains. What is his gain and what is his loss and what the remainder and let that be stated.

Solution: $60 (1-\frac{1}{2}) (1+\frac{1}{2}) (1-\frac{1}{4}) (1+\frac{1}{4})=36$.

Proofs. (a) $\sqrt{1 = \frac{3}{(1-\frac{1}{2})(1-\frac{1}{2})(1-\frac{1}{2})(1-\frac{1}{2})}}$, whence $x^1 = 60$. (b) $60 (1-\frac{1}{2}) (1+\frac{1}{2}) (1-\frac{1}{2}) (1+\frac{1}{4}) = 36 = 60$. (c) $x^1 (1-\frac{1}{2}) (1+\frac{1}{2}) (1-\frac{1}{2}) (1+\frac{1}{4}) = 36 < 60 > 60$

G 5.

1 1 1 5 1 5 1 1 5 1 1	apahrita śulka pindam 24 kritvā rūpā kshayam pāsta† 2 3 4 jātu samgunya 3 4 5 etāvad api rūpa samśudhā jātam 3 anena bhaktvā śulka 5 jātam 40 eśa pindam 40 gunita jātam 16 śesham 24 evam 40	
karanam jātam 2 5 pindam gunitam pratyayam 2 5	kritvā rūpā kshayam pāsta† 2 3 4 jātu samgunya etāvad api rūpa samsudhā jātam 3 anena bhaktvā sulka jātam 40 esa piņdam	
jātam 2 5 piņdam guņitam pratyayam 2 5	etāvad api rūpa samsudhā jātam 3 anena bhaktvā sulka 5 jātam 40 esa piņdam	
pindam gunitam pratyayam 2	jātam 40 eśa pindam	
pratyayam 2		
_ 5	40 gunita jātam 16 sesham 24 evam 40	
anyam asya prat	yayam 40	
n. udā° guḍa	pinda jñāta tulyoś chatu avye gudam	
tri-cl	natu ϕ -pamcha-shad vriddhya chatvārimsa (bha*) ve kshaya	
still quotes from the same Solution: \$.\$.\$.\$\$, 1 Proof: \$ of 40=16 an Another proof of this:	40 (1-\frac{1}{4}) (1-\frac{1}{4}) = 16 and 40-16 = 24. n amount of molasses equal to . four is increased by one-third, one-fourth, one-fifth, one-sixth	
· udā°]] ajñāt	ārambha-lohasya tri-chatu φ-panichakā kshaye 14	verso.
sapta	-vimsati piņdasya tri-dhānta šeshya drishyate	
kim s	arvam vada tatvajña 🧪 kshayam cha mama katthyatām 📙	
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	
	le.—An unknown quantity of lapis lazuli losss one-third, one-fourth, and one-fifth; and the remainder	

G 5. [12] verso.] (i) Ezample.—An unknown quantity of lapse lazult loss one-turd, one-tourth, and one-into; and the remainder after the three-fold operation on the original quantity is twenty-seven. State what the total was, O wise one, and also tell me the loss.

Solution §.§. § = ‡; 1—‡ = 2; 27—‡ = 45 and 45—27 = 18 and this is the loss.

The meaning of ambha-loha = lapis-lazult was suggested by Dr. Hoernle.

G 5-contd.

	karaņam	† kritvā rūpa kshayam pāstha† 2 3 4 guņitam 3 4 5
	jātarh	2 rūpa kshayam 3 anena sesham bhaktam sesham 27
	bhaktam	jātam 45 asya saptā-vimsa pātya sesham 18 eta
	kshayam	11
IJ.	udā°	parikshīņasya lohasya tri-dhāntam pamcha māśakam
		na jñāyatet pravrittkām na tu sesha pradrisyate
		pravritti sesham yo pindam kevalam vinisati sthitam
		ajňāta kām pravritti syā kim vā šesham vadašva me
		1 1 1 kritvā 3 4 5

This interpretation, however, is by no means certain. The solution is lost,

G 6.

. pravritti hhavet sakhe 15 verso. $\left[\begin{array}{c|cccc}1&1&1&1&1\\3&3&3&3&3\end{array}\right] \text{ se } 16$ karanam | dhāntaso ghātitam tena | †rūpa kshayam kritv↠jātam

ii. Example.—Of the loss of iron the third is one-fifth of a masha. The original quantity is not known and neither is the remainder given; but only the original remainder which quantity stands at twenty. Tell me what is the unknown original quantity and what is the remainder.

^{[15} cerso.] There is a suspicion that this is a double leaf. The lenticels on the h ft side are well-marked but hardly any trace of them appears on the right side. Also the contents are to some extent incongruous.

The example may be represented by $x (1-\frac{1}{2}) (1-\frac{1}{2}) (1-\frac{1}{2}) = 16$. Now $\frac{3}{2},\frac{3}{2},\frac{3}{2}=\frac{1}{2}$ and $16+\frac{1}{2}=81$ and this is the original

quantity.

Another method by kala-savaras. (This term laterally means 'parts resembling one-sixteenth.' but by Mahavira it is used to denote tractions generally iii. 1). The question is inverted: 'Of iron (refined) four times eighty-one is given. What is the remainder, state, O expert, which is solved by working hard in calculating. 81 $(1-\frac{1}{2})(1-\frac{1}{2})(1-\frac{1}{2})(1-\frac{1}{2})=16$.

[&]quot; Another proof is made and the original amount is not known."

 $x^{2} = \frac{16}{(1-b)(1-b)(1-b)(1-b)} = 81$ pain.

G 6-contd.

2 2 2 2 gunitam 16 bhaktam 81 seshena gunaye 3 3 3 3 81 śesham 16 gunita jātā 81 ... pravrittir ity artham 1 athānya vidhi kalā savarņe chatur dhānta . lohasya ekasıtıs-cha dattavān kim sesham vada dharmajna ya ganite kritam sramam puna pratyayam kriyate mūlam na jñāyate 0 1 1 1 1 bhā° śe° 16 | phalam loha pala 81 || 1 1 1 3 + 1 3 + 1 3 + 1 | 15 recto. kaśchi yadi śakya tad uchyatam dhānta kshayam vichāranāh etan me samsayam prājnad 2 3 4 ksha° śe° 32 3 4 5 1 karaṇam || dhānta samguṇya guṇitam jātam | $\frac{3}{5}$ | rūpam dadyā | $\frac{8}{5}$ bhāge hrite labdham bhak...... 5 32 8 1 phalam 20 esa sā pravritti śesham 12......32 || pamcha-vimśatima sūtram || 25

The example may have been:— $(1-\frac{1}{2})(1-\frac{1}{2})=x-r$ and x+r=32. From this $\frac{1}{2}x=x-r$, $(1-\frac{1}{2})x=r$, $\frac{1}{2}x=x-r$, $\frac{1}{2}x=x$

G 7.

L	vibhaktar	m jātam 2 śe° 10
	anena gu	nitam jātam 90 bhāge hrite labdham 12
	asya prat	tyaya trai-rāśikena
		$egin{array}{cccccccccccccccccccccccccccccccccccc$
ij.	udã°	mākshikag-ghatakasyaiva dvi-tri-bhāga pravardhitam
		dvitiye dvi-pamchamo-bhāgo tritiye dvi-saptakodbhavam
		chaturthe dvi-navam-bhāgam evam jāta pala trayam
		babhūvā saulkikai hritvā kim sarvam vada paņdita
		$egin{array}{cccccccccccccccccccccccccccccccccccc$
	dhāntaso	iti kritvā

^{[16} recto.] i. The find order is 30 and the writing is α2.4. Only the remnants of a problem: Loss on $\frac{1}{4}$ is 7/6; what is the original when the remainder is 10? Loss on 1 is $\frac{1}{4}+\frac{1}{4}=\frac{1}{4}$ therefore x $\frac{1}{6}=10$ and $x=\psi=12\frac{1}{4}$.

Proof by the rule of three: $\frac{1}{4}:10:12\frac{1}{4}$. It is the second two-fifths, to the third two-sevenths, to the fourth two-ninths, till only three pales (are left) O Pandit, state how much altogether was taken away by the tax collector.

H 1.

	sütram	16 verse.
i.	idāni suvarņa kshayam vakshyāmi syedam	
ii.	sütram kshayam samgunya kanakās tadyutir bhājayet tatah	
	samyutair eva kanakair ekaikasya kshayo hi sah	
iii.	udā° eka-dvi-tri-chatus sankhyā suvarņā māshakai riņai	
	eka-dvi-tri-chatus samkhyā rahitā sama-bhāgatām 📗	
	sthāpanam krivate eshām $\begin{vmatrix} 1+ & 2+ & 3+ & 4+ \\ 1 & 2 & 3 & 4 \end{vmatrix}$	
	karanam †kshayam samgunya kanakādibhi† kshayena samgunya jātam	
	1 4 9 16 esha yuti 30 kanakā yuti 10 anena	
	bhaktvā labdhani	
	by the remark—"Now I shall speak about suvarna kahaya." It should be noted that Mahkvira uses the term kahaya as synonymous with varna in his section (vi, 189ff) on suvarna kwitikāra. In our text there seems to be some confusion about the meaning of kahaya which here really means varna or 'quality' although the author obviously thought it denoted a loss. Mahkvira's rule is— **Ranaka kshumi samvargo miśrasvarnāhritah kshaya fūeyah paravarna pravibhaktam suvarna gunitam phalam hemna 169 "It should be known that the products of gold kshaya, when divided by the mixed gold gives rise to the kshaya. When divided by the last varna (=kshaya) and multiplied by the gold gives the corresponding quantity of gold." ii. Rule.—Having multiplied the parts of gold with the kshaya let this sum be divided by the sum of the parts of gold. The result is the average kshaya. This means f= 1 \cdot 2 \cdot 1 \cdot 2 \	
i.	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	17 recto.
iL.	udā° eka-dvi-tri-chatus samkhyā suvarna projjhitā ime	
	māśakā dvi tritām chaiva chatu samkhyā pamchakarāmśakam	
	kim kshayam	
	1 2 3 4	
	$egin{bmatrix} 1 & 2 & 3 & 4 \ 1 & 1 & 1 & 1 \ 2 & 3 & 4 & 5 \ \end{bmatrix}$	
H 1.	[17 redo.] i. The remnant of a proof of the example given on 16 rerso. 10: 30: 4: 12, i.e., $\Sigma g: \Sigma f g: g, \cdot g, F$. ii. Example.—Gold one, two, three, four; 'abandoned' the following maskakes one-half, one-third, one-fourth and one-fifth. $F = \frac{(1+\frac{1}{2}+\frac$	

H 2-contd.

	1 .		1	300		
	10	163 60	3	pha° 163 200	! ! ! ! !	17 v e
	, 10 1	163 60	4 1	pha° 163 150	1	
krameņa dvay suvarņam me sthāpaņam 4+ 5		·	atām į			

H 3.

L	(sūtram)	aprāpta samgunā kati kamchanāni tatojjhitam	18 recto.
		kāmchanai yad bhave labdha sa kshaya jñāta māśaka	
i i.	udā°	eka-dvi māshako prāpto dvau cha prāptam cha pamchabhi	
		trayaś cha katibhi¢prāpta shad eva . ni kevalam	
		chaturbhi māshakair hīṇain kaṭi dṛishṭvā mayā sakhe	
		trayas cha katibhi ¢ prāptā suvarņām masako vadaḥ	
		$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
	karaņam	† †aprāpta samguņā katīd† iti 6 aprāpta kaṭi chatvāra 4	
	samgunye	†kāmchanāni tatojjhitam† dvābhyām eka pamchabhi	
	dvayam ı	samgunya jātam 2 10 tad yuti 12 hitvā 2	
	hitvā jāts	m šesham 12 aprāpta gandikai	
н а.	F= 1, 5, 1, 1, 2, 2, 1, 1, 2, 2, 2, 1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,	i. The salm is largely restored from the quotations given in the solution below. The application of the terms aprapta t at all clear; but given that $ \frac{F \cdot \Sigma g - (f_1 g_1 + f_2 g_2)}{f_2} + g_1 + g_2 + g_2 + g_3 +$	
		ashta-vimsatima sūtram	18 verso.
i.	sūtraṁ	ii unais samgunya kanaka tat pindam cha visodhayet	
		suvarņa kanakābhyastā rāśi shesham vibhājayet	
		aprāpta gaņdika śeśa śuddhena kanakena tu	

^{[18} verse,] The end of the 28th edira is marked.

i_s_Bule.—Having multiplied together the (known); gold pieces and their versus determine the sum of that. Divide the remainder of that quantity and the sum of the product of the average versus and known gold by the difference between the average versus and the versus of the unknown gold. That which results consider to be the measure of the unknown gold.

This may mean, for example, that if $F = \frac{f_1}{g_1 + g_2} \frac{g_1 + g_2}{g_1 + g_2}$ then $x = \frac{(f_1 \cdot g_1 + f_2 \cdot g_2) - F_2}{g_2 - g_2}$. H 3.

H 3-contd.

11.	udā°	11	eka-dvi-tri-chatus sainkhyā aprāpta māśakāni tu
			eka-dvi-tri-chatus sainkhyā ekatrāvartitā kilah
			gandikā jūāta kanakā ūnaikā daśa māshakai
			aprāpta jūāta kanakai pra yah
			$egin{array}{c c c c c} 1 & 2 & 3 & 4 & 0 \\ 1 & 2 & & & & \\ \end{array}$
	karan	ari	1

J 1.

	· · · · · · · · · · · · · · · · · · ·	
sūtram	eka yuta nara sarvash shadbhi pa	
	anena labdham hītā pratham	
	36 42 48 54 6 78 7.	
	sadriśa kri bhāga hāram kriyate 234	30 ven
tu	alādhe 3 mudgādhe 1 kriyate 24 47 70	
, [Folio 30.] fol. 31.	Find order 32. Writing α4. By appearance this fragment and fol. 28 perhaps belong to the same leaf. See also	
[30 recto.]	A restoration is suggested in part I, §78, vii, but I doubt its being correct. We have $\frac{1}{2} = 34\frac{\pi}{3}$ and $\frac{34\frac{\pi}{3} + 2}{3} = 1\frac{\pi}{3}$. The term $mudga$ ' 'a kidney bean' occurs also on folio 31. See also	
	J 2.	
	J 2.	
	timanushyā ya lagyanti	đố ro
etat-kāla apara pras	timanushyā ya lagyanti	đố ro
apara pras	timanushyā ya lagyanti	đố ro
apara pras	timanushyā ya lagyanti shṇaḥ	6ő ro
apara pras yady (prastu	shnah eka purushasya drammāsh-shat, trimšabhir dinai jīva-lokā tat kāryam	66 red
apara pras yady (prastu	shnah eka purushasya drammāsh-shat. trimšabhir dinai jīva-lokā tat kāryam utam ssaptatīnām pāka rākshakānām drammaish-shadbhi	66 rec
apara pras yady d prastu kati d karanam	shnah eka purushasya drammāsh-shat. trimšabhir dinai jīva-lokā tat kāryam utam ssaptatīnām pāka rākshakānām drammaish-shadbhi dinā jīva-lokam bhavati .	бб гос
apara pras yady o prastu kati d karanam	shnah eka purushasya drammāsh-shat, trimšabhir dinai jīva-lokā tat kāryam utam ssaptatīnām pāka rākshakānām drammaish-shadbhi linā jīva-lokam bhavati l ādau tāva yady ekapurushasya drammāsh-shat trinšabhi	66 rec
apara pras yady o prastu kati d karanam	shnah eka purushasya drammāsh-shat. trimšabhir dinai jīva-lokā tat kāryam utam ssaptatīnām pāka rākshakānām drammaish-shadbhi dinā jīva-lokam bhavati l ādau tāva yady ekapurushasya drammāsh-shat trinšabhi tat saptatīnām kim 1 pu° dram° 6 30 di° 70 pu° phalam 1	₫ŏ rec
apara pras yady o prastu kati d karanam jivyāh drammā	timanushyā ya lagyanti shṇaḥ eka purushasya drammāsh-shaṭ. trimśabhir dinai jīva-lokā tat kāryam utam ssaptatīnām pāka rākshakānām drammaish-shaḍbhi linā jīva-lokam bhavati ādau tāva yady ekapurushasya drammāsh-shaṭ trinśabhi tat saptatīnām kim 1 pu° dram° 6 30 di° 70 pu° phalam 1 trīni śata-sā	66 rea
apara pras yady prastu kati d karanam jīvyāh drammā	timanushyā ya lagyanti shṇaḥ eka purushasya drammāsh-shaṭ.trimśabhir dinai jīva-lokā tat kāryam utam ssaptatīnām pāka rākshakānām drammaish-shaḍbhi dinā jīva-lokam bhavati tādau tāva yady ekapurushasya drammāsh-shaṭ trinśabhi tat saptatīnām kim 1 pu° dram° 6 30 di° 70 pu° phalam 1	65 re

live on six drammas? The details are, however, uncertain.—K. N. D.]

J 3.

^{3.} Folio 41 is much damaged and the illustration (Plate xxviii) suggests a double leaf; but the illustration is deceptive, for the cause of the uneven colour is the presence of game on the original leaf. The find order is unknown: writing at.

^{[41} resto.] This is undoubtedly closely connected with fol. 65 resto and the repair of fol. 41 and the separation of the two parts of fol. 65 would possibly make both intelligible.

^[4] verso.] Not understood. "Possibly the 8 and 6 are change-ratios.

K

ì	$ud ilde{a}^\circ$ ko ră	āsi pamcha yutā <i>mūladaḥ</i> sā rāsis sapta hīna	59 recto
	mūlada ko so rās	śir iti prashņah	
	0	5 yu° mū° 0 sā 0 7+ mū° 0 1 1 1 1	
	karanam †y	yuta hinam cha-m-ekatvain† 12 tad dalam 6 dvi	
	hrinam 4	dalam 2 vargam 4 thine yutim cha kartavy↠	
	hinam 7+	anena yuti 11 eśa sā rāśi asya pratyānayam kriyate	
		$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	
	pamchāšama sūt	tram 50	
ii.	sūtram gavān	m višeshu kartavyam dhanam chaiva puna	

^{[59].} The find order is unknown but the saits number is 50 and it probably originally preceded fol. 60. The reverse is blank, which possibly means that there are portions of two leaves stuck together.

(i) Example.—What number with five added is a square and that same number with seven subtracted also being a square? What is that number? is the question. K

Statement $x+5=s^2$, $x-7=t^2$.

⁸ Solution $\langle x=[\frac{1}{2}(\frac{\delta+7}{3}-2)]^2+7=11$ by steps thus > : having combined the added and subtracted numbers $\delta+7=12$: that haired -6; two subtracted 4; haived 2; squared 4; then the subtractive number (7) is to be added and by the addition of this 4+7-11 and this is the required quantity.

Proof: 11+5-4*, 11-7-2*. See Part I, §81.

⁽ii) There appears to be a reference to this fragment on fol. 60 recto where suites 51 is closed.

L 1.

• • • • • • • • • • • • • • • • • • • •
ekona-vimsatima gāvo 10 rūpa 8 vivaritāsti 1
eka pamchāsama sūtram 51
sūtram aya vyaya višesham tu vibhajya drishya samgunam
yal labdhan sā bhavet kālam ayam prashne . ya vidhi 📗
udā° dvi-dine ārjaye panicha tri-dine nava bhakshaye
bhāṇḍāgāram tasva trinsā kim kālam ārja bhakshaņam
$\frac{\mathrm{d} i^{\circ}}{\mathrm{d} i^{\circ}} \frac{5}{2} \qquad \frac{\mathrm{d} i n \bar{a} r a}{\mathrm{d} i n a} \frac{9}{3} \qquad \frac{d r i^{\circ}}{30}$
karaṇam †āyā vyaya viseshan tu† tatrāyam 5
· ·
[60.] Writing a2. Notice the 'sickle's. Find order unknown. Connected with fol. 59 on one side and folios 61—63 on the other. Folios 60—63 form a fairly definite section (L) relating to earning and spending. [60 recto.] (i) This fragment is connected with the satra at the bottom of fol. 59, but very vaguely. (ii) Rule.—The known quantity is divided by the difference between the expenditure and earning. This result is the time This means t— * (iii) Example.—In two days one calms five, in three days he consumes nine. His store is thirty. In what time will his earnings be consumed?
Solution: $t = \frac{30}{1-6/2}$ < 60 and the amount earned in this time is ξ of $60 \cdot \cdot \cdot 150$ dinaras.
bodi phalam 180 dvāpamchāśama sūtram 52 60
sūtram aha dravya harāśauta tad višesham vibhājayet
yal-labdhan dviguņan kālam° dattā sama-dhanā prati
[60 verso.] (i) Remnant of proof of the example on the obverse. The complete proof probably was:— 2 days: 5 dindra:: 60 days: 180 dindra 2 days: 9 dindra:: 60 days: 180 dindra and 180—150—30.
(ii) Rule,(If one carms e ₁ in d ₁ days and anothere ₂ in d ₂ days and the first gives g to the second then d ₁ t−g = d ₂ t+g and) t= e ₂ d ₃ d ₄ t+g and t= e ₄ d ₅ d ₄ d ₅

L 1—contd.

ш.	udā°	1	tri-dine ărjaye panicha	bhritako-m-eka panditah
			dvitīyam pamcha divase	rasam ārjayate budhah
			prathamena dvitīyasya	sapta dettā nidhānatah
			datvā sama-dhanā jātā	kena kālena katthyatām
			5 rū	6
			3 di	6

See Indian Antiquary, XL11 (1888), pp. 41, 44; but in 1915 Dr. Hoernle sent me the following note:—"The textual difficulty was not fully understood by me: the text is badly corrupted, a portion (the 2nd påda) has dropped out, and another (the lat påda) has been mixed up with the commentary. The real text of the first påda is quoted in obverse line 8 of the next folio, in the commentary of the second example of the sātra, and the missing part of the social påda must be supplied from obverse lin. 4 and 5 of sātra 52; which is merely a variant of satra 53. The latter sātra should really run as follows:—

ahadravya risesham cha ribhajya datta samgunam | yal-labdham drigunam kalum datta sama dhana prati ||

Solution: $t=\frac{3\times7}{5/8}=30$.

L 2.

pratyayam trai-rāśik	ena kri <i>yate</i>		
3 5 30	pha° 50	prathame dvitīyasya (s) sapta dattā 7	.]
5 6 1 30	36	prathame dvitīyasya (s) sapta dattā 7	

L 2. [61 recto.] i. The end of the solution of the example given on sit verso.

Proof by the rule of three: 3:5::30:50 and 5:6::30:36 and 50-7-43=36+7.

i.e., "the difference of the daily earnings, having divided (invested), is multiplied with the given amount: the result being doubled is the time; the given amount goes towards making the possessions equal."

⁽iii) Example — In three days one pandit cams a wage of five and a second wise man earns six (rasa) in five days. The second is given by the first seven from his store and by this giving their possessions become equal. Let it be stated in what time.

L 2-contd.

prathamena dvitiyasya daśa dināra dattavān
kena kālena samatām gaņayitvā vadāśū me 📗
$egin{bmatrix} 13 & 3 & & ext{dattam} & 10 \ 6 & 2 & & 1 \end{bmatrix}$
karaṇam †aha-dravya viśesham cha† tatva
ii. Example.—Two Rājputs are the servants of a king. The wages of one are two and one-sixth a day, of the second one and one-half. The first gives to the second ten dināras. Calculate and tell me quickly in what time there will be equality. (Indian Assignary, 1888, p. 44). Statement: \$\forall \cdot \hat{q}\$, given 10. Solution: The difference of the daily earnings,
55 56 sama dhanā jātā
sūtram tri-pamchāsamah sūtram 53
sūtram vikrayena krayam bhājyam rūpa hīnam punar bhajet
lābhena guṇaye tatra 🛮 nivī bhavati tatra cha 📗
udā° dvibhi x krīņāti yas sapta vikriņāti tribhish shat
ashtā-daśa bhaved lābhā kā nīvī tatra katthyatām
7 6 18 lābhā

L 2.

^{[61} verso.] i. Proof of example on the obverse—

1: \(\frac{V}{2} :: 30 :: 65 \\
1: \(\frac{V}{2} :: 30 :: 45 \) and 65—10=45+10.

ii. The rule means $C = \frac{p}{c(s-1)}$ where C is the capital, p the profit, c the rate of purchase and s the rate of sale.

iii. Example.—One buys 7 for 2 and sells 6 for 3 and 18 is his profit. What was his capital P

Solution.— $C = \frac{18}{(s-1)} = 24$. The proof is given on folio 62 recto.

L 3.

	nīvī jātā sya pratyaya trairāśikena 62 roota
	yadi dvibhis sapta labhyate tadā chaturvimsatibhi χ kim
	2 7 24 phalam rū° 84 1 1 1 1
L	asya vikrayam kriyate \parallel yadi shadbhi traya labhyate tadā chaturāsītibhi χ
	kim
	6 3 84 phalain 42 mülain 24 pātya sesham 18 esa lābhāh
	chau-pamchāsama sūtram 54.
ıL	sūtram , vikrayam bhājaye chaiva guņayet kraya piņdatām
	rūp <i>one</i> mūla guņaye - labdha lābham cha prāpyate -
iii.	udā° dvibhi krīņāti yas sapta vikriņāti tribhish shat
	mūlā cha
l. 3.	[62 recto.] L. Continued from folio 61 cerso. "Iffortwo 7 are obtained, then what for twenty-four?"
	2 7 : 24 - 84 articles. Again " If by six three are obtained then what for eighty-four?" 6 - 3 : 84 - 42
	and the original quantity was 24 and the difference $42 \div 24 = 18$. ii. The rule means $p = C(c/s - 1)$
	iii. Example.—Attacles are bought at 7 for 2 and sold at 6 for 3.
Ĺ	2 7 24 pha° 84 atha vikrayani 6 3 84 62 verso. 1 1 1 1 1 1 1 1 1
	pha 42 24 pātya śesham 18 esha lābham 1
	pameha-pamehāsama sūtram 55
ii.	sūtram 🔒 vikrayam bhajaye chaiya - ganayet kraya pindavat
	vibhaktam sa cha kartavyam gunaye misrakam budhah
	yal labdham sā bhaven mūlam yatch . chhesham lābha piṇḍatām
	2
L 3	[62 verso.] i. Solution.—Continued from the obverse; p=24 (\frac{1}{2} \dip \frac{1}{2} \dip 1)=18. Proof.—2: 7:124: 84 and 6:3:: 84: 42 and 42-24=18 is the profit. M. Rule,—C=\infty \dip \dip \dip \dip \dip \dip \dip \dip

L 3-contd.

	L & conta,
#1.	· udā° tribhis cha labhater ashtau chaturbhis cha vikrayamsh shat
	sa mūla läbham utpaņņa satam sashti vimisritam
	kim mūlam kascha lābham cha kathayed gaņakottamah
	, g.,, II
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
	karanam †vikrayam bhājaye chaiva gunayet†
	• • • • • • • • • • • • • • • • • • • •
	iii. Example.—Eight articles are obtained for three and six are sold for four. The sum of the capital and profit is one-hundred and sixty. State, O best of calculators, what was the capital and what is the profit The solution is lost except for the first quotation, but part of a proof is given on folio 63 rects. The solution was $< C = \frac{100}{1+\epsilon} = 90$ and the number of articles bought was $\frac{1}{4}$ of $90 = 240$.
	L4.
i.	1 240 phalam 90 1
	6 4 240 phalam 160 mülam 90 patya sesham 70
ii,	shat panichāśama sūtran 56
	vikrayam cha vibhaktavyam gunitam kraya rāsivat
	kritvā rūpa kshayam chaiva vibhaktam mūlam āpnuyāt
lii.	udā ^c pamchabhiś chatu vargam tu grihitam kena manava
	kenash shat vikrītamsh - shat pamchasa riņam kritam
	kvava vikrava samgunya – nivis tasyaiva kathyatām
	$egin{array}{cccccccccccccccccccccccccccccccccccc$
	bhājaye chaiva 1 6

L4

^{[63} recto.] 1. Proof of example given on folio 62 verso.

8 3 : 240: 90 and 6: 4:: 240: 160 and 160=-90+70.

ii. The rule means $C = \frac{1}{1-r_0}$, where I is the loss sustained, i.e., having investigated the selling rate multiply with the purchase rate and having subtracted from unity divide—and the capital is obtained.

iii. Example.—With five four squared are obtained by some man. For one six are sold and fifty-six is the loss. Calculating purchase and sale let his capital be stated.

The solution is $-C = \frac{r_0}{1-r_0} = 120$ and the number of articles is $\frac{r_0}{r_0}$ of 120 = 384.

L 4—contd.

L.	punāsya vikraya 6 1 384 phalam 64 mūlam 120 68 verso
	chatush shashti pātya šeshani 56 eša riņani kri
	saptā-pamchāśama sūtram 57.
u.	sütram vastra sulkam yad bhavati tada hrita vastratam
	trai-rāśika vidhānena śulka vikraya tatvatah
iii.	udā° patasya śulka vimśāńśam ka tris-śatam
	paṭa-kānām paṇa kṛite dvau patau hṛita śaulkikau
	mūlyam pana dašas teshāh kim mulyam

M 1.

	1 20 rakti dhā° 1 su° 1 chhe° 80* rakti-su° rakti 1 pha° dha° 4 1 1 1 1 1 1 a° 0 ya° 4 ya° 1 pā° 3 mū 1 1 4	20 recto
	puna tritiyasyaiva 2 20 1 1 1 1 1 3 1 1 1 1 1 1 1 1 1 1 1 1 1	
	chhedam 6 dhā°-dra° pha° dhā° 4 ya° 1 pă° 2 mū° 1	
	suvarņasya māņam samā	
i.	udā° sa panicha nava bhāgāņi dināni trayo-daśaḥ	
	· · · · · · · ·	
	i. A fragment of a solution or 'proof'. There were at least three statements, of which the second is 11 of 20 rakts: 1 dha + 41 ya	
	 1: law'+1 ra': 4 dha'+1 ya'+3 pa'+1 mū'-on 25 ra': 2025 mū'-: 81 ra': 6561 mū >. Then a similar statement of the third (restored) 2½ of 20 rakti: ½ dra'+½ ½ dhā'+½ ya': 1 su +1 ra': 4 dhā'+1 ya'+1 ka'+2 pā'+1 mā' < or 45 ra': 3625 mū'-: 81 ra': 6525 mū'>. The numbers marked with asterisks are change-ratios. See Part 1, §§ 103-104; and § 110 for the measures employed. ii. Example.—Too mutilated to restore. 	
•	Then a similar statement of the third (restored) $2\frac{1}{4}$ of $20 \operatorname{rakti}: \frac{1}{4} \operatorname{dra}' + \frac{1}{4} \cdot \frac{1}{4} \operatorname{dra}' + \frac{1}{4} \cdot \operatorname{ya}' : 1 \operatorname{su} + 1 \operatorname{ra}': 4 \operatorname{dra}' + 1 \operatorname{ya}' + 1 \operatorname{ka}' + 2 \operatorname{pd}' + 1 \operatorname{ma}' < \operatorname{or} 45 \operatorname{ra}': 3825 \operatorname{ma}' : 81 \operatorname{ra}': 6525 \operatorname{ma}' >.$ The numbers marked with asterisks are change-ratios. See Part 1, §§ 103-104; and § 110 for the measures employed.	20 verso
	Then a similar statement of the third (restored) 2½ of 20 rakti: ½ dra' + ½,½ dhāc + ½ ya': 1 su + 1 ra': 4 dhāc + 1 yac + 1 kac + 2 pāc + 1 mac < or 45 ra': 3825 māc >. The numbers marked with asterisks are change-ratios. See Part 1, §§ 103-104; and § 110 for the measures employed. ii. Example.—Too mutilated to restore.	20 verso
	Then a similar statement of the third (restored) 2½ of 20 rakti: ½ dra' + ½.½ dhā' + ½ ya': 1 su + 1 ra': 4 dhā' + 1 ya'' + 1 ka'' + 2 pā'' + 1 mā'' < 0.525 mā'' >. The numbers marked with asterisks are change-ratios. See Part 1, §§ 103-104; and § 110 for the measures employed. ii. Example.—Too mutilated to restore. mū 12000	20 verso
	Then a similar statement of the third (restored) 2½ of 20 rakti: ½ dra' + ½ ½ dhā' + ½ ya' : 1 su + 1 ra': 4 dhā' + 1 ya' + 1 ka' + 2 pā' + 1 mā' < or 45 ra': 3825 mā' >. The numbers marked with asterisks are change-ratios. See Part 1, §§ 103-104; and § 110 for the measures employed. ii. Example.—Too mutilated to restore. mū 12000	20 verso
	Then a similar statement of the third (restored) 2½ of 20 rakti: ½ dra' + ½½ dhā' + ½ ya' : 1 su + 1 ra': 4 dhā' + 1 ya' + 1 ka' + 2 pā' + 1 mā' < or 45 ra': 3025 mā' >. The numbers marked with asterisks are change-ratios. See Part 1, §§ 103-104; and § 110 for the measures employed. ii. Example.—Too mutilated to restore. mū 12000	20 verso
	Then a similar statement of the third (restored) 2½ of 20 rakti: ½ dra' +½ ½ dhā' +¼ ya' : 1 su +1 ra': 4 dhā' +1 ya' +1 ka' +2 pā' +1 mā' < or 45 ra': 3025 mā' >. The numbers marked with asterisks are change-ratios. See Part 1, §§ 103-104; and § 110 for the measures employed. ii. Example.—Too mutilated to restore. mū 12000	20 verso
•	Then a similar statement of the third (restored) 2½ of 20 rakti: ½ dra' + ½ ½ dha' + ½ ya' : 1 su + 1 ra': 4 dha' + 1 ya' + 1 ka' + 2 pa' + 1 ma' < or 45 ra': 3025 ma' > . The numbers marked with asterisks are change-ratios. See Part 1, §§ 103-104; and § 110 for the measures employed. ii. Example.—Too mutilated to restore. mū 12000	20 verso

t of an angula a day. In what time will it have completely entered is hele $(\frac{1}{2}+\frac{1}{12}-\frac{1}{2}\frac{1}{2})$ and $\frac{1}{2}\frac{1}{2}$ years: 18×24 and 2 years 4 months led dayiii. Example. —A worm....(see Mahavira. V. 5).

M 2.

	udā°	II	sumeru prithivi samku surānām parimāsrayam il	33 verso.
			āga . χ kašchi tarasā suramadiram 🚻	
			satatam sapta-sārdhāṇām—sa pamadhya	
			sa tri-bhāgā tri-pamchāniśa nityam evam cha gachchhati	
			yojanānātii sahasrāņichatur-āšītir uchchhritam	
			kena kālena sau gachchhe vada me ta śuniśchitam	
	• •	•	7 di l vo 84000 adha chchhedam 360* di $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$	
М 2.	and the d and one-f considered Ther	lwellin ifth. d answ e is sor	Example.—From the home of the gods a certain person desires to ascend swiftly St MERU, the pole of the Earth g place of the gods. He goes constantly at the rate of seven times one and a half and its quarter with one-third. The height of Sumeru is eighty-four thousand yopinus. In what time will be reach the summit? Give me well term doubt about the rate of going and the only clear parts of the statement are the second and third terms (1 day mas), but possibly the complete statement was $7(1-\frac{1}{2})(1+\frac{1}{4})(\frac{1}{2}+\frac{1}{4})uv \cdot 1 \text{ day} := 84,000 \text{ yo} \leftarrow \frac{1200000}{120000000000000000000000000000$	
L	นdลิว	1)	dināra ko nāma višā ttī du z khārjanīyam sukha-bhojane cha	33 recto.
	tasyā	rdha	am ardhain cha yad ardhain ardhain ta ke . deva guru prasādam	
	kripa	ņa d	hana bhuktam	
			$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
ii.	udac	11	ardham stāram nava roma śatāni cha	
	dvāda	sa s	tīti charmāni kati romā	
			12 24 1 1	
	900	12	2 24 12 24 pha° roma 1 1 1 1	
		erto.] i	i. Example.—The earning of dinaras is difficult but consuming them is easy. One gives one-half increased by ration	

^{[33} recto.] i. Example.—The earning of dinaras is difficult but consuming them is easy. One gives one-half in of one half (six times) for food for the poor. What is the amount consumed in 108 days?

1: \(\frac{1}{2}, \frac{1}{2}, \frac{1}{

M 3.

	. chandraanibhāṇa	32 recto.
	tu gaganam nita ravane ra yam	
	tyakta sutaya éetayā sā kai kena parāvartam dhanur bhāga éa	
	pa vane patamānasau daśa bhāgam nidhāryate evam tat	
	parimāņa . hīya mānam tu nityasah kiyatas tu parāvartaī bhūmim	
	prāpyayate ja .	
	dha ^c 1 1 + parā ^c 8 yoja ^c 30 chhe ^c 8000 yo ^c -ja ^c 1 1	
	phalam parā° 218181 śe 9	
i.	udā° nāga śva chehharma gāmi dratama daša	
	i. A mutilated example about RAVANA and (?) Sits. When Sitä had been carried up 30 yoqanas into the air she dropped something to earth, which turned over 8 times in 1, dhanus. How many revolutions did it make before reaching the earth? Solution.—(1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1	
.	100	32 verso,
H.	udā vraja	
	tri-śatāmsya nām tu sapta yojana hīyate	
	chatur daśas tu kotti hūyata pamcha-śashti cha	
	kai dinai bhūtale prāpya va <i>da me gana</i> kottama	
	nyāsa sthāponam kriyate	

M 4.

1.	hyā pam	cha trigunita sakhë	36 resto.
		esha deśa pramāṇam samaptam	
iL.	udā	sa lavanasya rāshe koshthatām va kritām rharai	
		eshān chaikām rāśi punar e dhā nītā	
		saptāņām m api chaikā rāśis tulitāņi	
		pamcha saptatyā sahasram bhavet saptāshta gunam kim	
	rā 1	1075 56 adha chchhedain 2000* pa*-bhā° pha- bhā 30 pa* 200	
	esha rāśi	lavaņa pramāņam	
ii.	kākini da	sa bhagasya dadyad ashtadasiti	
	tasyām v	imsati bhāgas cha sata bhāgam prayachchhati	
	naro vaks	shaśa	
1 4.	ii. The ext	i. 'This land measurement is completed' may refer to the fragmentary example at the bottom of folio 32 abt it. 1: 1075:: 56::30 bhā +200 pa' 1: 1075:: 56::30 bhā +200 pa' 200:: 56::4000 bhāra = 30	
	ya^ 3	1 1* yo° 5 chhe° 4608000* ya°-yo° pha° va° 21333 1 360 1 ma° 4	36 verso.
1.	yojanasya	tribhāgārdham sa tribhāga padonakam	
	yā nau di	nat tribhāgena gena gachchhati	
	śā punaφ	pamcha bhāgārdham yojanasya tathāshtamam	
		ti nivartanite – vāyu vega valāhatā	
	yojanānā	mshtau tara satam <i>kena</i> kalena gachchhati	
	di	1 bhā 1 1 gu 1 1 1 3 bhā 3 3 2 5 2+ 8	
		The statement many 2 and 1 days. Know, 21 222 years 4 months as 2 and 1 many 5 at 4.00 000 and 51 220	

^{[36} verso.] i. The statement means 3 ya': 1 day:: 5 yo':: 21,333 years 4 months or 3 ya': \tau_{kb} years:: 5 \times 4,608,000 ya':: 21,833 years 4 months < \frac{5 \times 4,608,000 ya':}{5 \times 4,608,000 ya':: 21,833 } \times \frac{5 \times 4,608,000 ya':}{1,833} \times \frac{5 \times 4,608,000 ya':}{1,833} \times \frac{1}{5 \times 4,608,000 ya':: 21,833 } \times \times \times \times \frac{1}{5 \times 4,608,000 ya':: 21,833 } \times \times

M 5.

L	khagā ekādaśā bhuktā prasritim chaiva meva cha	34 rect
	shtau vada sakhe kim khagam vada sundari	
	pra° 1 kha′ 11 khā 5760 phalam khaga* 63360.	
	esha bāhu pramāṇam	
ti.	kaśchit pumām suvarņas tu· kalā pāda yutam yavam	
	pratyahan sūline šuddhi · kila dattavān	
	pamchābdai māśam evam tu dinai panichadaśas tathāḥ	
	datvā sya sarvāya jūātum ichchhāmi tatvata	
	di 1 1 6* bhā 5 chchhedain 192* yava-tola 1 1 1 1 4 4*	
М 5.	[34 recta.] 1. The problem is: Eleven birds leed on a prayriti (handful) of corn, how many can feed on 8 Kharis of corn? It ends "Say, O friend, say what are the Khagas, O Sundard." If this is correct, the name Sundard, beautiful one, is used in exactly the same way as Lifavati is used by Bhāskara. The solution is 1 pra = 11 khā :: 8 khā : 63,380 khagas which would make 720 prayriti= 1 khāri; but there are many elements of doubt and the application of e-kā bāhu pranamam to the particular problem is not clear. ii. By certain persons one kabī plus one pada and one yara are given in gold daily at the shrine of Sillin. What would be the amount of the cuft in they years, five months and fifteen days	
L	chittritāmgai tāni yata śara-paramparay ārjunena griddhra tayā	34 ven
	spriśaniti 1 śa° 1 yoja° 777 1 8 phalan 940 8 1 222 7 chchhe 1 9 1 5	
ij.	māśakārdha yuto dhyanta vista pamchapamchāśa satereņa vajra maņai	
	labdham tra kathayaśva mūlyam śāṇa chaturbhāgasya siddhārtha pamcha	
	bhāgasya.	
	ku ^c 1 chhe ^c 128* mā ^c -ku ^c 1 mā ^c chhe 40* si ^c -mā ^c sa ^c 55 1	
	[34 verso.] i. The fragment chitrilimgs: drjunens griddhra is extremely interesting although it throws no light on the problem. See Part I. § 47. The statement is puzzling: it may mean \$\frac{1}{k} + \frac{1}{a_0} + \frac{1}{a_{0.0}} \text{: 1 esc: 777 mpc} + 222\frac{1}{4} kro^2 \text{:40} But all the terms except the second are ambiguous. ii. The problem is about a diamond weighing \$\frac{1}{4}\$ mash aks, and obtained for \$\frac{1}{2}\$ 55 eaters. The statement means \$\frac{1}{2}\$ \frac{1}{4} m^2 \text{: 55 ea'}, and indicates that \$128\$ mas = 1 km and that \$40\$ si = 1 mas. See Part I, \$\frac{1}{2}\$ 111. The whole page is an interesting puzzle. (Is the leaf a double one \$\frac{1}{2}\$ Neither side shows any clear lenticle \$\frac{1}{2}\$	

M 6.

i.	sūrya māņasya	37 recto.
	divākarasya ghatikaiχ kim prayatasya vada . nišchitam	
	30 mu° chhe° 2* gha°-mu 500,000,000 gha° 1 pha° yo° 83 333333	
11.	bhāņo ratham sura mahoraga siddhasam(g)hai vidyādhara i ϕ parivritam	
	ahorātru koṭī śatārdharii sa rathanii pryāsyāt — tad bruhi śastra	
	kuśalo vaktum muhūrtam ekena kim gachchhe brūhi me	
	ganakottamā	
	500000000 gha ^c 2 pha ^c yo ^c 166,666,666 ₃	
м с.	[37 recto.] i. The question may be roughly restored. The Sun (sūrya) traverses 500,000,000 yojanas in a day. State with certainty the amount of the journey of the sun (Drynama) in a ghatikā. The statement means 30 ma*: 500,000,000. 1 yha*: \$3,333,333\cdot was and it indicates that 2 yhatika=1 muhūrta (*\frac{1}{10}\) of a day). The origin of the length of the daily journey of the sun, namely 500,000,000 yoyanas, is not known. See Part I, \(\frac{1}{2}\) 100. ii. The chariot of the sun (Buine') is surrounded by the groups of gods, great anakes. Siddham and Vidyandamas. In a day and night its journey is said to be half a hundred kots. Tell me, 0 best of calculators, how much in one muhūrta? 30 mu-: 500,000,000 :: 2 yha* 16,666,886\(\frac{1}{2}\) yo*	
L	bhage bhaved rāśi	37 verso.
	ūrdha chhhedani 108000 viliptāņam liptā 5	
H.	pamchārdha samvatsare bhukte rāśaikā yadi bhānujah brūhi ka tatvajña	
	samaśve vāsareņa kim	
	$egin{array}{cccccccccccccccccccccccccccccccccccc$	
	ürdha chhhedam 108000 viliptānām rāśi adha chchhedam viliptā lipta	
	phalam viliptā 2 esha graha gatim	
111.	udā° rāja yudhisthiro nāma φ pāṇḍu-vamēa	
	[57 verso.] i. The remnant of a problem possibly related to the daily motion of Jupiter, which according to the Sarya Siddania, amounted to very near; 5 minutes of are (lipit). ii. If Brindra (Saturn) nor -schrough a sign in two and a half years, state, O knower of the truth, what will its motion in a solar day be equal to. The solution is 2½ years: 1 sign:: 1 degree: x and x = 1 sign * sin degree = 200,000 + 200 = 120" = 2 minutes of are (not 2 seconds as stated in the text, where rilipital appears to have been written by mistake for lipit). The terms employed are all orthodox except perhaps related fay, but its special use is quite intelligible. See Part I, § 100; and also my Hindu Astronomy, p. 57. iii. This fragment is of interest because of the reference to Yudhishina.	

M 7.

	vyūha pārtham hehayakī ghnata	
	sāyakais chaiva ϕ patti sva-pāda dala sodasai	
	a nyā chatasrā vai hatā tena mahātma vām	
	śarāṇām cha parīmāṇam viśārada	
	śi 1 16 4 a° chhe° 21870 phalam śarā 2624400 1 1 1 1 4 1 2	
	anya 1 pramāņam	
iL.	sūtram eko ratho gaja	
M 7.	[47 recto.] i. This appears to relate to PARTHA the Mahäbhärata hero, who pierced each soldier with 16 (1+\frac{1}{4}) (1+\frac{1}{4}) arrows and slew four divisions of the army. How many arrows did he use? 1 \$i^0:16 (1+\frac{1}{4}) (1+\frac{1}{4})::4 \times 21,870:2,824,400. The abbreviation \$i^0=?: ;\$a^0=anikini.\$ See Part I, \$52. There is a very similar example about Pārtha in the Lildwell (\$67) which has already been quoted (Part I, \$47). 11. Rule.—There is little doubt that this rule relates to the constitution of an army and is exemplified on the reverse (fol. 47 recto.)	
1.	, , , , , , , , , , , , , , , , , , , ,	47 recto.
1.	vichakshanah	47 recto.
1.		47 recta.
1.	chamūs tu pritanās tisras tisras cha anīkīni daśaguņām āhu arakshohanī buddah	47 recta.

M 7—contd.

aksho	hi												
ra°	1	i	esha pati		3 1	3 1	3 1	3	3 1		3	10 1	$\mathbf{g}\mathbf{u}^{\mathrm{c}}$
ga°			•	-	guņi					ath	 9.	218	70
nac				•	5 1 -		,			aja	-	218	
tu°	3	_							_	ara		1093	
									h	aya	,	656	10
												(218	700)

esha akshohini pramānam ||

M 8.

chhedam 480* rakti-pala . . . gunitam jātam 419942 36 pala

to° 8* pale -to° 3 tolen āsti dhā° 12* dhā° 7 dhāņe nāsti am' 4* am' 2 .

ii. Example.—A certain prince Satrudama [The phrase may as well mean: 'a certain prince (engaged in) curbing (his) enemies, (employed or fought so many soldiers)—K. N. D.]

^{[48} recto.] This is a statement belonging to some lost problem and, omitting the change-ratios (marked with asterisks), it means

or 5: 231-- palae :: ? : 419942 116300

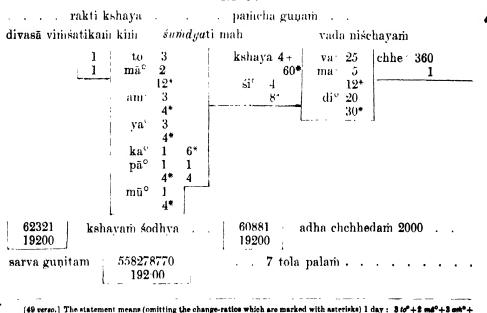
or or $\frac{118800}{118800}$ pages :: 1 : $\frac{118800}{118800}$ $\frac{5 \times 4189420}{118800} \times \frac{118800}{800 \times 950}$ or nearly 180 years.) The abbreviations employed, the changeratios, and the measures are explained in Part I, # 103 and 111.)

M 8--contd.

ı.		phalam bhā° 2 enāsti 44 wa
	•••	pala 2000 bhā" pa° 270 to° 8
		dhā° 2 tola-pala to' 6 tole nāsti dhāņe 12 dhā° 8 chhe° 12*
		gum ^c 3
		chhe 5* ya 2 3* bhā
		5
ii.	yadi din	um ekena esha dattam tad-dvādaša varshena

[48 verso.] This exhibits two mutilated statements of proportion that evidently belong to the same problem i. The first is $\frac{7}{2}:\frac{7}{2}+2\frac{3}{4}\delta^2+3\frac{3}{4}ym^2+2\frac{3}{4}ya^2+\frac{7}{2}=246\frac{3}{4}h\delta -270\frac{3}{4}r^2+6\frac{3}{4}t^2+8\frac{3}{4}\delta^2+...$ ii. If this is given in one day what is that in twelve years, $\frac{1}{2}$ day $\frac{216}{4}ha^2+270\frac{3}{4}t^2+6\frac{3}{4}t^2+\frac{$ M 8.

M 9.



⁽⁴⁹ verso.) The statement means (omitting the change-ratios which are marked with asterisks) 1 day: $3 to^6 + 2 ma^6 + 3 cm^6 + 3 cm^6 + 1 pa^c + 1 ma^c - (+4 ra^c + 4 si^c) :: 28$ years + b months + 20 days: x or 1 day: $\frac{1138}{1000} tolas - \frac{1138}{1000} tolas$ 3 pº 11 mū.

M 9—contd.

ya° 3 yavanāsti ka° 6

. . . ka° 4 kalānāsti pā 1

. . pādanāsti mūdri° 4 pāmu mū° 2

udāharaņam - 11

śūkhyair yajamti devi pratimahni kechit dadāmi devyā . . kamchah krītvā dināra satāni chatvarita dhānakā amdikā raktikā yavā kalā pāda mūdrikā cha | etad mulyam vada me tatra m . sva kim

1 to 12* mū 400 1 1 1	dhā am	1 1 4*		•			dināra			
	ra	1	1* 1	bhā	dn	. 1	dhāņe 	nasu	am	4*
	ya	1	1	bhā						
	ka	1	5 6* 1	bhã						
	рã	1 4*	4_		ل					
	mū] 4*	-							

^{[49} resto.] i. This is the end of the answer to the problem on 49 zerso. See Part I, # 101 (40) and 111.

ii. Example.—The first part is too broken up to make out, but it appears to refer to a git commented with an image of Davi and wership by Sakhyas. (cf. Sakhers, the name of a Saiva sect). [It is possible to read Makhyasir for Sakhyasir, in which case the chiefs of some clam or territory are intended. K. N. D.]

The statement (emitting change-ratios) means—

1 to :: cost 400 :: 1 dha*+1 on*+1 re*+1 ye*+1 he*+1 p4*+1 m6*: 50 dt* +10 dha*+1 on** <or 12 dha*: 400 dt*::

1464 dha*: x and x=5064 dindres>= 50 dt*+10 dha* +1 an*.

M 10.

L	to° 1 va° 5	to° 1 dhā° 1	pha° va° 6 se° 9 gunitam 10	55 recto.
	3	am 12*	1200	
		ra° 1	1* bhā° 1	
		ya° 1	4 3* bhā° 1	
		si° 1	5 2* bhā° 1	
		ka° 1	2 2* bhā° 1	
		pā° 1		
		mū° 1 4*		
	atha śaddrammako .	jjarad	d, vidhānakais dramam śā vimsati-	
	pālā hatai dhānakā	asyaiva sk	andha-	
ii.	to° 1 va° 5 to° 1 3	1 dhā°	1 1* am 1 1* ra 1 1* ya 1 1* 1 12 1 48 1 60 1 192	
	si° 1 1* ka° 1 1 480 _ 1	1* pā°	1 1* mū° 1 1* 1 4800	
M 10.	i. The first statement means- l to: : 5} years :: 1 to:+1 d =6 years, 3, d days. B	 hd°+1 am°+1 ra°+ ut the answer given	ome before folio 49, which has the same knot as 44. 1 $ya^{\circ}+1$ $si^{\circ}+1$ $ka^{\circ}+1$ $pa^{\circ}+1$ $ma^{\circ}: x$, and $x=5\frac{1}{2}\times\frac{3+3+5}{2}=\frac{7+3+5}{2}=\frac{6}{2+5}$ years appears to be 6 years	
			paṁchatriṁ satam	55 vers o.
	divardha tolakasya div	ardha māsak	Kasya .	
	divardha chāṇdikā div	ardha yavas	sya kim mūlyam	
			* Comment of the Comm	

^{[55} serso.] If 1 tota cost thirty-five drammas what will be the price of one and a half totas, one and a half maskakes and one and a half draftkes and one and a half yesus.

M 10—contd.

nyāsa	to°	1	35 1	1 1 2	to°	pha° dram° 58 śe°	31 128
				1 1 2	1* mā° 6		
				1 1 2	1* am [°] 2		
				1 1 2	1* ya° 2		

punānyam

to°	1 1	35 1	1	1	1* 12	1	1* 48	1	1* 192		phalam 58 se°	31 128	
			2	2		2		2		1			

 $Statement. -(i) \ 1 \ to^{c}: 35 \ :: \ 1\frac{1}{4} \ to^{o} + 1\frac{1}{4} \ md^{o} + 1\frac{1}{4} \ am^{c} + 1\frac{1}{4} \ ya^{o}: 58\frac{4}{14} \ dram^{o} \ or \ <1: 35 \ :: \ 319\frac{1}{4}/192: 58\frac{4}{14} >.$ (ii) This is exactly the same proportion with cumulative change-ratios indicated. See Part 1, \$\$ 104, 105

M 11.

kālam ārjana bhakshane nivi sapta-śatānām kaz nyāsa sthāpanam kriyate $bh\bar{a}nd\bar{a} \quad 700$ etat kāleņa ārjana bhaksh *vyaya* rāśi 144

Daily earning $\frac{14}{14}$; given for Bha(vāni) 8 in $5\frac{1}{4}$ days; given for $pa(ra\cdot loka)$ 1 in 32; given for $S\bar{u}(lin) \stackrel{34}{\underset{n \to \infty}{=}}$; $\frac{1}{14\pi}$ years; reserve 700.

700. The daily earning is $\frac{2}{8} = \frac{12\frac{1}{8}}{148}$. The expenditure quantity is $<\frac{8}{13} + \frac{34}{14} + \frac{34}{148} = > \frac{23}{148}$. < The daily loss is $\frac{130 - 163}{148} = \frac{43}{148}$ so 700 will last $\frac{120}{128} + \frac{43}{148} > = \frac{43}{148}$ vers and 'in this time the earning will be consumed.'

Then 1 day: $\frac{214}{148} :: \frac{44}{148} \times 360 : 2559\frac{1}{14}$ and this is the (total) expenditure in $\frac{12}{16} = 4$ years, 7 months, 234 days.

Then the income, $\frac{12}{14}$ days: $\frac{13}{148} :: \frac{44}{148} \times 360 : 2559\frac{1}{148}$, and $\frac{2559\frac{1}{148}}{14859\frac{1}{148}} = \frac{1859\frac{1}{148}}{14859\frac{1}{148}} = \frac{1859\frac{1}{148}}{14859\frac{1}{1488}} = \frac{1859\frac{1}{1488}}{14859\frac{1}{1488}} = \frac{1859\frac{1}{1488}}{14889\frac{1}{1488}} = \frac{1859\frac{1}{1488}}{14889\frac{1}{148$

^{[44} verso.] the capital is seven hundred. What is the time of the consumption of the earnings. M 11.

M 11—contd.

2559 di 1 223 esha vyaya pramāņam 44 recto.

и udā $^{\circ}$ | eka daśārdham utpati sa tribhāga dina dvayāt

pūjārtham sa tribhāgam cha trayodaša . tatāš chayet

sāslīta bhāga dinā trīņi vāsudevasya chārchayet

pādoņa trayodaśāņām cha ashta sārdha dināni chet |

brāhmaņā bhojane dadyā paraloka hitārthinah

sa tribhāgam . jjaram sa pamcha bhāga dinattrayet

pa°

ardham sārdham dine

^{[44} resto. 1. Again 149: 2588 1; 1: 14: 142. This is the expenditure measure. See Part I. 196.

Busingle.—One produces ten and a half in two-and one-third days. For the sake of religion hagives thirteen and one-third in three and one-eighth days; he effers for Visunuva one quarter less than thirteen in eight and a half days. Desiring reward in a future world he gave to Brähmans for food one and one-third in three and one-fifth days two and a quarter in five days

M 12.

ārayet	43 re
sārdha dvādaśam evā tra bhojanē madyam uttamet	
sa tri bhāga trayastrimsai dinaid vāņijyakasya tu.	
bhāṇdāre dvādaśa śata vajārāṇān sthitāsya vai	
eshā vyayasamutpattau kaz kālam brūhi paņdita	
karaņa-vidhānena dvādaša šatasya bhāṇḍāre sti ta .	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	
12 33 bhā 1 1 bhāṇḍā 1200 guṇitāni 1 1 1 360 1 2 3	
[43 recta and also twelve and a half in thirty-three and one third days for the best wine for the consumption of merchants. In the treasure house was stored twelve hundred. Say, O Pandit, how long can this expenditure continue. The statement means: Daily income = $\frac{108}{24} + \frac{18}{64}$. Daily expenditure = $\frac{138}{34} + \frac{14}{64} + \frac{14}{64} + \frac{1}{34} + \frac{14}{64} + \frac{1}{34} + \frac{12}{34} + $	
In the treasure house was stored twelve hundred Say, O Pandit, how long can this expenditure continue. The statement means: Daily income = $\frac{104}{94} + \frac{13}{9}$. Daily expenditure = $\frac{134}{94} + \frac{13}{94} + \frac{14}{94} + \frac{14}{14} + \frac{1}{14} + 1$	4 3 ve
In the treasure house was stored twelve hundred Say, O Pandit, how long can this expenditure continue. The statement means:— Daily income = \(\frac{104}{24} \rightarrow \frac{4}{2} \rightarrow \frac{13}{24} \rightarrow \frac{1}{2} \rightarrow \frac{1}{24} \rightarrow \frac{1}{24} \rightarrow \frac{1}{24} \rightarrow \frac{12}{24} \rightarrow \frac{120}{24} \rightar	4 3 ve
In the treasure house was stored twelve hundred Say, O Pandit, how long can this expenditure continue. The statement means: Daily income = \frac{104}{24} - \frac{1}{2}. Daily expenditure = \frac{134}{24} - \frac{14}{2}. \frac{14}{24} + \frac{1}{14} + \frac{1}{14} + \frac{1}{24} + \frac{12}{24} \frac{120}{240}. The daily loss is therefore \frac{1840}{1840} - \frac{1}{2} - \frac{120}{120} \fr	43 ve
In the treasure house was stored twelve hundred Say, O Pandit, how long can this expenditure continue. The statement means: Daily income = \frac{104}{34} - \frac{1}{8}. Daily expenditure = \frac{134}{34} + \frac{14}{81} + \frac{14}{31} + \frac{1}{14} + \frac{1}{12} + \frac{1}{14} + \fra	43 70

^[48] verso.] Proofs.—2\frac{1}{2}: 10\frac{1}{2}: \frac{1}{24}\frac{1}{2} \times 360: 1782_\frac{1}{2}\frac{1}{2}\theta the total amount earned and 17824\frac{1}{2}\frac{1}{2} + 1200 = 28824\frac{1}{2}\text{c}.

Again 1: \frac{1}{2}\frac{1}{2}\times 28824\frac{1}{2}\text{c}; and lastly \frac{1}{2}\text{c}: 2982\frac{1}{2}\frac{1}{2}\text{c}: \frac{1}{2}\text{c}\text{ the daily expenditure.} Thus each item (can be tested) by the rule of three.

M 13.

	ārdha yukte trayo-daśa sārdham bhavati	42 recto.
	40 bhā° 160 13 eshām chemhedām kritā jātā ekeņa	
	sārdha trayo-daśabhi kim iti $\left \begin{array}{c cccccccccccccccccccccccccccccccccc$	
	. ekena labdha chatvārish shadbhi sampadyate katham $egin{bmatrix} 1 & \ldots & 4 \\ 1 & & \end{bmatrix}$	
	eko labhati chatvāri śansardhasya tu kim bhavet	
M 18.	[42 recto.] This contains portions of a solution that is not, at present, fully understood. The preliminary work is missing and then comes the following proportion 40: 180 ·· 13½ · 54, or cancelling by 40 we get 1: 4 ·· ¾ · 54. The next part is missing but apparently was— 1: 4 ·· 6: 24 1: 4 ·· 3: 12 1: 4 ·· ¾ : 18	
i•	j ātā 54 4adbhi 24 12 ardhā 18 ekatrain 54	42 verso.
	e trai-rāśika karaņa pratyeka mūlya vidhi 📗	
iı.	aparam vakshyāmi vimśānām diva kim prathame khandhakeśu yo	
	bhilikhita apāsya prashņā vidhi 20 1 1 guņaye guņitā 1 1 3	
	jātā $\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
	10 esha vimsānām diva bhavati atra uparimās khandhakasya esha	
	guņākāram bhavati	

^{[42} verso.] 1. A fragment: $24+12+(24+12)\div 2=5\frac{1}{2}$ This stirt gives the three term solution with respect to one price.

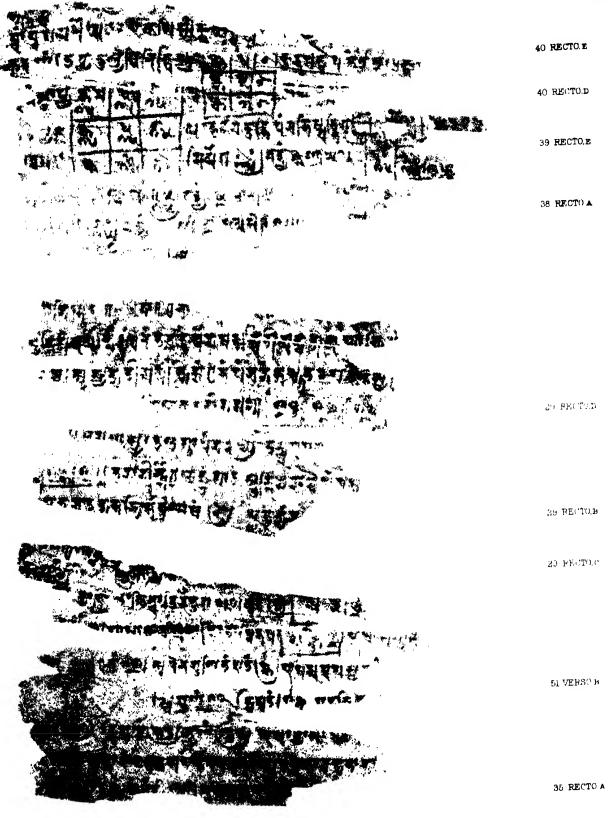
ii. 1 shall instance another......what is that which is written in the first term? The solution is a matter of intelligence. $20\times 1\frac{1}{2}\times\frac{1}{2}=20\times\frac{1}{2}\times\frac{1}{2}:=20\times\frac{1}{2}\times 1=10......$ Now this is the calculation of the foremost term.

M 14.

50 Verso.

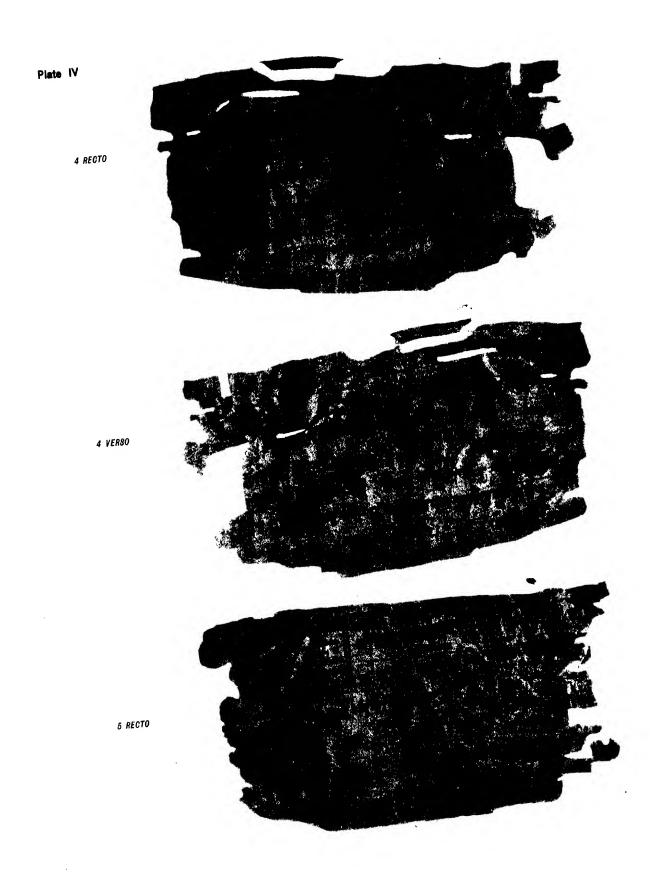
eka rāśis tu kalanā gar	1 dramme	phalam 50		
	1 dramme 100 trapusā 1 2	pnatam 50		
aparam u da ^c sārdha	a dvaye . yasardha di	vardhe labhyateχ ka	1 2 1 2 1 2 1 2	
sūtrain ardhen op	ari samgunya	vardha krameņa ch	2 a	
ardhena ūrdham gunay	e ma pamel	ia saingune I		
	•			
bhajaye labdha panyan	1			
bhajaye labdha panyari	ramma: 100 trapusa :: † 50ted to understand. The satro seed	us to apply to the problem, bu	t it is not clear.	
bhajave labdha panyari	ramma: 100 trapusa :: † 50. ted to understand. The satra wee	us to apply to the problem, bu	t it is not clea r.	50
bhajave labdha panyan	ramma: 100 trapusa :: ½ 50. ted to understand. The satra week vasishta put tra upayogyam bhava	as to apply to the problem, bu ara atuh	t it is not clear.	50
bhājave labdha panyan	ramma: 100 trapusa :: ½ 50. ted to understand. The satra week vasishta put tra upayogyam bhava	us to apply to the problem, bu	t it is not elear.	50
bhājaye labdha panyan	ramma: 100 trapusa :: ½ 50. ted to understand. The satra week vasishta put tra upayogyam bhava tra ganaka rāje	us to apply to the problem, bu fra atuh brāhmaņena	t it is not clear.	50
bhājave labdha panyan 50 verso.] i. The solution is 1 d n-nt. The problem is too mutik sikasvārthe putra pau likhitam Chehhajaka pi sarveshām-m-eva śāstrā	ramma: 100 trapusa :: ½ 50. ted to understand. The satra weel vasishta put tra upayogyam bhava tra ganaka rāje	as to apply to the problem, bu fra atuh brāhmaņena rdhni tishţati	t it is not elear.	50
bhājave labdha panyan 50 verso.] i. The solution is 1 d n-nt. The problem is too mutik sikasvārthe putra pau likhitam Chehhajaka pi sarveshām-m-eva śāstrā	ramma: 100 trapusa :: 1 50. ted to understand. The satra week vasishta put tra upayogyam bhava tra ganaka rāje nām ganitam mū utpamnna m	as to apply to the problem, buttah brāhmaņena rdhni tishtati	t it is not clear.	50
bhājave labdha panyan [50 verso.] i. The solution is 1 d n—nt. The problem is too mutik sikasyārthe putra pau likhitam Chchhajaka pi sarveshām-m-eva šāstrā ādyāvasāne samsāre pašchā šrishţi tadā kart	ramma: 100 trapusa :: 1 50. ted to understand. The satra week vasishta put tra upayogyam bhava tra ganaka rāje nām ganitam mū utpamnna m	as to apply to the problem, butten atuh brāhmaņena rdhni tishtati ahat ana	t it is not elear.	50

^{[50} recto.] At the top of this page is the remnant of a problem, too broken up to make out. The rest of the page is devoted to what appears to be a cotophon. This is not all clear but what remains seems to state that the work was written by a certain Brahman, a prince of calculators, the son of Chhajaka. It also refers to the importance of the science of calculation, which, it is said, we owe to Siva.



RE-ARRANGED FRAGMENTS

Survey of India Offices Calcutta 1923

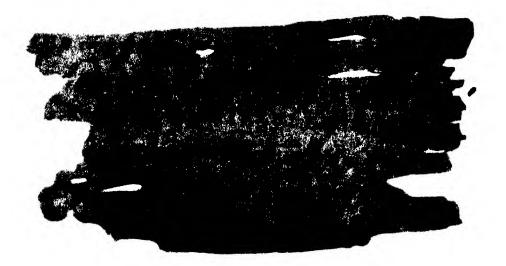








6 RECTO



6 VERSO

Plate VIII 10 RECTO 10 VER80 11 RECTO

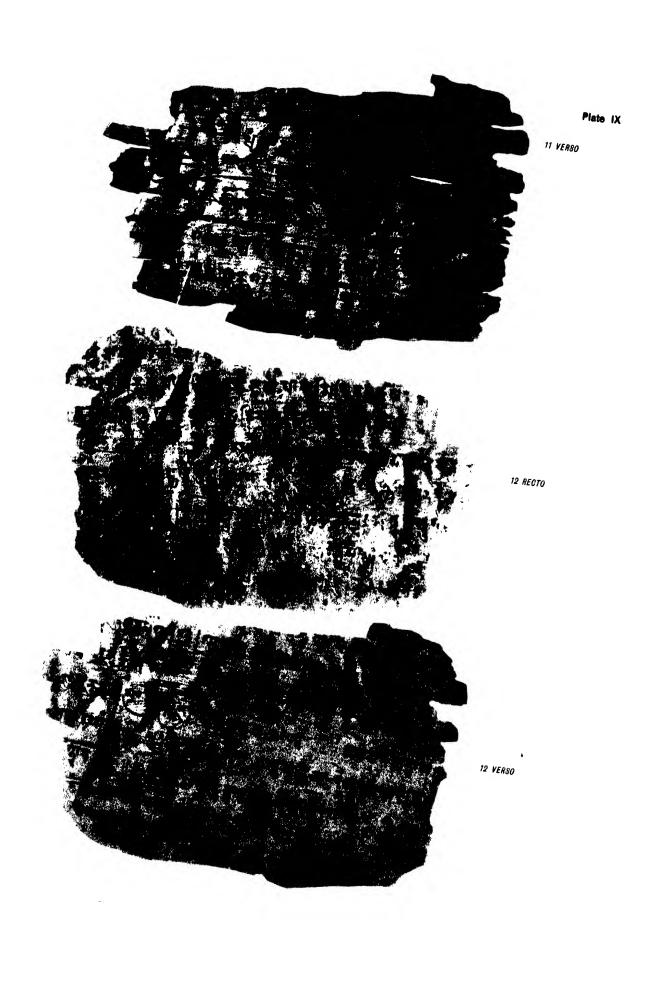
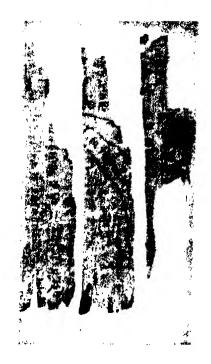


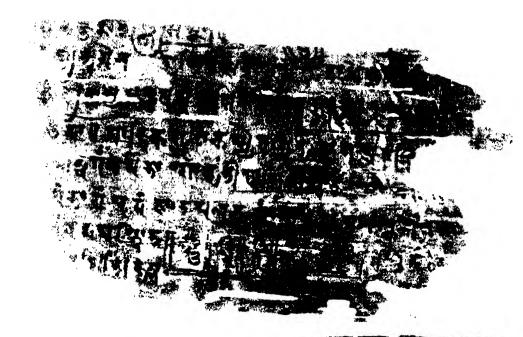
Plate > 2 - 8100 /3**VE**#80 14 RECTO











16 VI R80

17 RECTO

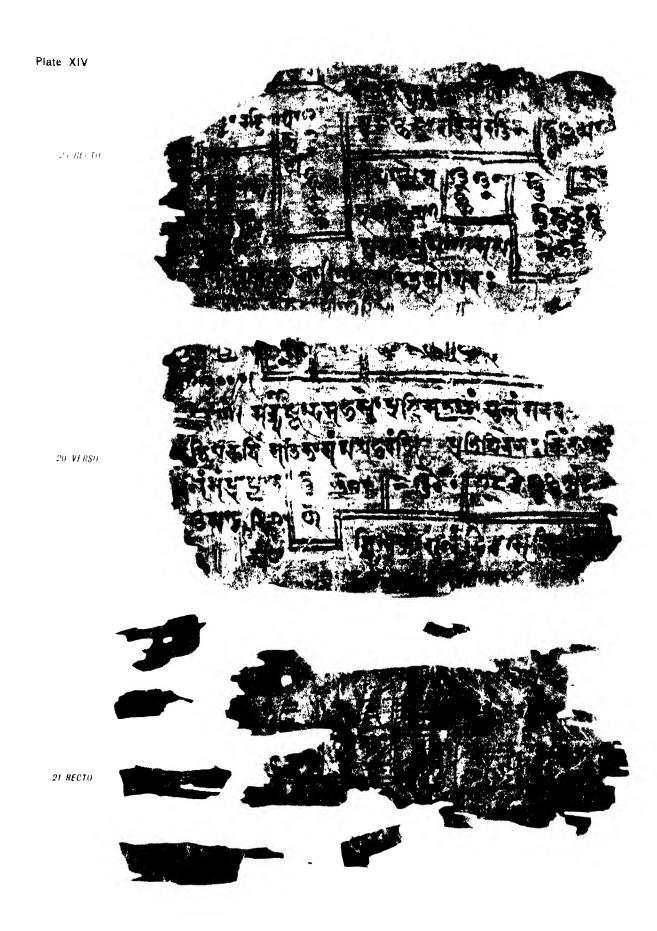
17 VER80



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18 VERSO

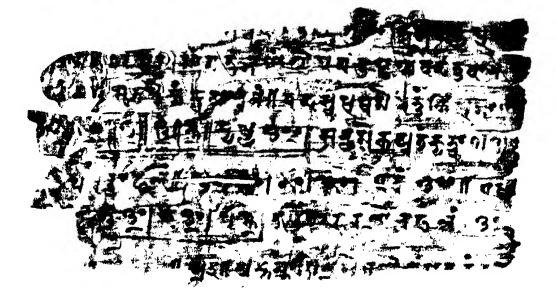




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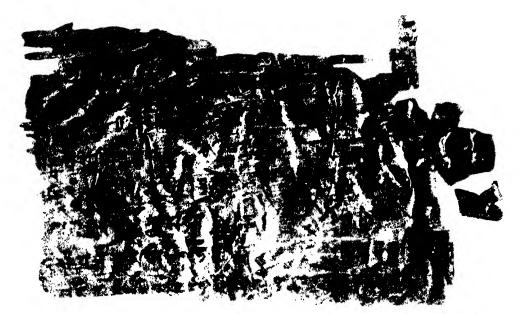
22 Kr CT6



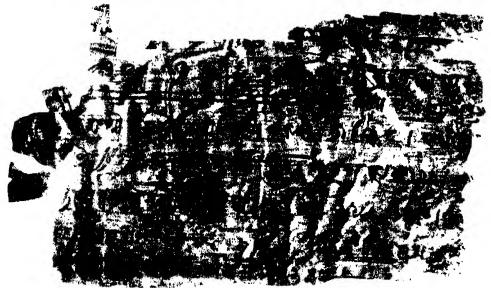
22 VERSO

Plate XVI

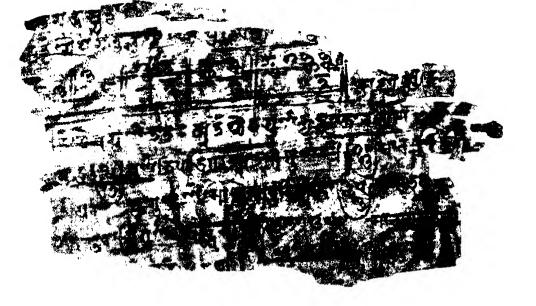
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23 VERSO



24 RECTO



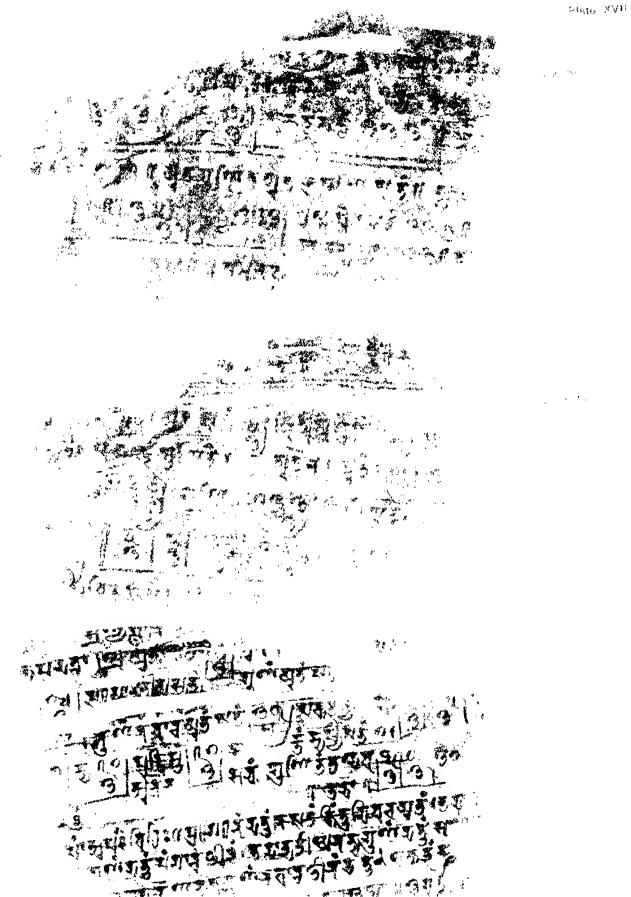
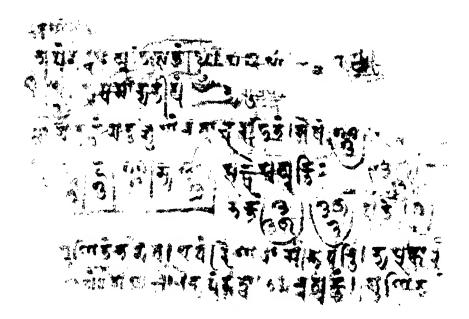
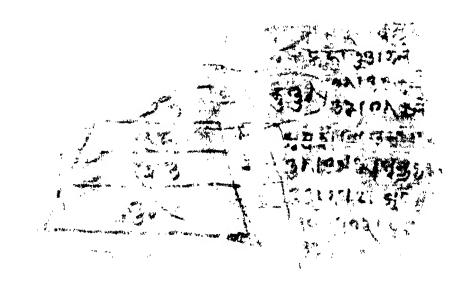


Plate XVIII

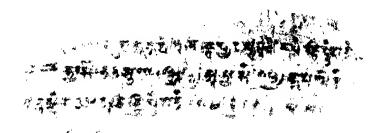
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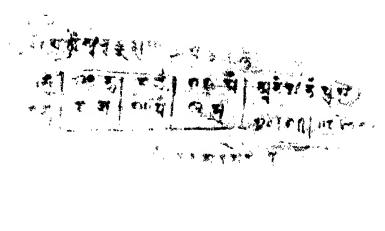


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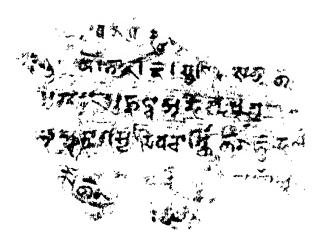




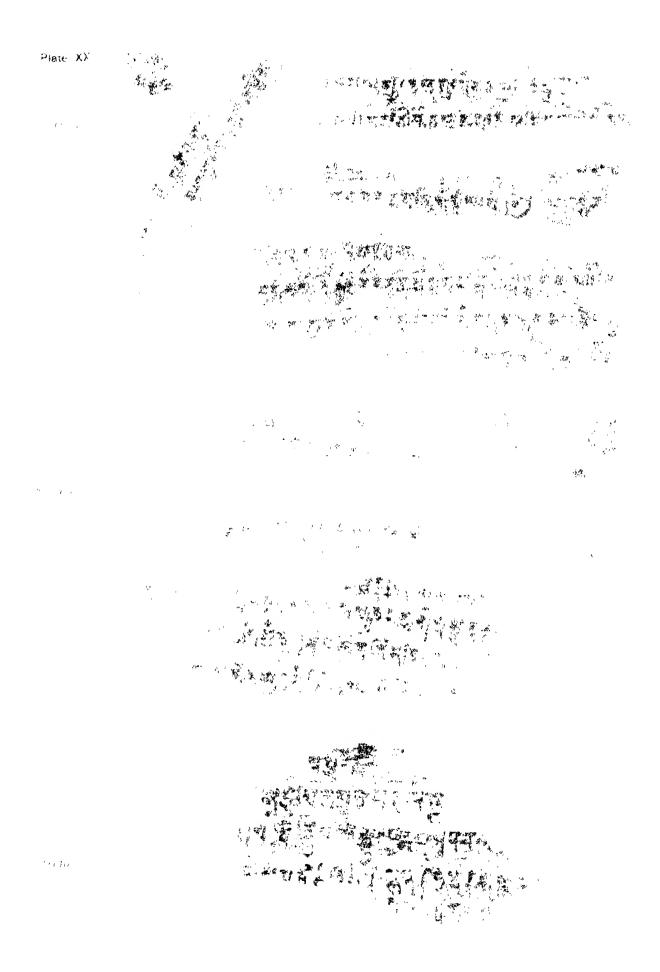
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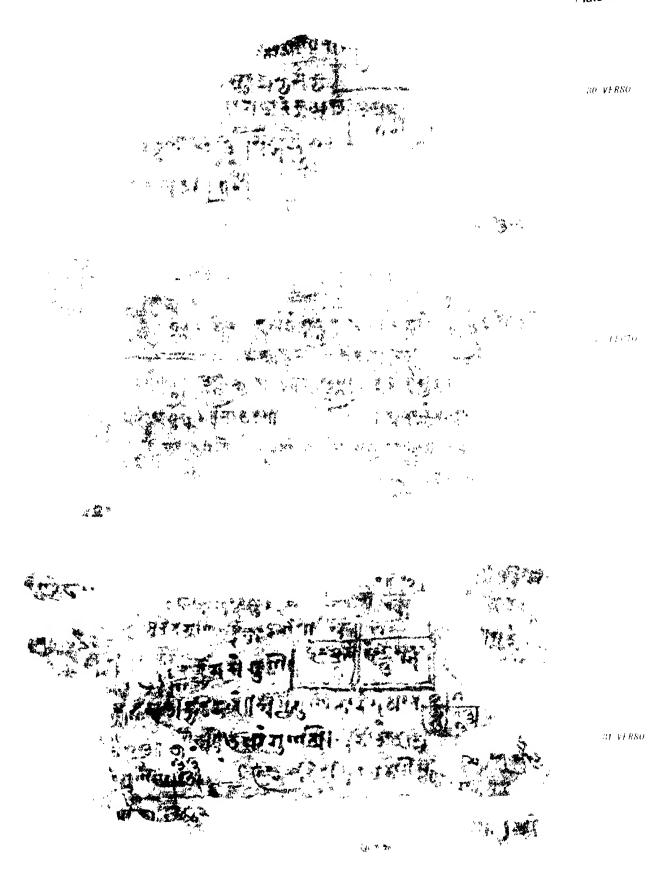


Plate XXII 82 RECTO 22 \$128c 35 RECTO

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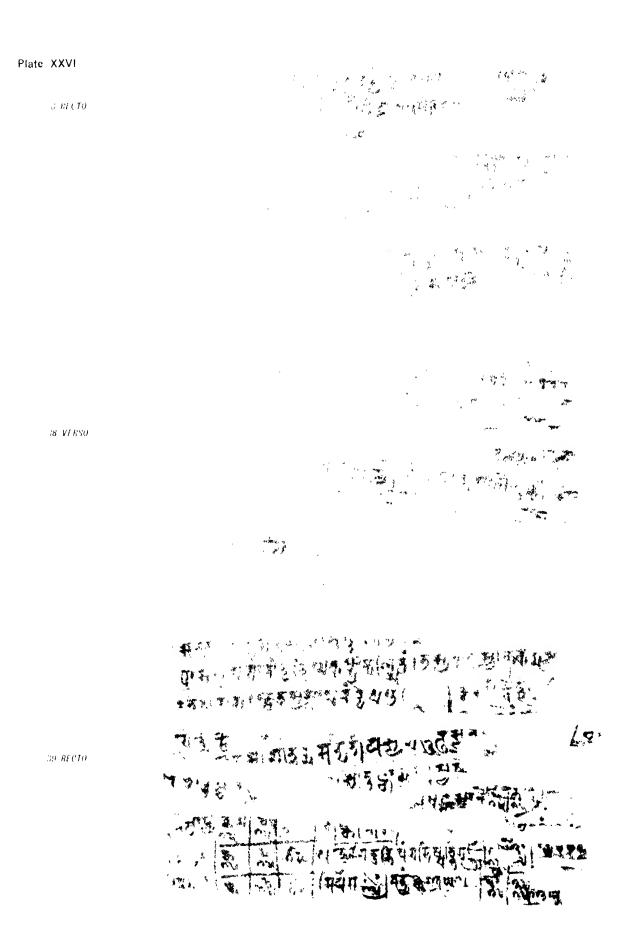
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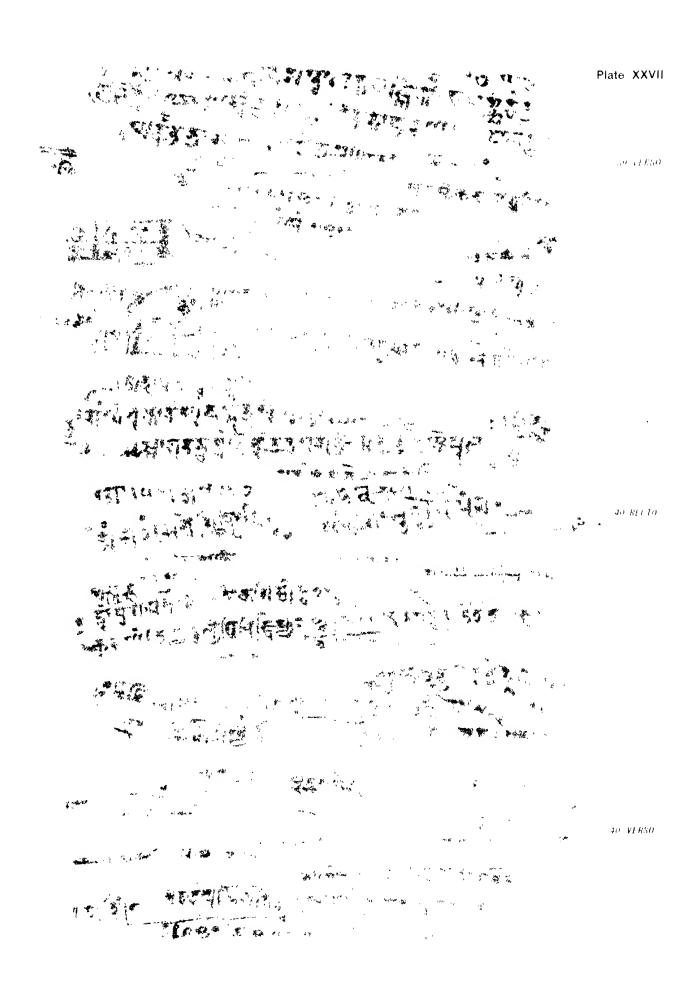


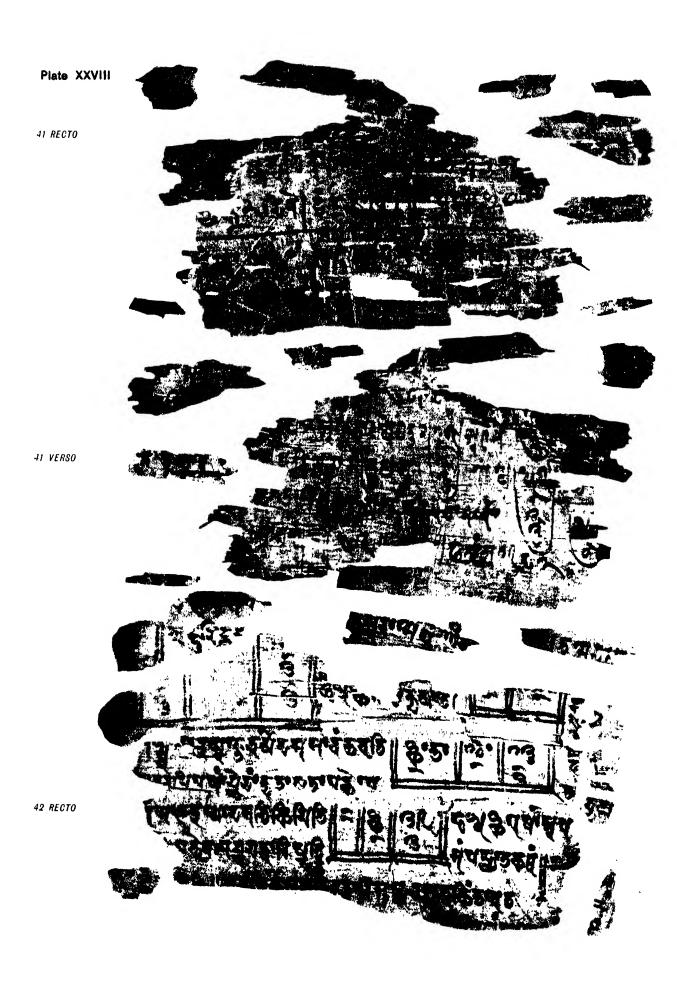
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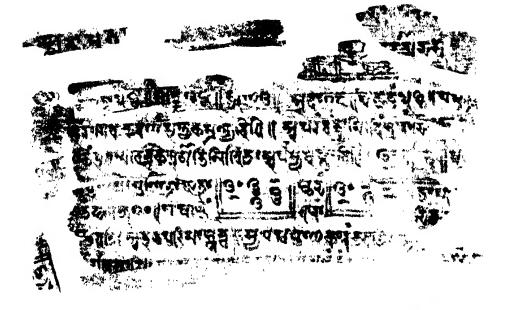
. 2 VERSO



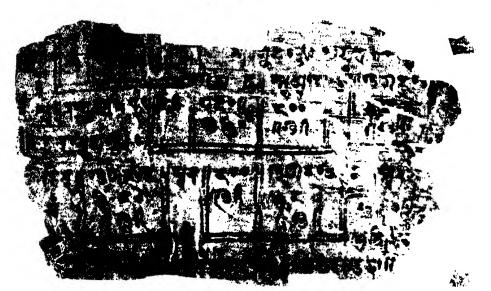




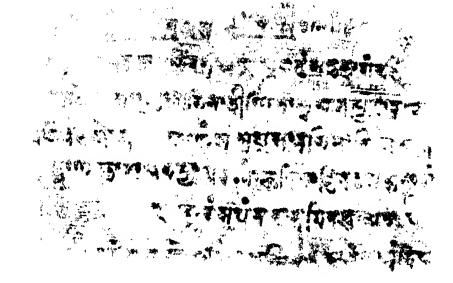
42 VER80



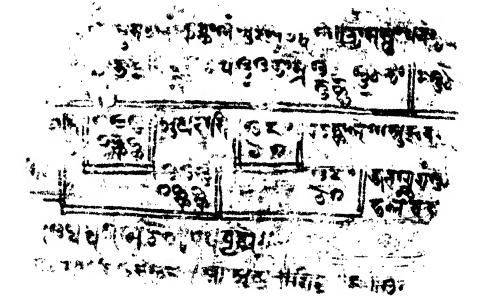




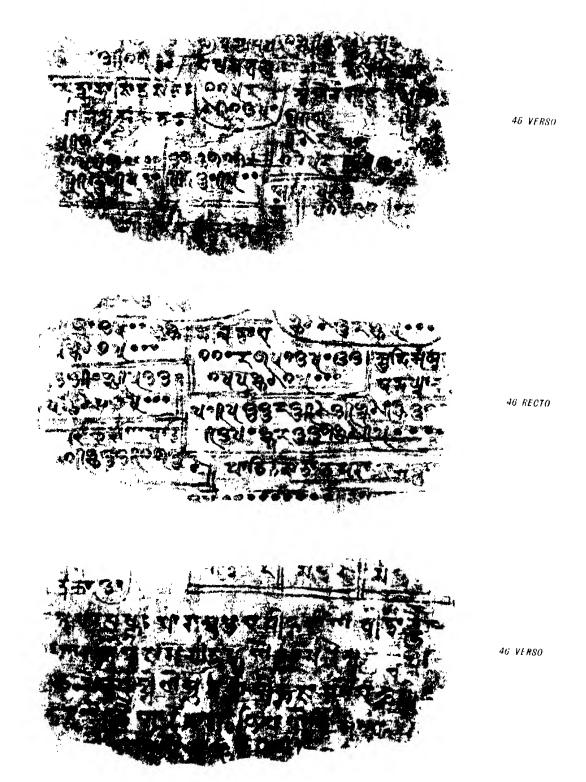
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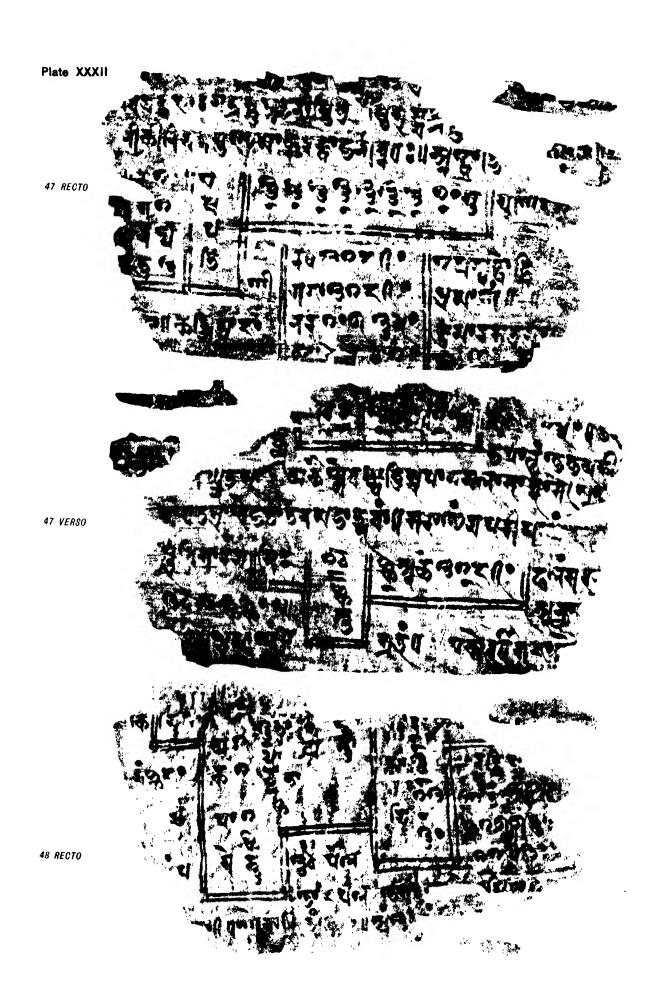


44 Vi R80

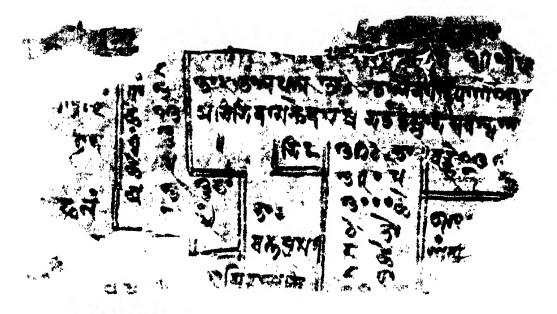


30316











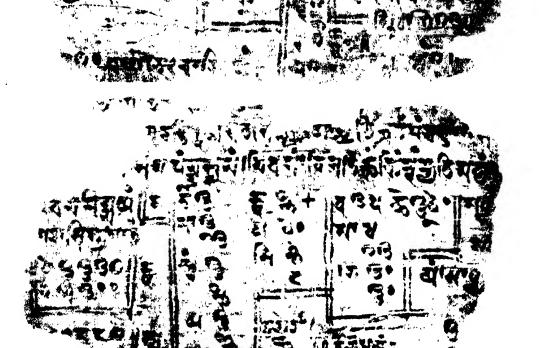
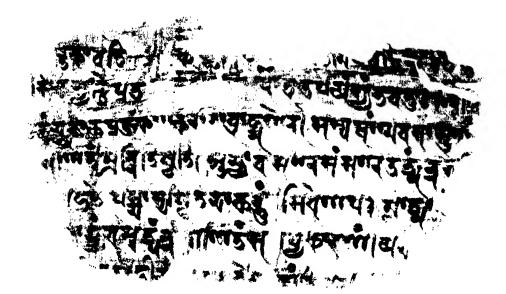


Plate XXXIV

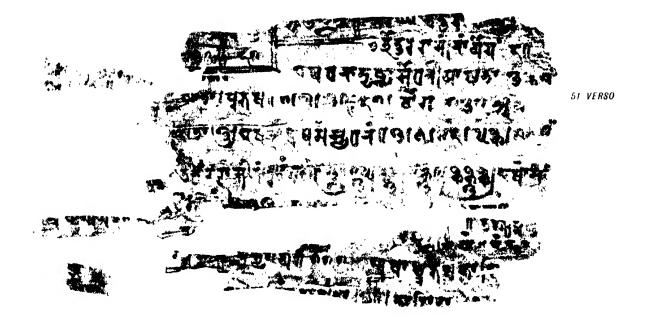
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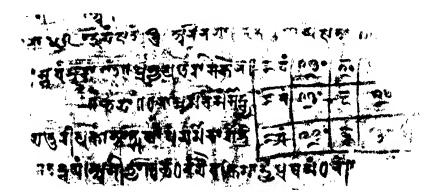


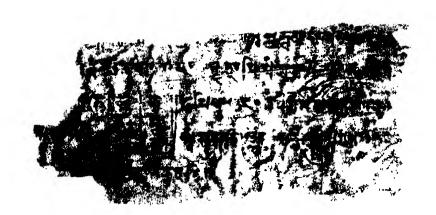
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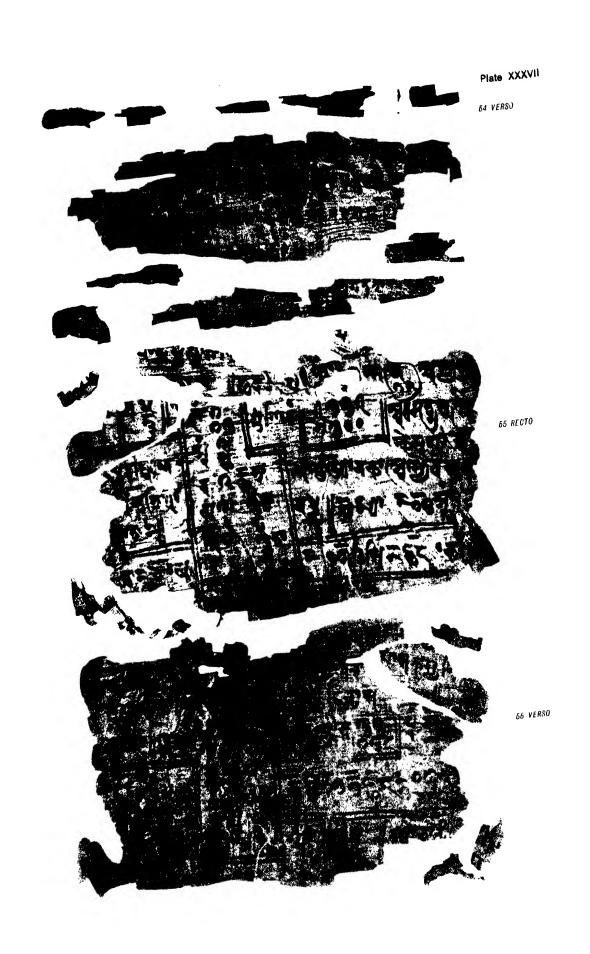




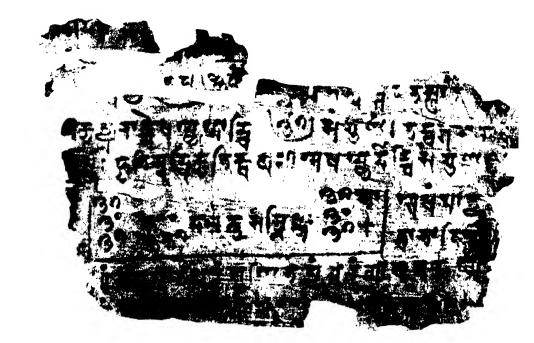








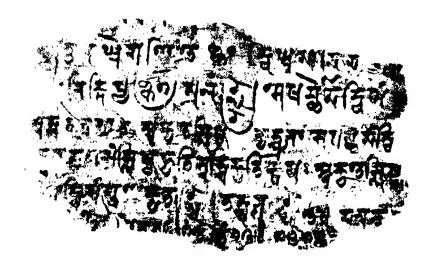


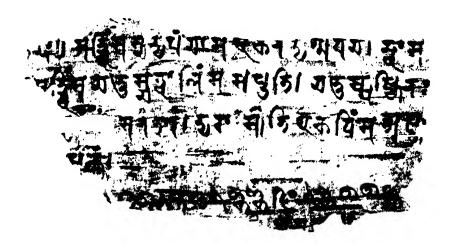












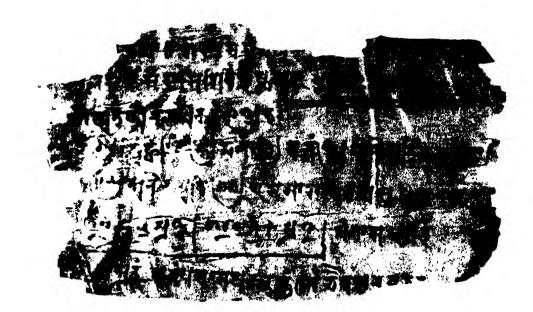
58 REC10



68 VERSO

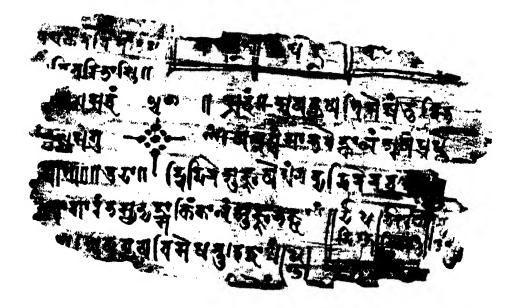
Plate XL

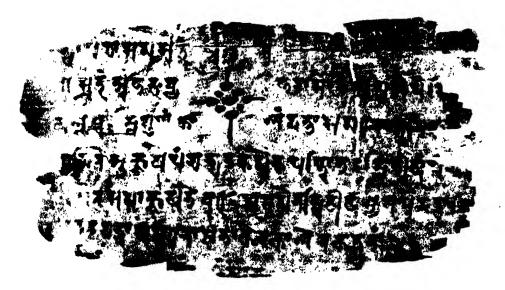
69 RECTO

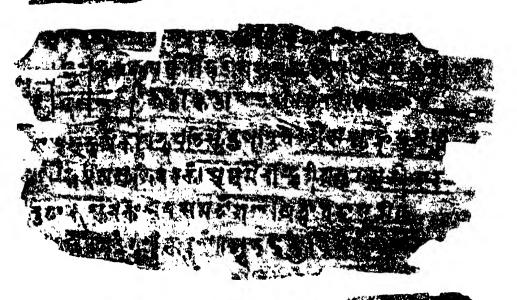


59 Verso is blank

60 RECTO

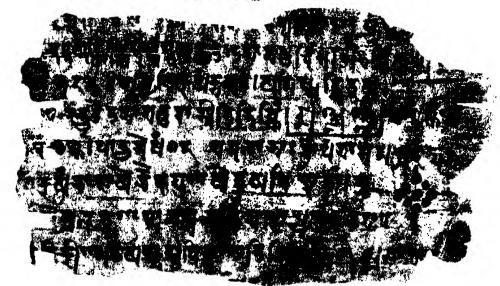








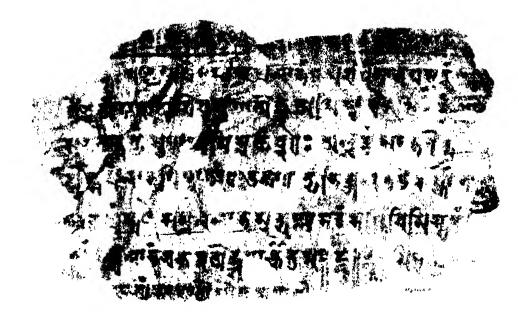
61 VERSO



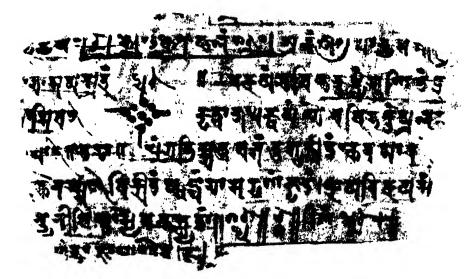
62 KECTO

Plate XLII

62 VERSO



63 REC10

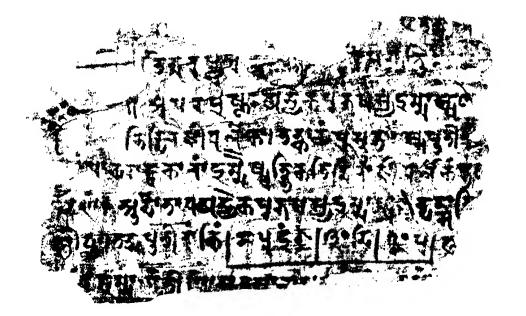








r-4 V1 RSO



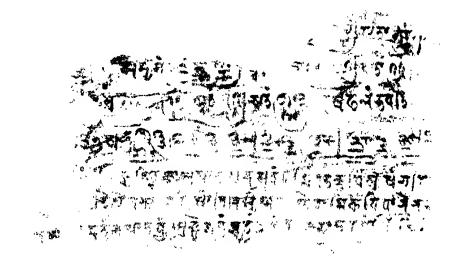
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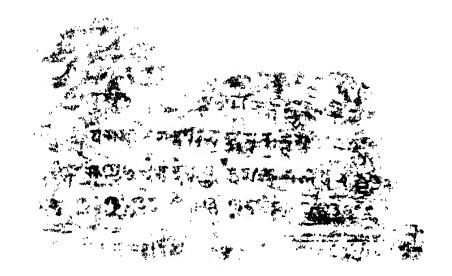
Plate XLIV





66 VERSO





67 VERSO



Plate XLVI

69 RF CT0

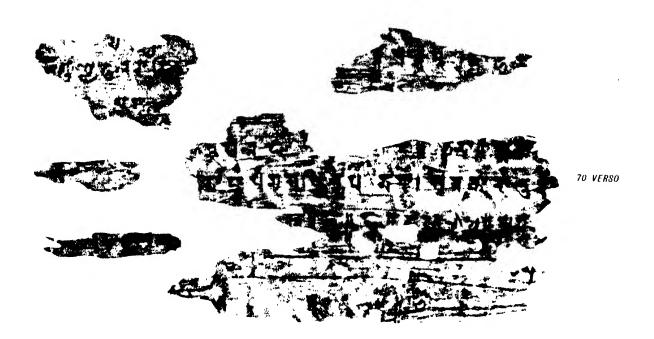




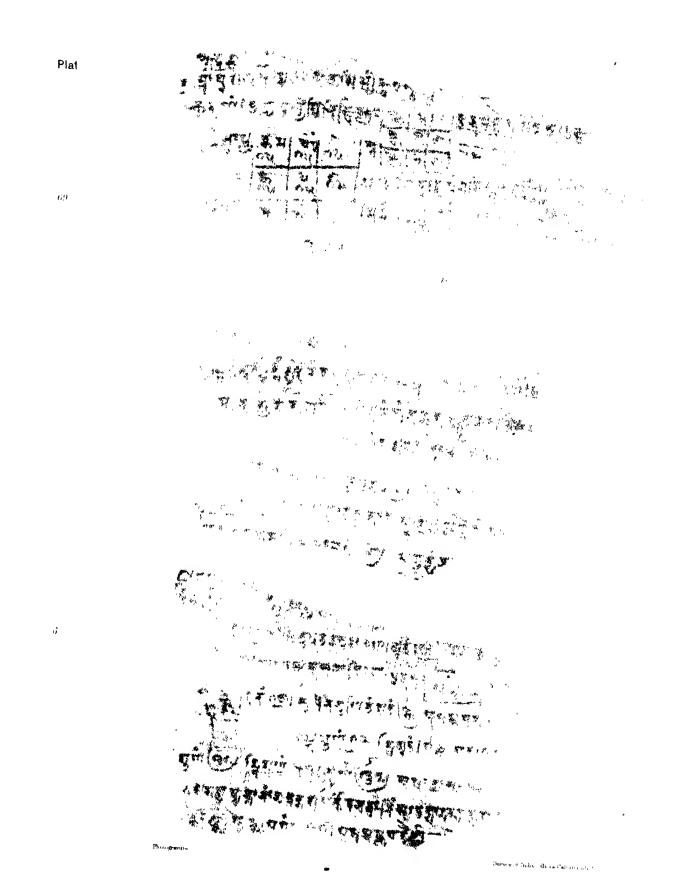
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